

1 Understanding spatial effects in species
2 distribution models

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11 **Abstract**

12 Most Species Distribution Models include spatial effects to improve
13 prediction at unsampled locations and reduce Type I errors. Ecologists
14 tend to try ecologically interpret the spatial patterns displayed by the
15 spatial effect. However, spatial autocorrelation may be driven by many
16 different unaccounted drivers, which complicates the ecological interpre-
17 tation of fitted spatial effects. This study wants to provide a practical
18 demonstration that spatial effects are able to smooth the effect of mul-
19 tiple unaccounted drivers. To do so we use a simulation study that fit
20 model-based spatial models using both geostatistics and 2D smoothing
21 splines. Results show that fitted spatial effects resemble the sum of the
22 unaccounted covariate surface(s) in each model.
23

24 **1 Introduction**

25 Understanding and predicting species spatial patterns through Species Distri-
26 bution Models (SDM) is pivotal for ecology, evolution and conservation (Zurell
27 et al., 2020)). SDMs quantify the relationship between species occurrence or
28 abundance with biotic and abiotic factors in order to gain ecological and evo-
29 lutionary understanding (Elith and Leathwick, 2009)). This way SDMs allow
30 us to predict distributions across landscapes and make future predictions based

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31 on identified drivers, as well as other latent variables such as spatial or spatio-
32 temporal correlation effects. Generally, a SDM is composed by three types of
33 predictors: non-spatial covariates; spatially structured covariates; and spatial
34 or spatio-temporal autocorrelation effects that accommodate the spatial or spa-
35 tiotemporal autocorrelation of the data that is unaccounted by our covariates.

36 Spatial autocorrelation refers to the dependence between pairs of observa-
37 tions in space. In SDMs, spatial effects allow us to predict better and reduce
38 Type I errors in the presence of covariates (Lennon, 2000; Legendre et al., 2002)).
39 In species distribution, spatial autocorrelation may arise as a combination of
40 different factors such as: a geographical range dispersion process, e.g. coloni-
41 sation; unaccounted environmental or biotic drivers; and other highly dynamic
42 processes such as wind and current (Keitt et al., 2002; Dormann, 2007; De Knecht
43 et al., 2010)). These drivers can influence species distribution at all scales, from
44 micrometres to continental and ocean-wide scales (Legendre, 1993)). However,
45 the size, spacing and extent of sampling units will constrain the scale of inferable
46 drivers, and the scale of spatial autocorrelation (Dungan et al., 2002; De Knecht
47 et al., 2010)). In other words, if we sample at a kilometer scale, we cannot infer
48 processes at a smaller scale, and inversely, if our study area is one kilometer
49 long, we cannot infer processes that affect at a larger scale.

50 The statistical interpretation of a spatial effect is related to the sign and
51 link function of our linear predictor, but in general terms, positive values refer
52 to areas where we expect more than that predicted by the rest of the linear
53 predictor and vice versa. Ecologically, many SDM studies have linked spatial
54 effects to biological features like home-range (Keitt et al., 2002)), hot-spot size
55 (Ungaro et al., 2014)) and unaccounted environmental drivers (Borcard and
56 Legendre, 1994)), providing reasonable arguments. For example, given a species
57 that is driven by two environmental variables, one that drives the large-scale
58 variation and another that drives the small-scale variation, the residual spatial
59 pattern of a SDM that includes one of the two covariates will resemble the
60 pattern of the unaccounted explanatory variable, either the large-scale or small-
61 scale one. However, as we mentioned before, reality behind ecological processes
62 is often high dimensional and variables that drive spatial correlation can occur
63 at several different scales. In fact, SDMs are seldom able to identify more
64 than a small portion of all the drivers that influence the distribution of the
65 species under study. This results on spatial effects that are potentially driven
66 by many different unaccounted drivers, diluting their interpretability in terms
67 of an individual process. Although this interpretation issues have sporadically
68 been addressed in the literature (Perry et al., 2002; Diniz-Filho et al., 2003;
69 Dormann, 2007; Legendre et al., 2009; De Knecht et al., 2010; Pasanen et al.,
70 2018; Flury et al., 2021)), many modellers fail to acknowledge this probably due
71 to the lack of an explicit study that shows this.

