

On the use of SuperDARN Ground Backscatter Measurements for Ionospheric Propagation Model Validation

Authors:

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Key Points

- **We introduce an ionospheric model validation technique using SuperDARN ground backscatter.**
- **Performance of the IRI-2016 is best during the daytime of January 2014 and 2018, whilst sporadic-E in June causes significant degradations.**
- **IRI-2016 range errors are seen to be most significant near the terminator and during the nighttime.**

24 **Abstract**

25 Prior to use in operational systems, it is essential to validate ionospheric models in a manner relevant
26 to their intended application to ensure satisfactory performance. For Over-the-Horizon radars (OTHR)
27 operating in the high-frequency (HF) band (3-30 MHz), the problem of model validation is severe
28 when used in Coordinate Registration (CR) and Frequency Management Systems (FMS). It is
29 imperative that the full error characteristics of models is well understood in these applications due to
30 the critical relationship they impose on system performance. To better understand model performance
31 in the context of OTHR, we introduce an ionospheric model validation technique using the oblique
32 ground backscatter measurements in soundings from the Super Dual Auroral Radar Network
33 (SuperDARN). Analysis is performed in terms of the F-region leading edge (LE) errors and
34 assessment of range-elevation distributions using calibrated interferometer data. This technique is
35 demonstrated by validating the International Reference Ionosphere (IRI) 2016 for January and June in
36 both 2014 and 2018. LE RMS errors of 100-400 km and 400-800 km are observed for winter and
37 summer months, respectively. Evening errors regularly exceeding 1,000 km across all months are
38 identified. Ionosonde driven corrections to the IRI-2016 peak parameters provide improvements of
39 200-800 km to the LE, with the greatest improvements observed during the nighttime. Diagnostics of
40 echo distributions indicate consistent underestimates in model NmF2 during the daytime hours of
41 June 2014 due to offsets of -8° being observed in modelled elevation angles at 18:00 and 21:00 UT.

42

43 **Plain Language Summary**

44 Models of the ionised upper atmosphere, a region known as the ionosphere, must be validated using
45 appropriate techniques prior to their use in operational systems. This is of greatest importance for
46 Over-the-Horizon radars (OTHR) that rely on the reflection of radio waves in the 3-30 MHz band
47 from the ionosphere for their operation. The accuracy of OTHR is largely related to the performance
48 of the model ionosphere used to establish target positions, and so it is essential to understand how
49 models behave under different circumstances. We introduce a new technique for validating models

50 using measurements from the Super Dual Auroral Radar Network (SuperDARN) of research radars.
51 Using a dominant feature present within these radar echoes, we perform an example validation of the
52 International Reference Ionosphere (IRI) 2016 by modelling the expected path of radio waves. The
53 performance is seen to be best during winter and typically worse in the evening. Using further
54 information present within the measurements, we diagnose the likely cause of errors to be due to
55 underestimates in a key model parameter. This is confirmed when we offset model parameters using
56 direct measurements of the ionosphere and observe a significant improvement in model performance.

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60 **1. Introduction**

61 By operating in the high-frequency (HF) band (3-30 MHz), radars can regularly see beyond the
62 horizon, with ground ranges exceeding 3,500 km (Thayaparan et al., 2020) in some cases. This
63 beyond line-of-sight (BLOS) propagation is achieved through the use of the ionosphere as a reflector,
64 as within the HF band, this region of the upper atmosphere is refractive and has a profound impact on
65 the path of radio waves. Over-the-horizon radar (OTHR) systems exploit this phenomenon and are
66 unique in their ability to detect targets at extreme ranges, offering an effective solution to the problem
67 of wide-area surveillance.

68 For the successful design and operation of HF systems, it is often essential to model HF propagation,
69 and this is achieved through the combination of a suitable ionospheric model and raytracing solution.

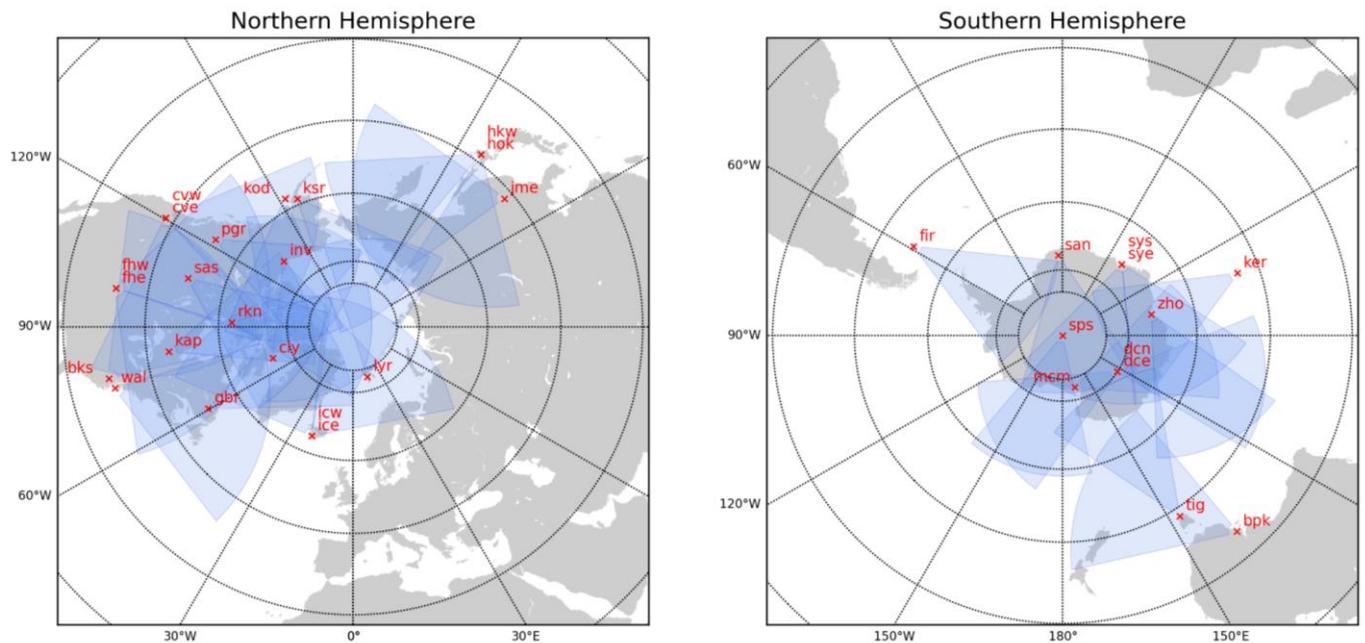
70 The positional accuracy of OTHR target detections is entirely beholden to the representativeness of
71 the ionospheric specification on the immediate ionosphere. HF modelling is required to perform
72 coordinate transforms from slant coordinates to geographical positions and to associate multipath
73 echoes with the correct scatterers. This process is known as coordinate registration (CR) and forms a
74 critical system of any OTHR (Fabrizio, 2013). For this, real time ionospheric models (RTIMs) are

75 employed that assimilate the most up to date measurements of the ionosphere (Fabrizio, 2013;
76 Fridman et al., 2012). Providing a suitable ray tracer is employed, propagation errors, and thus CR
77 positioning errors, can largely be attributed to shortcomings in the specification of the bottomside
78 ionosphere. Due to the large dependence of OTHR accuracy on the ionospheric model employed, it is
79 therefore paramount to understand the performance and error behaviours of models prior to use in
80 operational CR systems if accurate and reliable OTHR target positioning is to be expected.

81 Typical validation methods for assessing ionospheric models include examination of peak density
82 parameters (Shim et al., 2011; Themens et al., 2017), integrated profile densities (Chen et al., 2020;
83 Chou et al., 2023; Themens & Jayachandran, 2016) and topside in situ satellite densities (Shim et al.,
84 2012; Themens et al., 2019). In the context of the oblique propagation encountered in many HF
85 systems, these techniques are of limited suitability as they provide little insight to the cumulative
86 effect of ionospheric density gradients on HF ray paths which are limited to the bottomside
87 ionosphere. Validation efforts must assess the full climatology and latitudinal structuring of the
88 ionosphere if a truly holistic assessment is to be made. Furthermore, typical OTHR measurements
89 such as backscatter soundings that may provide an alternative avenue are often highly restricted due to
90 the classified nature of the systems. A relatively dense global data set of publicly available oblique HF
91 soundings covering at least a full solar cycle are required to facilitate the global validation of
92 ionospheric models. For the real time ionospheric models (RTIMs) employed in operational OTHR
93 systems, suitable validation should also be capable of assessing the model at high cadences besides
94 just assessing climatological performance. Validation of models with consideration to all these factors
95 necessitates the development of new model assessment techniques.

