

# An eigenvalue problem for nonlinear Schrödinger-Poisson system with steep potential well

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## Abstract

In this paper, we study an eigenvalue problem for Schrödinger-Poisson system with indefinite nonlinearity and potential well as follows:  $-\Delta u + \mu V(x)u + K(x)\Phi u = \lambda f(x)u + g(x)|u|^{p-2}u$  in  $\mathbb{R}^3$ ,  $-\Delta \Phi = K(x)u^2$  in  $\mathbb{R}^3$ , where  $4 < p < 6$ , the parameters  $\mu, \lambda > 0$ ,  $V \in C(\mathbb{R}^3)$  is a potential well, and the functions  $f \in L^{3/2}(\mathbb{R}^3)$  and  $g \in L^2(\mathbb{R}^3)$  are allowed to be sign-changing. It is well known that such a system with the potential being positive constant has two positive solutions when  $\lim_{|x| \rightarrow \infty} g(x) = g_\infty < 0$ ,  $K=0$  in the set  $\{x \in \mathbb{R}^3 : g(x)=0\}$  and  $\lambda > \lambda_1(f)$  with near  $\lambda_1(f)$ , where  $\lambda_1(f)$  is the first eigenvalue of  $-\Delta + \text{id}$  in  $H^1(\mathbb{R}^3)$  (see e.g. Huang et al., J. Differential Equations 255, 2463 (2013)). The main purpose is to obtain the existence and multiplicity of positive solutions without the above assumptions for  $g$  and  $K$ . The results are obtained via variational method and steep potential. Furthermore, we also consider the concentration of solutions as  $\mu \rightarrow \infty$ .

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