72 The aim of this article was to provide a practical demonstration that spatial
73 effects are able to smooth the effect of multiple unaccounted drivers, making
74 the biological interpretation of spatial effects rather complicated. To do so, we
75 used model-based spatial models applied over simulated species distribution sur-
76 faces. Simulated fields were based on three spatially structured environmental

77 covariates acting at different spatial scales, and a geographical range dispersion
78 process.

79 **2 Simulation**

80 We used an iterative simulation approach to produce spatially aggregated dis-
81 tributions (link to code in Annex A). At each iteration we added a fixed number
82 of new specimens to the study area based on a probability surface constituted
83 by three spatially structured covariates, each operating at different scales (i.e.,
84 small, medium and large scale), plus a spatial aggregation process driven by
85 the abundance of the neighbouring areas, mimicking the colonization of a plant
86 species for example. As a result, our simulated species distributions were driven
87 by the sum of four different effects (Figure 1): the influence of three explanatory
88 environmental variables operating at different spatial scales (S = small, M =
89 medium and L = large) and a spatial dispersal effect that increase the spatial
90 autocorrelation of the response variable.

91 We simulated fifty different scenarios, selected 100 random samples for each
92 scenario and fitted all the possible combinations of model-based spatial models
93 that ranged from a purely spatial model to a full model that accounted for
94 the three covariates (see Table 1). We used two spatial modelling approaches,
95 geostatistics through the Intergated Nested Laplace Approximation approach
96 (INLA) (Lindgren et al., 2015)) and 2D smoothing splines through the MGCV
97 package for R (Augustin et al., 2013; Wood, 2017)).

98 Our aim was to assess the resemblance between fitted spatial effects and un-
99 accounted covariate surface combinations. Resemblance was assessed through
100 the similarity in pattern score (SIP) (Jones et al., 2016)). SIP scores are bound
101 between zero and one, and high scores denote high similarity in pattern and
102 vice versa. For each simulated scenario, we calculated the SIP score between
103 the spatial effect of every fitted model (rows in Table 2) and all the possible
104 different combinations of covariate surfaces (columns in Table 2), and recorded
105 the absolute difference between the best SIP score and the rest (i.e., SIP dif-
106 ferences calculated per row in Table 2). This way, the spatial effect that best
107 resembled a given combination of covariate surfaces scored a zero and that with
108 the worst resemblance recorded the highest value (see Annex for a more de-
109 tailed explanation of the procedure). As a result, we obtained fifty scores per
110 model and combination of covariate surfaces. Finally, we summarised these
111 scores by their mean and standard deviation. All the R script is available at
112 <https://tinyurl.com/2p8n3e4r>.

113 **3 Results**

114 Results show that fitted spatial effects resemble the sum of the unaccounted
115 covariate surfaces in each model (see highlighted diagonal scores in Table 2).
116 Fitted 2D splines using generalized additive models (GAM) seemed to perform a

117 little worse than model based-geostatistics, probably due to the default selection
118 of knots, but the overall pattern is very similar. This result suggests that spatial
119 effects are able to smooth complex residual spatial patterns originated by a set
120 of covariates that operate at very different scales. For example, model M_M,
121 which only accounts for the mid-scale covariate, estimates a spatial effect that
122 resembles the aggregation of the small-scale and large-scale covariates (S and
123 L respectively). Similarly, the spatial effect of model M_0, which is a purely
124 spatial model (no covariates included), mirrors the combination of all three
125 covariate surfaces (S, M and L). In the particular cases where we included two
126 covariates (i.e., only one unaccounted covariate), spatial effects resembled the
127 missing covariate. At this point, the question is: how many times do SDMs
128 account for all but one driver? One can only speculate this answer but our
129 guess would be: hardly ever.