96 The Super Dual Auroral Radar Network (SuperDARN) is a network of HF coherent scatter research
97 radars operating in the range of 8-20 MHz (Chisham et al., 2007; Greenwald et al. 1995; Nishitani et
98 al., 2019) that provides a suitable data set. Over 35 SuperDARN radars are distributed across both
99 hemispheres at latitudes poleward from 30° either side of the equator as shown in Figure 1. This
100 expansive deployment provides an unparalleled coverage of ionospheric plasma dynamics at mid- to
101 high-latitudes. The large field of view (FOV) of the radars, often between 51.84° and 77.76°,

102 combined with OTH propagation permits even single SuperDARN radars to cover vast geographic
 103 areas. Measurements with radars of the SuperDARN design have been conducted since the first radar
 104 was installed in 1983 at Goose Bay in Canada (Greenwald et al., 1985) and are regularly performed in
 105 real time at most of the radar sites, thus offering an expansive data set of backscatter data.
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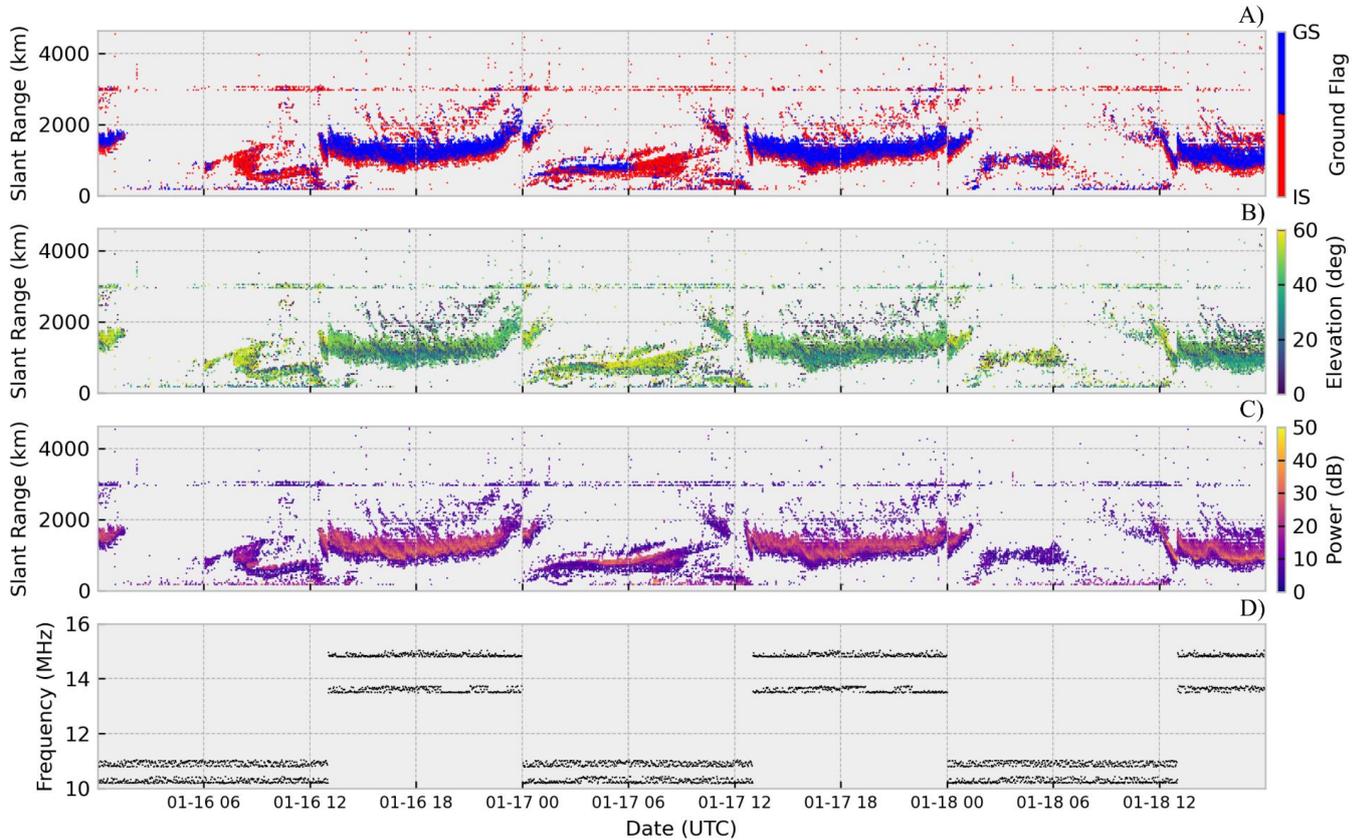


107
 108 *Figure 1. SuperDARN geographical coverage maps for a ground range of 3,500 km for all active radars as of January 2024.*
 109 *Parallels are plotted at 15° intervals.*

110 Whilst signals backscattered by field aligned ionospheric irregularities are of primary interest to much
 111 of the community due to the information they provide on bulk plasma drifts, a significant proportion
 112 of the data provided by SuperDARN soundings is of ground backscatter (GB) origin. GB echoes can
 113 typically be distinguished from ionospheric scatter (IS) due to their near zero doppler shift and other
 114 features characteristically different from IS, and so provide a useful secondary measurement within
 115 SuperDARN soundings. It is worth noting that at times, very slow moving IS may be improperly
 116 flagged by the SuperDARN processing procedures and can pollute GS echoes. An example summary
 117 plot of backscatter from the Blackstone SuperDARN radar beam 16 for the time period 16th to 19th
 118 January 2014 is demonstrated in Figure 2, showing the presence of GB echoes. This beam is 14.58°
 119 from boresight at zero elevation and corresponds to a bearing of -25.42° as presented in Figure 3 and

120 is the focus of this paper. We use the standard SuperDARN convention of zero-indexing when
121 referring to beam numbers.

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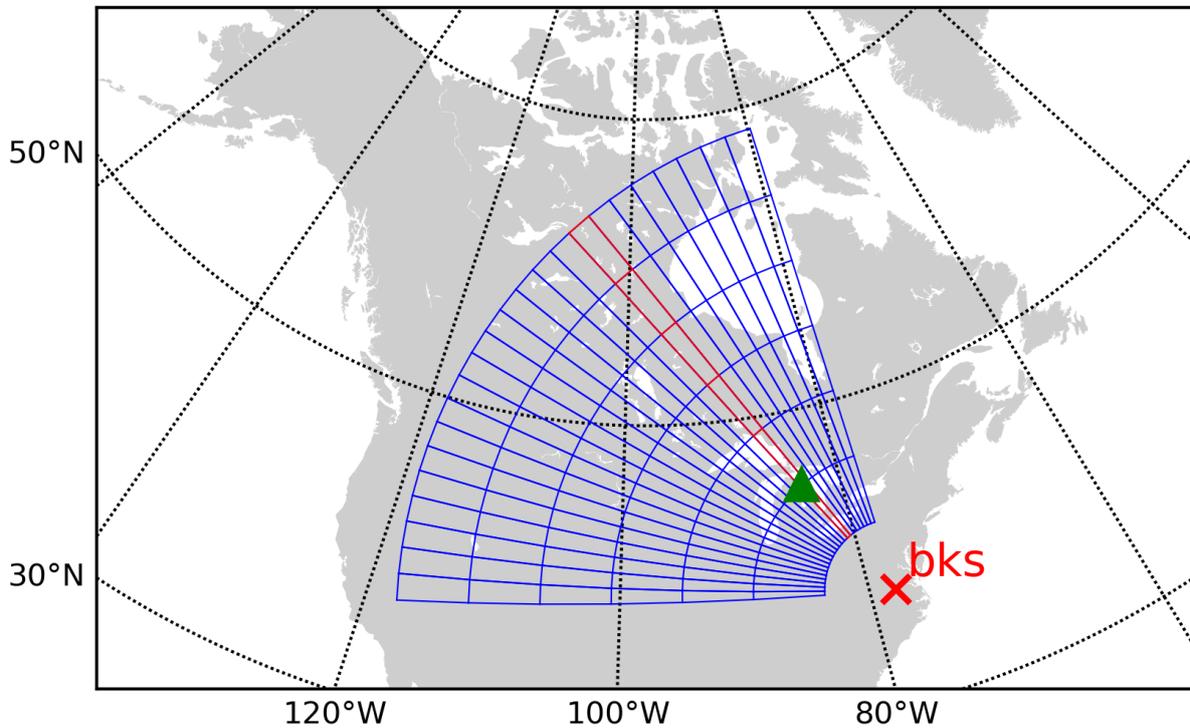
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124 *Figure 2. Summary data plot for the Blackstone radar Beam 16 between 16th and 18th January 2014, showing a dominating*
125 *presence of ground backscatter echoes and the operation of the radar in a dual frequency sounding mode. The presented*
126 *ground flags are from the standard SuperDARN fitacf files and no manual flagging has been performed. Panel B shows the*
127 *backscatter elevation angle of arrival estimates by the SuperDARN interferometer array calculated using the standard T_{diff}*
128 *estimate provided in the hardware data file for the Blackstone radar without calibration. Panel C provides signal to noise*
129 *ratio values from the SuperDARN ACF estimation whilst panel D presents the transmission frequency.*

130 GB measurements have found increasing utility over time, showing use for interferometer calibration
131 (Jiang et al., 2022; Ponomarenko et al., 2015; Ponomarenko et al., 2018) and real time determination
132 of ionospheric parameters including foF2 (Bland et al., 2014) and maximum useable frequency
133 (MUF) (Hughes et al., 2002). Further applications include analysis of short-wave fadeout events by
134 Chakraborty et al. (2018) and derivation of ionospheric winds by Theurer and Bristow (2017).
135 Climatological studies using GB data have also been performed by Ponomarenko et al. (2010),
136 Ponomarenko and McWilliams (2023), Oinats et al. (2016) and Koustov et al. (2022) to determine

137 occurrence rates, with Ponomarenko et al. (2010) additionally assessing the impact of the underlying
138 ground scattering surface.

139



140

141 *Figure 3. Geographical coverage of the Blackstone radar's 24 beams spaced at 3.24 degrees. Markers are provided in*
142 *ground range for intervals of 500 km. Beam 16 is indicated in red with the Alpeña ionosonde marked downrange by a green*
143 *triangle.*

144 HF propagation modelling may be used to represent the expected signal paths of GB echoes present
145 within SuperDARN backscatter, where differences may be predominantly attributed to the
146 ionospheric model. By modelling this data over a range of time periods and geographical areas, it is
147 possible to make comparisons between simulated SuperDARN GB echoes and those present within
148 the actual data set to gain a rigorous understanding of shortcomings in the model. By generalizing this
149 approach, the technique may be applied to any SuperDARN radar in the network, thus unlocking
150 almost all of the available SuperDARN GB data. Other HF radars with similar data sets may also
151 provide candidate validation opportunities.

152 A dominant feature within backscatter time series is that of the leading-edge (LE), which corresponds
153 to the skip distance. This may be used to make direct comparisons between the SuperDARN radar and

154 modelled data sets. This provides partial information regarding foF2, hmF2, and F-peak thickness
155 when combined with elevation angle measurements. To the first order, the group leading-edge
156 distance, P_{min} , is

$$P_{min} = \frac{2h_v}{\cos\left(\frac{\pi}{2} - \theta_{max}\right)} \quad 1$$

157

158 that is a form of Martyn's theorem for a planar earth geometry and vertically stratified ionosphere,
159 where h_v is the virtual height of reflection and θ_{max} is the maximum transmission elevation (Martyn,
160 1935). Here, the maximum elevation angle may be predicted by Snell's law under the same
161 assumptions of Equation 1 when ignoring particle collisions and Earth's magnetic field using the
162 following relation

$$N_{max} = \frac{f^2 \sin^2 \theta}{81} \quad 2$$

163 Where N_{max} is the maximum electron density and f is the transmission frequency (Davies, 1965).
164 Further to the LE, the provision of elevation angle estimates permits assessment of echo distributions
165 in group range-elevation space as an opportunity for model diagnostics.

166 In this study, we introduce a comprehensive method for the validation of ionospheric models at
167 minutely resolutions in a manner appropriate to OTHR and oblique HF systems in general by utilizing
168 the vast data set offered by the SuperDARN radars. A SuperDARN simulator is first demonstrated in
169 section 2.1 utilizing two-dimensional numerical ray tracing (NRT) with inclusion of power
170 calculations using modelled antenna array patterns established in section 2.2. Extensive data
171 processing is then performed in section 2.3 to permit proper comparisons between model and
172 experimental data. We then perform an example assessment of the International Reference Ionosphere
173 2016 (IRI-2016) using this method, including analysis of LE variations in sections 3.1 and 3.2,
174 comparison of echo elevation-range distributions in section 3.3, testing of simulated backscatter using
175 ionosonde driven peak density parameters in section 3.4, and diagnosis of model errors in section 3.5
176 using echo elevation-range distributions simulated with offsets to NmF2, hmF2 and the interferometer

177 calibration parameter, T_{diff} . Our analysis is applied herein across the months of January and June in
178 both 2014 and 2018 to encompass summer and winter periods during active and quiet phases of the
179 solar cycle

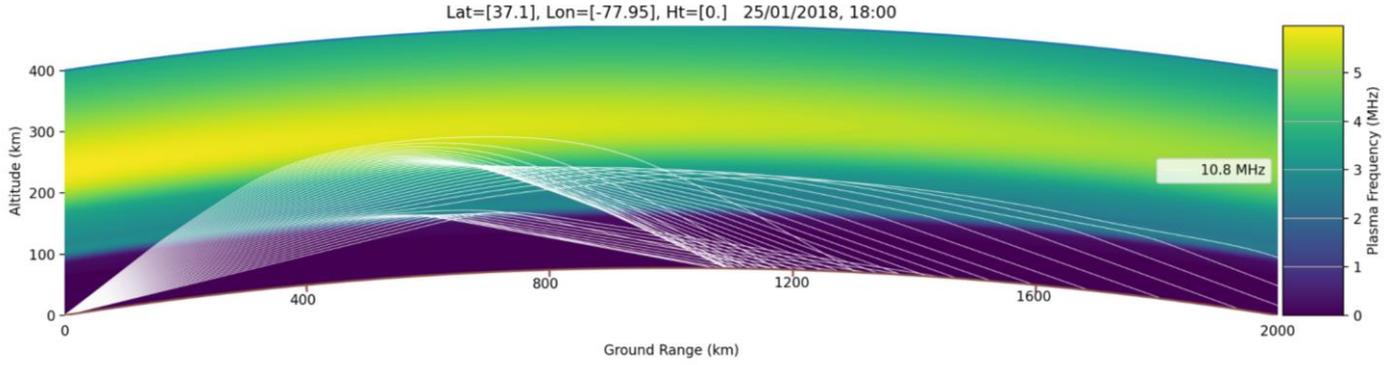
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181 **2. Methodology and Propagation Model**

182 **2.1 HF Raytracing**

183 NRT is a technique widely employed to study HF propagation through the ionosphere and is well
184 suited for simulating SuperDARN backscatter. NRT has been previously used by Perry et al. (2022)
185 for example in the context of SuperDARN to validate the Saskatoon radar's gain pattern. This study
186 makes use of the HFRM (high-frequency raytracing model) 2D NRT toolbox developed by the
187 University of Birmingham's Space Environment and Radio Engineering (SERENE) group and is used
188 to model the expected signal paths for the Blackstone radar beam 16 with the IRI-2016 ionospheric
189 model. It should be noted that the choice of ionospheric model and beam is arbitrary and used only for
190 demonstration of this technique, which may be applied broadly to any beam and ionospheric model as
191 appropriate. An example 2D ray trace for this beam simulated using HFRM is presented in Figure 4.
192 HFRM has previously been employed by SERENE to model multi-static OTHR and uses an improved
193 version of the NRT ray tracer detailed in the work of Coleman (1998), which is based on the
194 Haselgrove set of equations (Haselgrove, 1955).

195 2D ionospheric grids are generated using the IRI once every 15 minutes and linearly interpolated
196 down to the minutely resolution of the SuperDARN data. Whilst this is in excess of the model
197 resolution, a finer generation time step is included to permit future work with assimilative models that
198 operate with greater temporal resolutions. At each time step within the SuperDARN data, a total of
199 350 rays are propagated at elevations between 5° and 60° with frequency set to match that of the data.
200 Ray landing points are then extracted and binned by group range into the same range gate bins as for
201 the SuperDARN data.



202

203 *Figure 4. Example raytrace using HFRM for the Blackstone radar beam 16 at 18:00 UT on the 25th Jan 2018, showing*
 204 *distinct propagation modes via different regions of the ionosphere. Transmission frequency is set to 10.8 MHz.*

205 Due to the conic beam structure of linear arrays, non-boresight beams are spread in azimuth as the
 206 pointing direction of the main lobe varies with elevation (Shepherd, 2017). The SuperDARN array
 207 phasing matrices are configured to form beams at specific azimuths at zero elevation, and so at higher
 208 elevations there is always a mismatch between the stated beam direction and the true propagation
 209 direction. This effect is most significant for higher elevations and beams further from boresight. For
 210 the 2D NRT ray tracer utilized in this study, we restrict propagation to a great circle slice in the
 211 direction of the zero-elevation beam azimuth. This is a limitation of our technique as the modelled
 212 rays will transition a different geographical region of the ionospheric model in comparison to the real
 213 ionosphere. We do not consider this limitation a significant hinderance to our current analysis as F-
 214 region echoes are the focus of this study that typically arrive at lower elevation angles often below
 215 approximately 45° where the conic beam deviations are less pronounced. Beyond this, 2D NRT is
 216 only suitable for weak horizontal gradients as the technique is unable to capture off great circle ray
 217 deviations that cause rays to transition different geographical regions. For the reasons detailed here,
 218 2D NRT when using great circle ionospheres is only recommended for near boresight beams and
 219 conditions where large density gradients are not expected. To calculate the backscattered power for a
 220 given ray, a form of the radar equation must be used and is given by the following (Coleman, 1997):

$$P_r = \frac{P_T G_T G_R}{(4\pi)^3 d_T^2 d_R^2} \frac{\lambda^2 A_{eff} \sigma_0}{L_T L_R L_{Pol}} \quad 3$$

221 Where P_T is the transmitted power, G_T and G_R the transmit and receive antenna gains, λ the
 222 wavelength, A_{eff} the effective scattering area, σ_0 the backscatter coefficient, d_T and d_R the effective

223 distance along the transmit and receive rays, L_T and L_R the ionospheric absorption on the transmit and
 224 receive rays, and L_{Pol} is the polarisation mismatch at the receive array. Here, the effective distance
 225 represents both the group range of the ray flux tubes and the focussing/defocussing of them by the
 226 ionosphere (Coleman, 1997). We take L_{Pol} to be 3dB in order to account for the average mismatch
 227 with the receive antenna due to the ray polarization upon exiting the ionosphere being unknown.