130 4 Discussion

131 Many studies have analyzed the characteristics of spatial effects to describe the
132 unaccounted ecological mechanisms that drive the distribution of species and
133 try to associate spatial effect patterns to single unaccounted drivers. However,
134 most species distributions are driven by a large number of factors and we are
135 seldom able to identify most of these drivers in our statistical models. As a
136 consequence, SDM spatial effects constitute a combination of many unaccounted
137 factors (Keitt et al., 2002; Dormann, 2007; De Knecht et al., 2010)).

138 This study used a simulation study to illustrate the difficulty in interpreting
139 spatial effects with regards to unaccounted environmental drivers. Readers
140 must realize that did not attempt an exhaustive account of all possible cases, in-
141 stead, we aimed at illustrating our point using a simple and intuitive approach.
142 Fitted spatial effects resembled the sum of the unaccounted covariate surfaces,
143 including spatial patterns originated by covariates that operated at very differ-
144 ent scales. Therefore the biological interpretation of spatial effects may only be
145 valid when the unexplained spatial heterogeneity of the data is characterised by
146 a single dominant driver. However, the environmental and ecological processes
147 that drive the distribution of species are complex and diverse, and one could
148 only arbitrarily assume that there is only one covariate missing in our SDM
149 predictor to make biological interpretations over fitted spatial effects.

150 In this regard, one could use a multiresolution decomposition approach to
151 identify dominant features within the residual spatial correlation of the data
152 (Pasanen et al., 2018; Flury et al., 2020)). This method essentially estimates
153 the range of spatial correlation at different resolutions of the data, or in this case,
154 residuals of the SDM to help us identify the scale-dependent features within the
155 spatial effect of the residuals. Then, assuming that each scale is characterized
156 by a single dominant driver (Perry et al., 2002)), one could relate them to
157 underlying process generating mechanisms.

158 **5 Conclusions**

159 Spatial autocorrelation is a common feature in ecological data. As a conse-
160 quence, spatial correlation models are important to correctly estimate covariate
161 standard errors and therefore reduce Type I errors. Additionally, spatial cor-
162 relation terms estimate the residual spatial structure of the data, improving
163 the predictive capacity of our models at locations that are within range. In
164 ecology, residual spatial patterns are potentially driven by complex multivariate
165 and multi-scaled systems, which can be accommodated by a single spatial ef-
166 fect. Therefore, the biological interpretation of spatial effects is very difficult. A
167 multiresolution decomposition of residual spatial patterns (Flury et al., 2020))
168 could help us identify the scale-dependent features within the spatial correlation
169 structure of the residuals assuming that each scale is characterized by a single
170 dominant driver.

171 **6 Figure and Tables**

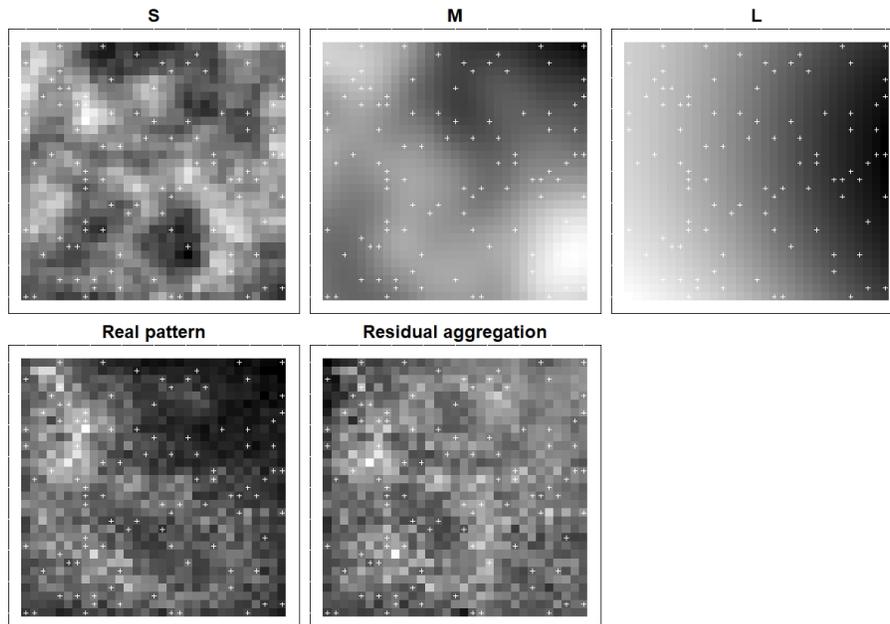


Figure 1: Visualization of the different autocorrelated drivers that influence the abundance pattern in a simulated scenario. S, M and L refer to the small, medium and large scaled covariate fields, respectively. Residual aggregation refers to the geographical range dispersion. White crosses refer to the simulated 100 samples.