228 The effective area can be considered as the imposed area of a flux tube at the ground, and can be
 229 determined by the following equation (Slimming & Cervera, 2019):

$$A_{eff} = R_e \sin\left(\frac{D}{R_e}\right) \frac{dD}{d\theta} \Delta\theta \Delta\Phi \quad 4$$

230

231 Where D is the ground range, $\Delta\theta$ is the ray fan elevation step, and $\Delta\Phi$ is the azimuthal beamwidth.

232 Calculation of the $\frac{dD}{d\theta}$ term is performed for pairs of rays in a fan.

233 Deviative and non-deviative ionospheric absorption is calculated along the ray path for the case of no
 234 magnetic field using the following equation derived from the Appleton-Hartree equation when
 235 ignoring particle Earth's magnetic field (Davies, 1965):

$$L = \frac{4.34e^2}{\epsilon_0 m_e c} \int \frac{1}{\mu} \left(\frac{N_e v}{4\pi^2 f^2 + v^2} \right) dP \quad 5$$

236 Where e is the charge of an electron, v the electron-neutral collision frequency, ϵ_0 the permittivity of
 237 free space, m_e the mass of an electron, c the speed of light in free space, μ the real refractive index,
 238 and P the group range. Collision frequency is calculated at each point on the ray path with electron
 239 density, neutral density and neutral temperature, with profiles for the latter two provided in the
 240 Appendix 1.

241 Backscatter losses vary widely depending on surface conductivity, roughness, terrain type as well as
 242 incidence angle, and it is known to be difficult to model due to the limited data sets available and the
 243 inherent difficulties with isolating the backscatter loss contribution. Studies of backscatter coefficients
 244 have been conducted around Australia using Jindalee Operational Radar Network backscatter

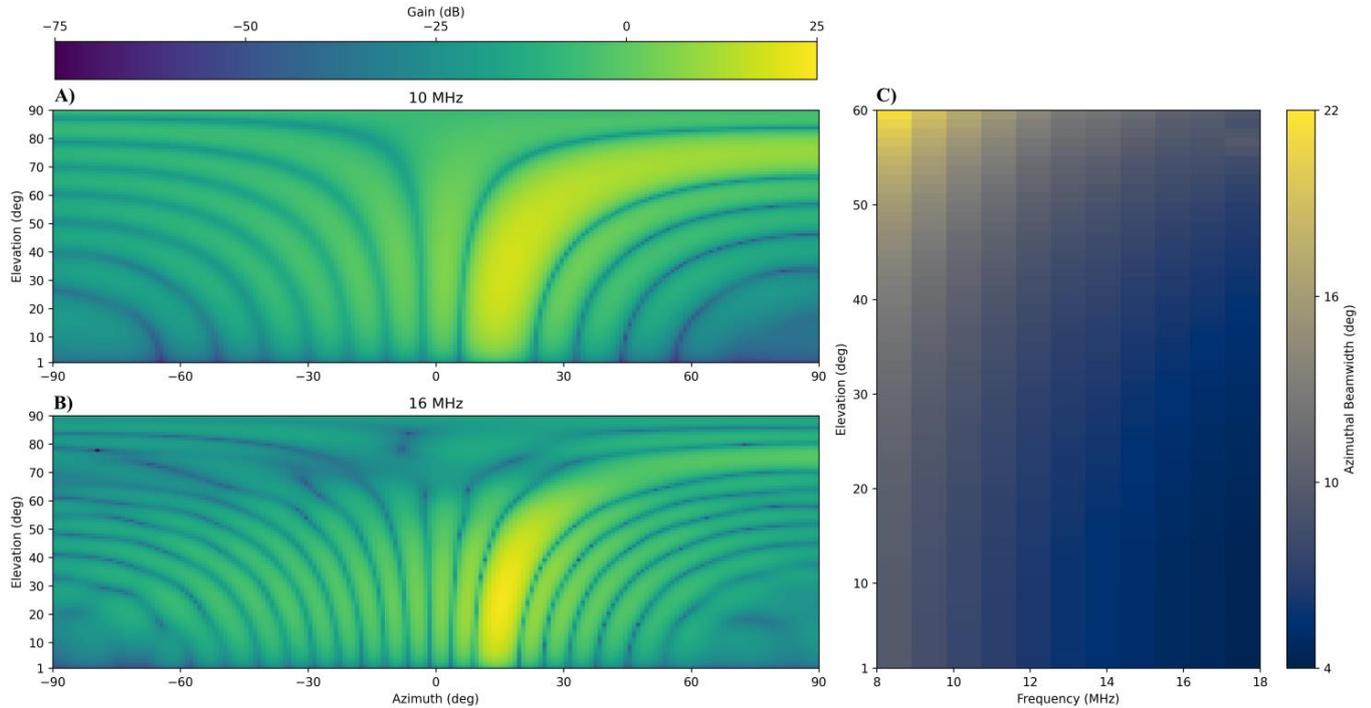
245 sounders by Slimming & Cervera (2019), Edwards & Cervera (2022), and Edwards et al. (2022), with
246 the latter demonstrating the variability of coefficients over different terrain conditions and the notably
247 strong correlation with vegetation. For the purposes of this study, a backscatter coefficient of either -
248 23 dB or -26 dB is simply used for backscatter from sea or land. A value of -23 dB is representative of
249 a fully developed sea (Coleman, 1997; Munk & Nierenberg, 1969), whilst the value for land is an
250 estimate based on the work of Edwards et al. (2022) for a 11-30% coverage of woodland. Due to the
251 large variations in land backscatter coefficients, it must be stressed that this is an approximate median
252 value.

253 **3.4 Antenna Array Modelling**

254 The antenna array gain patterns and beamwidths for the beamformed array are required for calculation
255 of power in equations 3 and 4. Two antenna array designs are used by the SuperDARN network, with
256 the older generation utilizing horizontal log-periodic dipole array (LPDA) elements, specifically the
257 Sabre Communications Corporation model 608 (Custovic et al., 2011), and the newer generation
258 utilizing the novel twin terminated folded dipole (TTFD) elements (Sterne et al., 2011). Whilst gain
259 pattern data for the TTFD antenna elements have been modelled by Custovic et al. (2011) and for the
260 array by Sterne et al. (2011), numerical data was not provided. Data for beam 7 of the Saskatoon radar
261 was provided by Perry et al (2022); however, no other beams are provided.

262 To permit validation across the full SuperDARN network on any beam, we model gain patterns for
263 each beam of the two antenna designs using the Numerical Electromagnetics Code (NEC) version 2.
264 NEC is a software program for the modelling of thin wire antennas developed at the Lawrence
265 Livermore National Laboratory by Burke and Poggio (1981). This program was selected due to its
266 prior use by Custovic et al. (2011), Sterne et al. (2011) and Perry et al. (2022). Far field radiation
267 patterns are generated at 1 MHz intervals for beam 16 of the TTFD array, respectively. This data is
268 provided to the community in the supplementary material along with data for beam 12 and 20.
269 Elevation gain patterns for beam 16 of the Blackstone TTFD antenna array are presented in panel A
270 and B of Figure 5, whilst the variation in azimuthal beamwidth with frequency and elevation is
271 presented in panel C. Whilst a simple analytical relationship for beamwidth may be used for a linear

272 array, we note the importance of including the elevation variation from the modelled gain patterns. A
273 change between low and high elevations of 5° and 60° presents a doubling of beamwidth in Figure 5C
274 and will directly introduce a 3dB change in power through equations 3 and 4.



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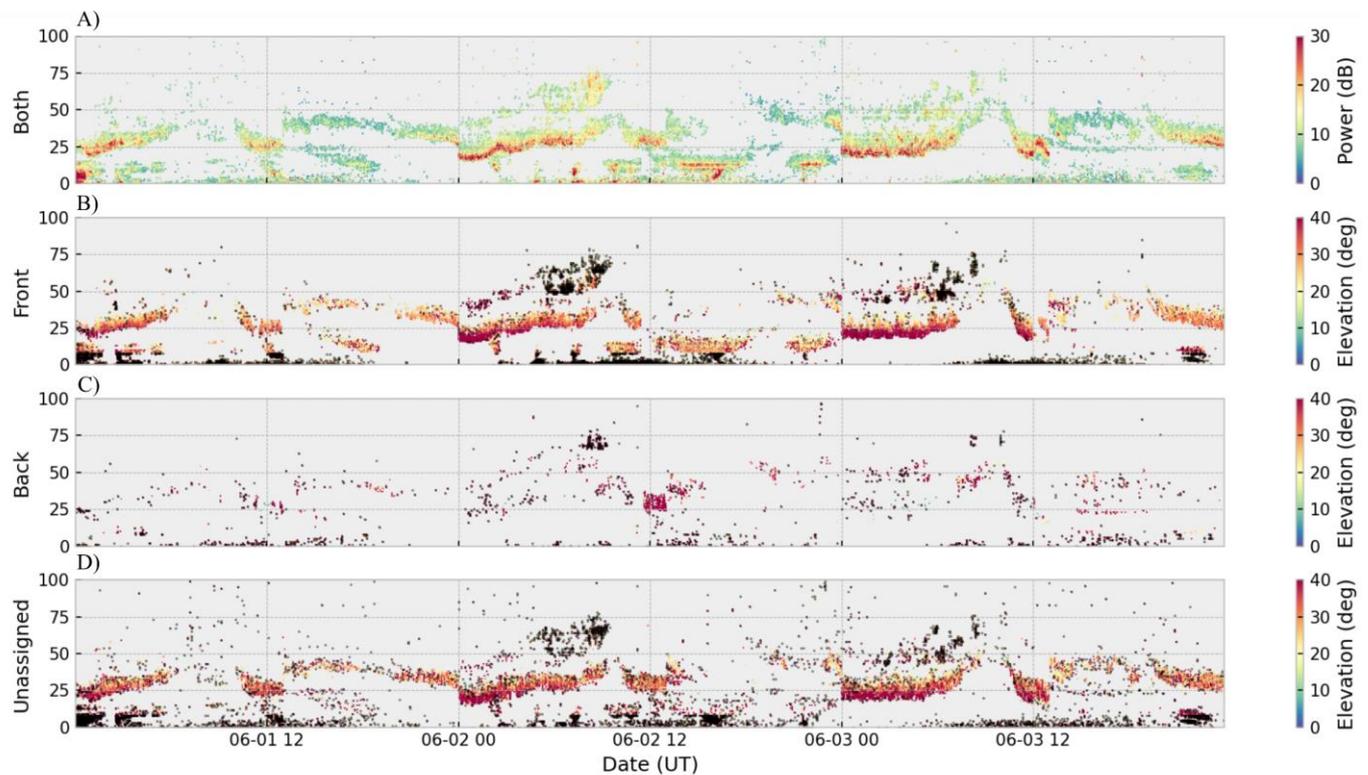
276 *Figure 5. Radiation patterns for the TTFD array phased to beam 16 at 10 MHz (A) and 14 MHz (B). The variation in*
277 *azimuthal beamwidth of the main lobe is provided in panel (C) for a range of frequencies.*

278 2.2 Data Processing

279 2.2.1 FOV Processing

280 Prior to performing validation, the SuperDARN and model data must first be conditioned to ensure
281 proper comparisons can be made, as echoes exist within SuperDARN data that are not modelled using
282 raytracing or are of ambiguous origin. These include echoes from meteor ionisation, sporadic-E,
283 incorrectly assigned ionospheric scatter, and echoes originating from the rear FOV. The latter has been
284 a long-understood problem for SuperDARN and is largely due to the relatively poor front to back ratio
285 of the LPDA arrays and the fact that beamforming causes a secondary lobe behind the radar, meaning
286 a non-negligible amount of power is radiated behind the radars (Milan et al .1997). Due to this
287 secondary source of echoes from behind the radars, it is important to correctly determine the origin
288 FOV when performing validation with simulated echoes to ensure comparisons are consistent. In our

289 application of the technique here, we remove any backscatter from behind the radar and focus on
 290 echoes from the front FOV. Based on the interferometric evidence of Milan et al. (1997), an automatic
 291 FOV detection algorithm was developed by Burrell et al. (2015) to assign correct FOVs and is
 292 included in this validation for radars using LPDA arrays. This algorithm is contained within the
 293 deprecated DavitPy Python package developed by Virginia Tech (Ribeiro et al., 2020) available from
 294 <https://zenodo.org/records/3824466>. Example FOV assignments are presented in Figure 6 for 1st – 3rd
 295 June 2014, showing the assignment of most echoes to the front FOV as expected for the TTFD array.
 296 The FOV Algorithm was applied to radar scans that were of equal frequency, operating mode and
 297 channel. For the 39783 echoes in this time period, we assign 46.68% of echoes to the front FOV,
 298 5.26% to the rear FOV, and are left with 48.10% as unassigned.



299

300 *Figure 6. FOV assignments for Blackstone beam 16 using the Burrell et al. (2015) automatic FOV detection algorithm in*
 301 *June 2014, showing a significant proportion of echoes being unassigned. Elevation data is calculated using the default T_{diff}*
 302 *value in the Blackstone hardware data file for this period which was equal to the calibrated value.*

303 Unfortunately, many echoes remain unassigned by the algorithm, and to avoid ambiguity, these are
 304 removed in conjunction with the rear FOV and IS. It is expected that tuning of algorithm parameters
 305 may improve assignment rates for specific periods; however, this does not permit the liberal

306 application of the validation technique and for this reason, the default values detailed in Burrell et al.
307 (2015) are used. We do not FOV process the Blackstone data in our current work beyond a
308 demonstration in Figure 6 as the TTFD corner reflector provides sufficient mitigation of rear echoes
309 as indicated by Figure 5A but stress the importance of doing so when using radar with LPDA design.

310 **2.2.2 Elevation Calibration**

311 Significant caution is warranted when utilising SuperDARN elevation data as the often-unsuitable
312 interferometer T_{diff} calibration values provided in radar hardware data files can produce non-physical
313 elevation distributions that are not indicative of the real propagation environment. Significant efforts
314 have been made to properly calibrate the radars in the last decade, and the reader is recommended to
315 consult Chisham et al. (2021) for a full treatment of the methods available. For this work, we rely on
316 the E-Region backscatter calibration technique of Ponomarenko et al. (2018) as it is capable of
317 providing automated daily T_{diff} values across all historical data. The value of T_{diff} was found to change
318 sporadically in January 2014 at the onset of significant noise in the Blackstone radar data and so
319 several values were required to mitigate elevation errors here. The values used in this study are
320 provided in the supplementary material and Appendix 2.

321 **2.2.3 Echo Cluster Filtering**

322 The principal interest of this study is 1F GS echoes, as these are clearly identifiable and regularly
323 exhibit a higher power due to skip-focussing. Echoes reflected within the E-region by normal 1E-
324 mode, Sporadic-E, Auroral-E, and meteor scatter are difficult to distinguish and so ambiguity exists
325 over their origin, which provides an unreasonable source of error for validation as no current
326 ionospheric model contains treatment of all. This necessitates the filtering of the data to remove these
327 unwanted echoes that all lie at nearer range gates than that of the 1F mode.

328 Various virtual height models exist that aim characterise echo origins based on climatological
329 SuperDARN data (Chisham et al., 2008; Thomas & Shepherd, 2022). These are unsuitable for our
330 purpose, since they include no consideration of the temporal variability of these channels.
331 Furthermore, using strict filter thresholds to define echo origins can introduce artificial leading-edge

332 features that would degrade the LE analysis of this technique. A neural network-based characterisation
333 scheme was introduced by Kunduri et al. (2022) that offers potentially improved assignments at the
334 expense of expected increased computation time. Conversely, filtering may be altogether avoided by
335 directly extracting the LE using the fitting method introduced by Bland et al. (2014), yet this was not
336 implemented as this would reduce the cadence of our validation due to the requirement to down
337 sample data into 10–15-minute windows. Furthermore, this method requires the radars to operate in a
338 multi-frequency sounding mode, which limits the method to periods when this special control mode is
339 being used.

340 Echoes from distinct propagation channels form temporally and spatially coherent structures in
341 SuperDARN backscatter time series that are often clearly identifiable. We apply the Density-based
342 spatial clustering of applications with noise (DBSCAN) algorithm (Ester et al., 1996) to both the
343 model and SuperDARN data in virtual height – group range space in 30-minute intervals. Virtual
344 height is calculated using the following equation (Bland et al., 2014), which assumes straight line
345 geometry using the distance to the reflection point r , which is equal to $P/2$ for ground scatter.

$$h_v = \sqrt{r^2 + R_e^2 + 2rR_e \sin \theta} - R_e \quad 6$$

346 DBSCAN has previously been employed for SuperDARN backscatter characterisation as part of
347 Kunduri et al.'s (2022) machine learning framework with success. Echoes with elevations below and
348 above 40° are clustered in separate instances, as this provides separation in cases where backscatter is
349 observed across most range gates that may otherwise be incorrectly grouped. The data is clipped and
350 normalised before the algorithm is applied with a maximum neighbourhood distance value of 0.07
351 that was determined through a quantitative assessment of all data in the current analysis using the
352 recommended approach detailed in (Ester et al., 1996).