Model	Linear predictor	Missing covariates
M_0	$\beta_0 + W$	S, M & L
M_S	$\beta_0 + S + W$	M & L
M_M	$\beta_0 + M + W$	S & L
M_L	$\beta_0 + L + W$	S & M
M_ML	$\beta_0 + M + L + W$	S
M_SM	$\beta_0 + S + M + W$	L
M_SL	$\beta_0 + S + L + W$	M
M_SML	$\beta_0 + S + M + L + W$	–

Table 1: Summary of fitted models. W refers to a geostatistical spatial correlation term, S , M and L refer to the small, medium and large scale covariates, respectively.

Combination of drivers

Model	Residual	S	M	L	S & M	S & L	M & L	S, M & L
M_0	0.62 (0.14)	0.30 (0.13)	0.27 (0.18)	0.35 (0.22)	0.11 (0.06)	0.17 (0.08)	0.12 (0.15)	0.01 (0.02)
M_S	0.56 (0.18)	0.66 (0.22)	0.19 (0.16)	0.25 (0.19)	0.33 (0.17)	0.41 (0.16)	0.01 (0.03)	0.16 (0.12)
M_M	0.47 (0.17)	0.19 (0.15)	0.71 (0.25)	0.26 (0.22)	0.26 (0.21)	0.04 (0.08)	0.37 (0.21)	0.11 (0.14)
M_L	0.55 (0.17)	0.21 (0.14)	0.24 (0.21)	0.78 (0.35)	0.04 (0.04)	0.29 (0.20)	0.33 (0.24)	0.08 (0.12)
M_SM	0.34 (0.17)	0.50 (0.24)	0.61 (0.28)	0.07 (0.13)	0.48 (0.26)	0.22 (0.15)	0.21 (0.18)	0.24 (0.20)
M_SL	0.41 (0.23)	0.51 (0.21)	0.08 (0.11)	0.67 (0.35)	0.18 (0.11)	0.53 (0.25)	0.17 (0.20)	0.20 (0.16)
M_ML	0.36 (0.18)	0.06 (0.10)	0.59 (0.24)	0.65 (0.26)	0.11 (0.11)	0.13 (0.14)	0.60 (0.24)	0.16 (0.17)
M_SML	0.09 (0.15)	0.27 (0.16)	0.40 (0.22)	0.43 (0.24)	0.25 (0.16)	0.28 (0.18)	0.40 (0.24)	0.25 (0.22)
M_0	0.50 (0.09)	0.18 (0.10)	0.11 (0.08)	0.07 (0.07)	0.09 (0.08)	0.12 (0.08)	0.04 (0.05)	0.04 (0.05)
M_S	0.50 (0.09)	0.38 (0.17)	0.10 (0.10)	0.08 (0.09)	0.22 (0.14)	0.28 (0.17)	0.02 (0.04)	0.14 (0.11)
M_M	0.48 (0.10)	0.15 (0.11)	0.35 (0.19)	0.03 (0.04)	0.24 (0.16)	0.07 (0.08)	0.23 (0.17)	0.15 (0.14)
M_L	0.33 (0.19)	0.13 (0.13)	0.06 (0.08)	0.16 (0.19)	0.08 (0.10)	0.16 (0.17)	0.11 (0.12)	0.11 (0.13)
M_SM	0.49 (0.10)	0.38 (0.17)	0.36 (0.19)	0.00 (0.02)	0.42 (0.22)	0.23 (0.14)	0.18 (0.14)	0.28 (0.19)
M_SL	0.35 (0.17)	0.25 (0.19)	0.05 (0.08)	0.16 (0.17)	0.16 (0.13)	0.26 (0.19)	0.10 (0.12)	0.18 (0.13)
M_ML	0.33 (0.16)	0.09 (0.10)	0.20 (0.19)	0.14 (0.16)	0.16 (0.14)	0.13 (0.14)	0.23 (0.19)	0.18 (0.14)
M_SML	0.34 (0.17)	0.23 (0.21)	0.20 (0.20)	0.14 (0.20)	0.27 (0.20)	0.26 (0.19)	0.22 (0.18)	0.28 (0.17)