353 If less than 5 points are available in a given 30-minute window, the data is removed as it is not
354 possible to reliably determine the origin of such backscatter using this clustering technique for such a
355 small number of points. Filtering is applied to cluster centroids by removing clusters with virtual
356 heights and group ranges falling below the thresholds in Table 1 for the low and high frequency

357 nighttime and daytime operation, respectively. Echoes flagged as noise by DBSCAN are tested to
 358 examine if at least 2 neighbouring points in a 3x5 box are contained within an accepted cluster, with
 359 such points kept and those failing this criterion removed.

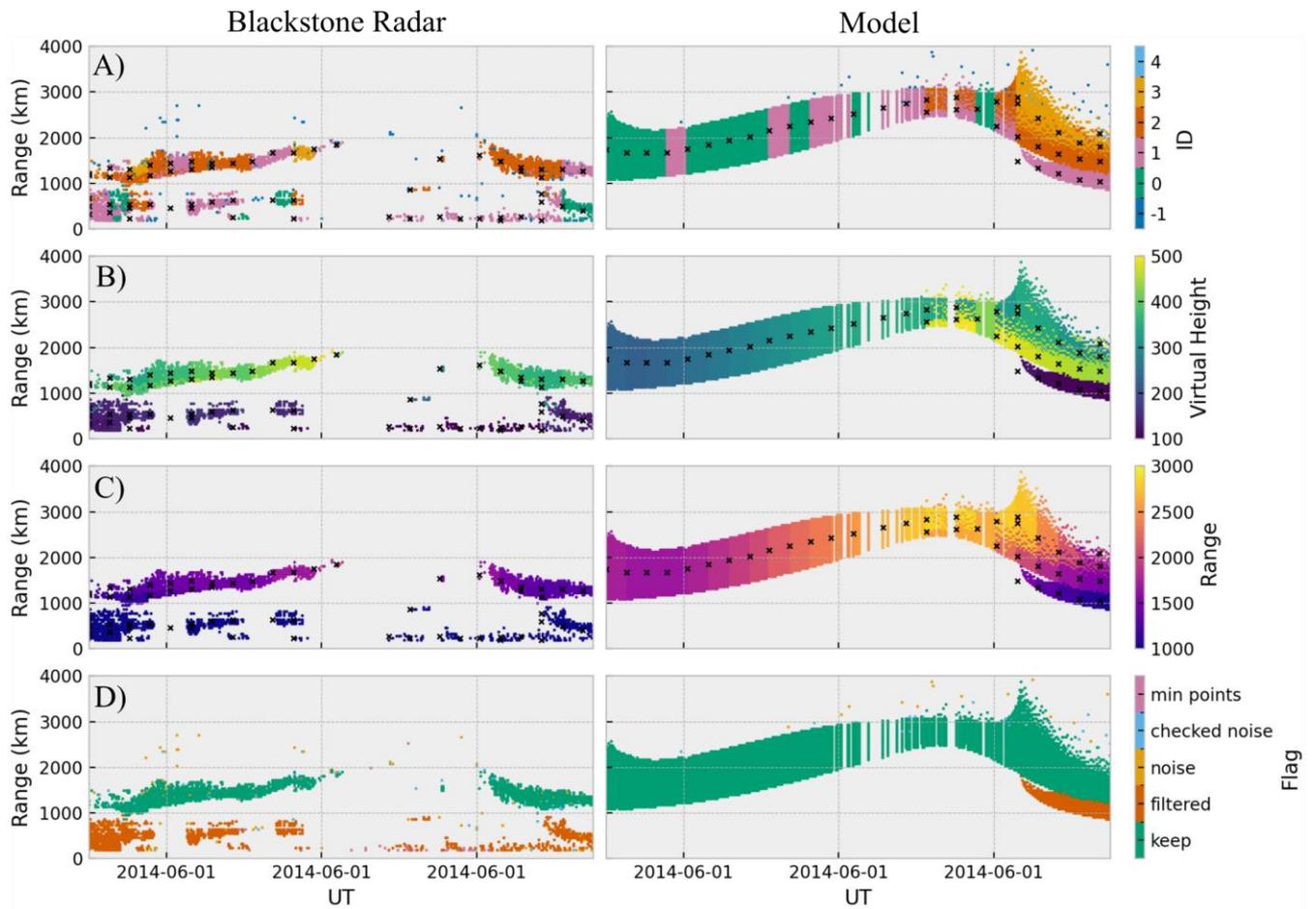
360 *Table 1. Cluster centroid filtering thresholds for the separate high and low elevation and frequency bands. Different*
 361 *parameters are used to tailor the filtering to the different echo regimes.*

	Low Elevation		High Elevation	
Frequency	Low	High	Low	High
Minimum Centroid	150 km	150 km	125 km	125 km
Virtual Height				
Minimum Centroid	1100 km	900 km	850 km	750 km
Range				

362

363 This approach removes the unwanted echoes providing they are contained within a coherent
 364 backscatter structure and Figure 7 shows the capacity of this method to process both model and
 365 Blackstone radar data. At times when the separation between near range echoes and the primary 1F
 366 group is small, these echoes may become clustered together, resulting in either both being removed or
 367 the non-1F echoes being kept. Furthermore, non-1F clusters whose centroids exceed the values in
 368 Table 1 are kept regardless of their origin. Whilst we recognise the limitations of our approach, the
 369 technique is sufficient for our application here and limits arbitrary modifications to the LE that may be
 370 imposed by alternative methods.

371



372

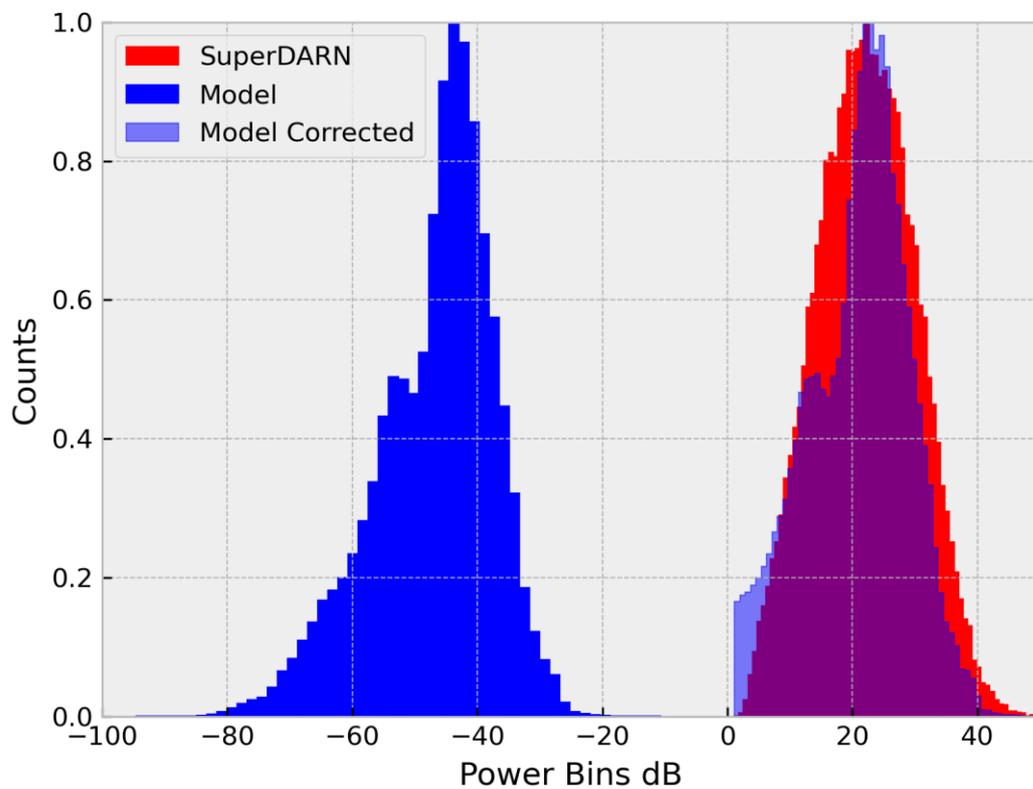
373 *Figure 7. Example action of the DBSCAN based filtering method, showing the identification of distinct groups in A), the*
 374 *calculation of cluster centroids in B) and C), and the filter determination in D). Echoes flagged in D) as filtered identify E-*
 375 *region echoes, noise identifies echoes classed as noise by DBSCAN, checked noise identifies echoes classed at noise that*
 376 *pass the check for a suitable cluster in the neighbourhood, and min points identifies instances where insufficient data was*
 377 *available in a given 30-minute window. The clustering technique demonstrates the filtering of coherent structures as a whole*
 378 *and minimises the impact of non IF echoes on the LE feature.*

379 **2.2.4 Power Normalisation**

380 Issues arise when comparing the modelled and experimental power data, as whilst modelling the
 381 power distribution can be done reliably, the absolute values are more difficult to determine as noise
 382 must also be estimated due to SuperDARN power values being in terms of signal-to-noise ratio
 383 (SNR). These values are found by the SuperDARN FITACF procedure by fitting an exponential
 384 function to the envelope of a complex ACF and taking the value at zero-time lag as the power
 385 estimate.

386 To avoid complexities here, the power profile of the modelled data is normalized in relation to the
 387 power distribution peaks found by binning power into 75 bins. It should be noted that the log scales of

388 modelled power and SuperDARN SNR values are different and are transformed here. Figure 8 shows
389 the histograms for the two data sets for January 2014, with this corresponding to a power offset of
390 72.70 dB being applied to the data in this case. Simulation data contains rays that would exist below
391 the receiver threshold of the radar, thus being undetectable and requiring removal prior to our
392 comparison. To this end, simulation data with power values below the minimum power of the
393 Blackstone radar power distribution are removed. This process is performed for each frequency band
394 across each full month to avoid sudden changes in power at shorter timescales and to ensure sufficient
395 data is available when creating the histograms.



396

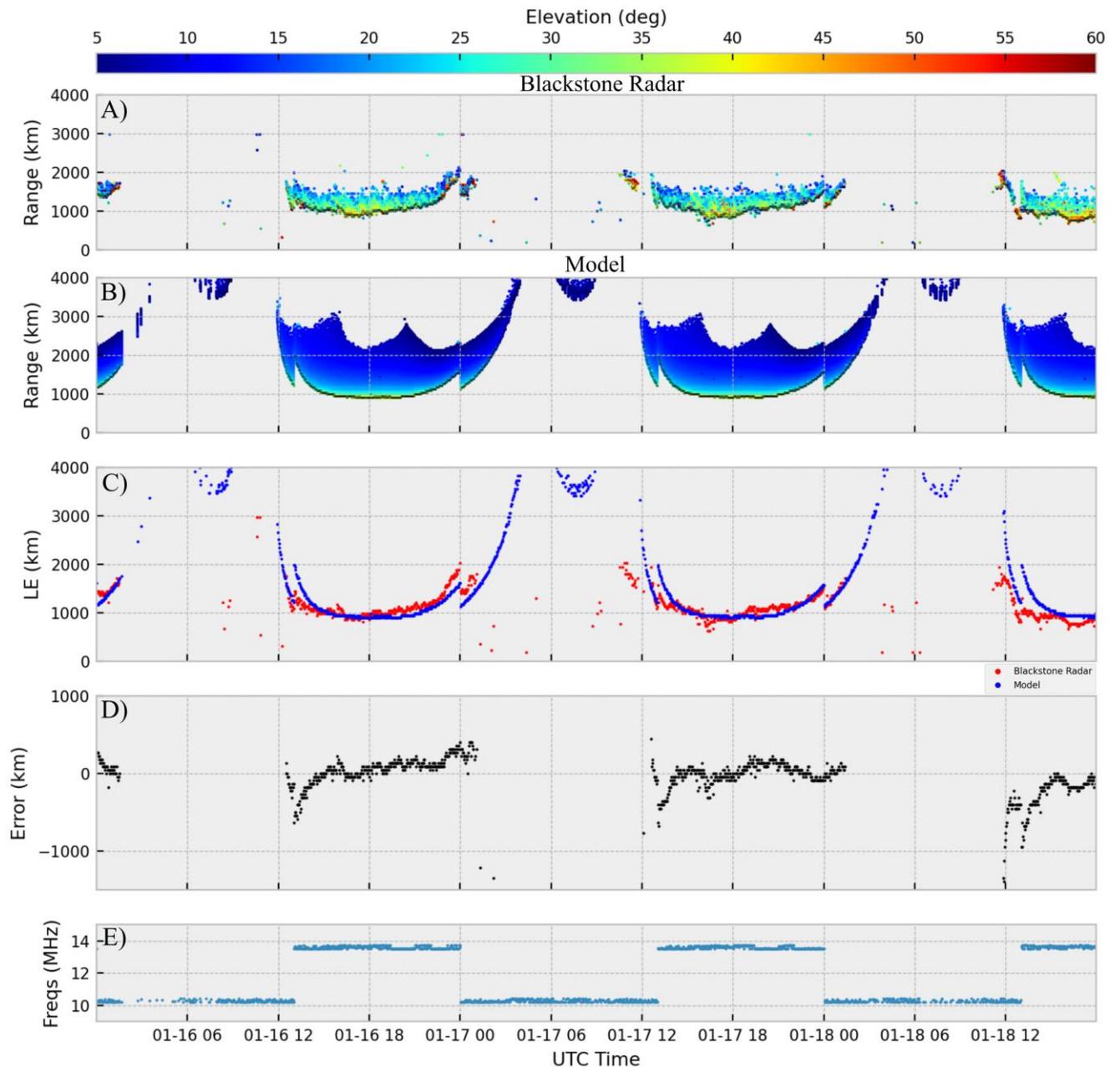
397 *Figure 8. Power histograms for data in January 2014 for the Blackstone SuperDARN radar (red), the model (blue) and the*
398 *normalised model with low power echoes removed (light blue). The normalisation process shows good agreement between*
399 *the corrected model and the Blackstone radar distributions.*

400

401 **3. Results**

402 **3.1 Example Backscatter Variation**

403 To examine the capacity of the simulation to model the Blackstone radars' GB, the time evolution of
404 backscatter echoes are plotted in Figure 9 for the 16th-18th January 2014. It should be noted that the
405 local time is approximately 6 hours behind UTC for this specific radar. The LE of the GB is extracted
406 by simply taking the minimum group range at each time step and is overlaid in black. Small-scale
407 variations observed in the Blackstone radar GB at timescales below 1-hour resolutions are not
408 captured within the simulation as the IRI offers only a smoothed representation of the monthly median
409 ionosphere at a limited temporal resolution. The passage of Travelling Ionospheric Disturbances
410 (TIDs) is a known source of variability in daytime GS on timescales of approximately one hour
411 (Samson et al., 1989) and is an example of a feature not within the modelled backscatter.



412

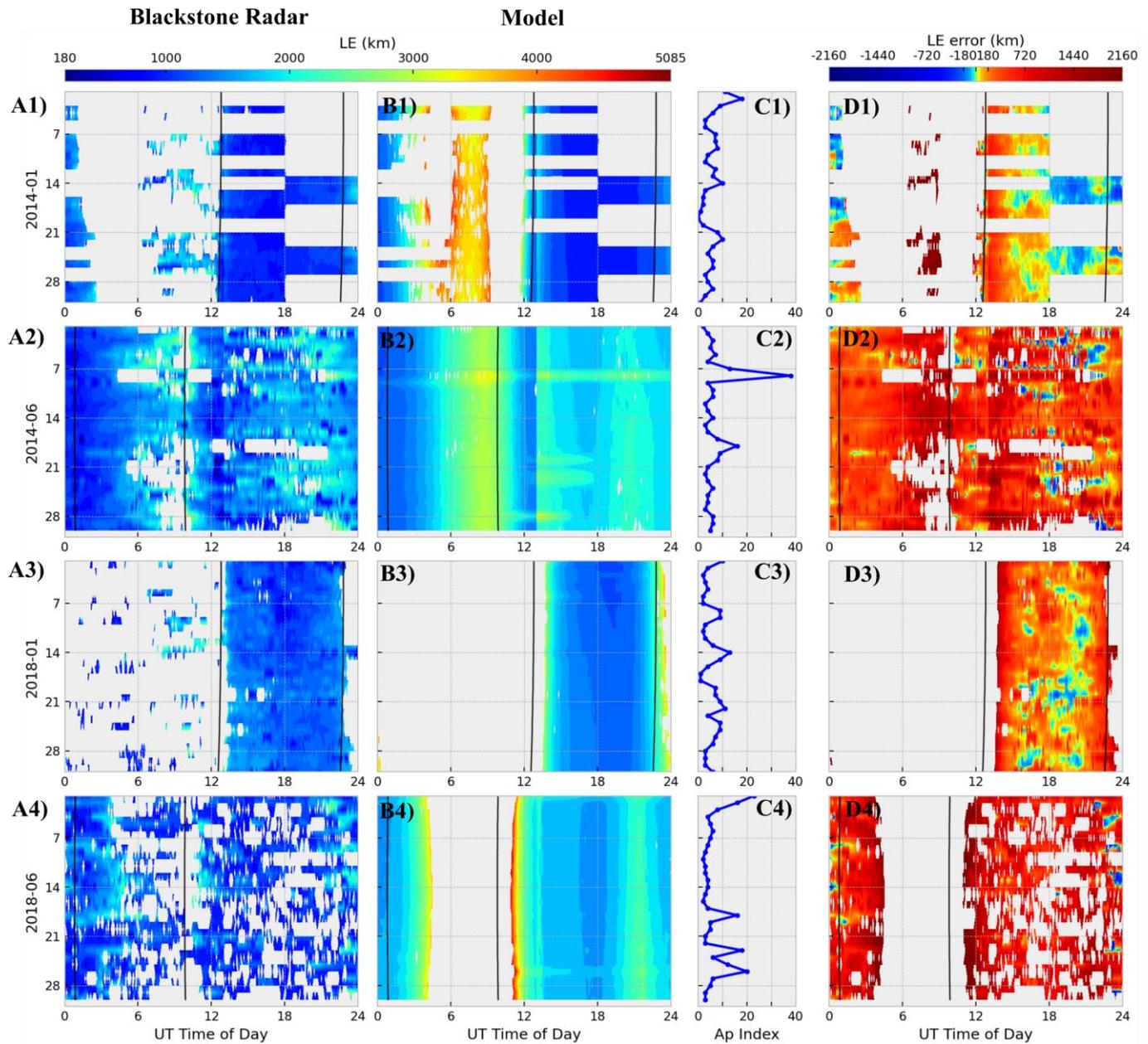
413 *Figure 9. Variation in elevation angle for the Blackstone SuperDARN radar (A) and the model (B) between 16th and 18th*
 414 *January 2014. The leading-edge range is extracted and plot in (C) for Blackstone radar (red) and the model (blue). The*
 415 *error in leading edge range is included in (D) whilst transmission frequency is included in (E).*

416 During the nighttime, almost no echoes are observed in both data sets. Upon inspection of Figure 2, it
 417 is clear that IS dominates at these time periods and so our analysis is limited to only daytime
 418 comparisons here. Good agreement is seen between the Blackstone radar and model LE at midday,
 419 with errors remaining within ± 250 km and large departures only occurring during the early morning.
 420 A notable offset in elevation angle is seen between the two, with the Blackstone radar consistently
 421 observing a higher elevation angle by approximately 10° .