Geostatistics (INLA)

2D splines (GAM)

Table 2: Resemblance between fitted spatial effects, using geostatistics and 2D smoothing splines, against all the possible combinations of covariate surfaces (per simulation). Scores must be read by row, and reflect the difference between the best SIP score and all possible combinations of drivers for each simulation and model. Therefore, lower values represent higher resemblance and have been highlighted in bold. We present the mean difference and standard deviation (in parenthesis). See Annex for a more detailed explanation of the procedure that we followed.

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236 **A Annex**

237 The aim of this annex is to explain the procedure that we followed to create
 238 Table 2. To do so we use a single simulated species distribution (as compared
 239 to 50 simulations in the study) that is also driven by three spatially structured
 240 environmental covariates acting at different spatial scales and a geographical
 241 range dispersion process.

242 We fitted all the models described in Table 1 and we computed SIP scores
 243 between each model’s spatial effect and all the possible different combinations
 244 of covariate surfaces. By doing so, we get Table 3, which displays highest SIP
 245 scores along the diagonal, matching the combination of drivers (columns) with
 246 the covariates that are missing in the fitted models (rows).

Model	Combination of drivers							
	Residual	S	M	L	S & M	S & L	M & L	S, M & L
M.0	-0.01	0.43	0.57	0.49	0.71	0.55	0.73	0.82
M.S	0.12	-0.04	0.73	0.43	0.49	0.25	0.85	0.59
M.M	0.03	0.50	0.19	0.69	0.47	0.72	0.46	0.72
M.L	0.05	0.40	0.75	0.06	0.78	0.33	0.65	0.75
M.SM	0.16	0.03	-0.09	0.81	-0.03	0.48	0.46	0.33
M.SL	0.11	-0.06	0.83	-0.15	0.57	0.01	0.76	0.53
M.ML	0.01	0.64	0.13	0.03	0.57	0.54	0.05	0.57
M.SML	0.22	-0.05	0.17	-0.12	-0.00	-0.12	0.10	0.09

Table 3: SIP scores between fitted spatial effects and all the combinations of covariate surfaces. Scores must be read by row. Values closer to one reflect bigger resemblance between spatial fields.

247 Once we repeat the simulation 50 times we get 50 SIP scores for each position
 248 in the table, which could be summarised by the mean and standard deviation
 249 of these 50 values. However, we decided to use the difference between the best
 250 SIP score for each model and combinations of covariate fields because results
 251 were clearer, i.e. differences by row in the Table 3. This way Table 3 becomes
 252 Table 4, where zero values represents the best SIP score per model (by row) and
 253 the rest of the scores represent the SIP score difference with respect to the best
 254 score by row.

Model	Combination of drivers							
	Residual	S	M	L	S & M	S & L	M & L	S, M & L
M_0	0.83	0.39	0.24	0.32	0.11	0.27	0.08	0.00
M_S	0.74	0.89	0.13	0.43	0.36	0.60	0.00	0.26
M_M	0.70	0.23	0.53	0.03	0.26	0.00	0.26	0.01
M_L	0.74	0.38	0.03	0.72	0.00	0.45	0.13	0.03
M_SM	0.66	0.78	0.90	0.00	0.85	0.33	0.35	0.48
M_SL	0.72	0.90	0.00	0.99	0.26	0.82	0.07	0.30
M_ML	0.63	0.00	0.51	0.61	0.06	0.10	0.59	0.07
M_SML	0.00	0.28	0.05	0.34	0.23	0.35	0.13	0.13

Table 4: The difference in score between the best SIP score and the rest for each model (by row). Values closer to zero reflect bigger resemblance between spatial fields.