422 Despite the GB LE showing good agreement, notable differences in the trailing edge distributions are
423 seen. Despite the power corrections clearly reducing the extent of the model trailing edge, a
424 significant overestimate remains. The same conclusion may be made for the long-range nighttime
425 echoes seen in the model but not by the Blackstone radar. Both trailing edge and nighttime echoes
426 occur at very low elevations that manifest in a significantly reduced power due to the falloff in gain at
427 such elevations. Of course, the methods used to adjust the powers to be comparable is a considerable
428 limitation here and so we must take any assessment of the power behaviour with some measure of
429 skepticism; as such, the absence of echoes in the Blackstone radar data, relative to the simulation,
430 cannot necessarily be taken as indicative of a propagation difference. This reinforces the importance
431 of utilizing the LE for comparisons due to the increase in observed power that occurs here.

432 **3.2 Climatology**

433 Investigation of model and Blackstone radar backscatter for several day periods is useful for
434 assessment of errors during specific events, but is insufficient for validating general or long-term
435 performance. We apply the modelling technique to the months of January and June in both 2014 and
436 2018 and present the LE characteristics in Figure 10 to capture the diurnal, seasonal and solar cycle
437 climatology of errors. The variation in LE is binned down to 5-minute intervals and averaged for this
438 analysis. It is important to note that there is not full coverage of every bin across the months. This data
439 sparsity is due to either the radar not being operational, a lack of GS, the filter removing non F-mode
440 echoes, or significant absorption hindering detection. One should be careful to notice that the sudden
441 step in LE at 13:00 UT in 2014 is due to the radar switching frequency and does not represent an
442 immediate change in the ionosphere. This also occurs in 2018 but is not immediately visible as the
443 difference between the day and night frequencies was much smaller.



444

445 *Figure 10. Variation of leading edge in January and June for both 2014 and 2018. Blackstone SuperDARN leading edge is*
 446 *provided in the first column, the model in the second, the Ap index in the third, and the calculated leading-edge errors in the*
 447 *fourth. One should note that leading edge errors are clipped to ± 2160 km to preserve dynamic range and in some rare cases,*
 448 *errors do exceed this. The error colormap is log10 scale and has contours every 45km which corresponds to the group range*
 449 *resolution of the measurements. Data is not available for many periods in January 2014 and is the reason for large blocks of*
 450 *missing data. The time of the local solar terminator is shown by the black vertical lines for a point 500 km down range.*

451 The LE in both data sets shows the expected diurnal variations of retreating in the evening and
 452 returning in the morning, with the daytime LE also shown to occur at considerably closer ranges for
 453 winter compared to summer in both data sets as expected. This is due to the winter anomaly, a
 454 midlatitude phenomenon where unexpectedly high electron density values exceeding those in summer
 455 are observed during the winter daytime (Davies, 1965). As a result, higher elevation rays that

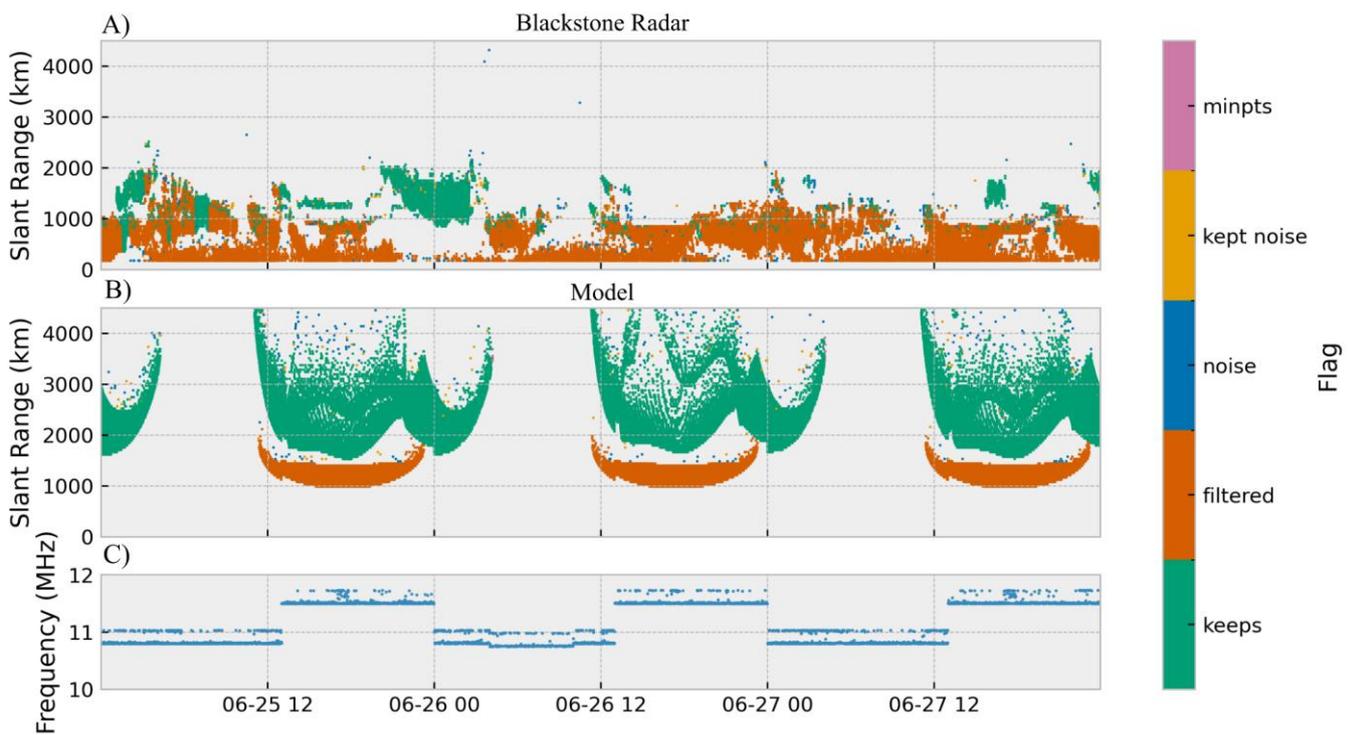
456 correspond to closer ranges are supported through the relation in Equation 2 as suggested by Equation
457 1.

458 A geomagnetic storm occurs on 8th June 2014 as indicated by the Ap index and the increase in model
459 LE. Unfortunately, echoes were not present within the Blackstone radar data for much of this day
460 and is likely due to increased ionospheric absorption coinciding with the storm. Echoes that are
461 present between 13:00-20:00 on this day indicate a consistent error exceeding 1,000 km throughout
462 this period. The lack of data during this storm is a notable limitation of using oblique HF
463 measurements for validation and can likely only be mitigated by using much greater transmit powers.

464 Errors are seen to be most significant for all months at the time of the local terminator where LE
465 ranges are increased and are generally lower during the middle of the day. Overall, LE errors are seen
466 to be overestimates by the model with the exception of daytime Les in January 2014. In January 2018,
467 the ability of the model to fully capture the overall increasing LE following the month progression is
468 demonstrated by daytime errors remaining below 500 km for the entire month.

469 The simulation predicts a population of nighttime echoes at extreme ranges of ~4000 km not seen by
470 the Blackstone radar in the month of January 2014, and this is attributed to low power echoes below
471 the receiver threshold of the radar. Evidently, these have not been removed from the simulation during
472 the power normalisation process despite having expectedly high free space path losses and typically
473 low antenna gain compared to the rest of the data. Nonetheless, periods where echoes occur in both
474 the model and Blackstone radar LE are the focus of this validation and where errors are computed, as
475 the absence of echoes is not necessarily indicative of the lack of propagation. One should be cautious
476 about instances where sudden retreats in LE are seen in the Blackstone radar data as this is not
477 conclusive of a physical change in the ionosphere but may be caused by limitations in the data or
478 filtering. This can be seen at 22:00 on the 4th June 2018 and is likely non-physical as Sporadic-E is
479 prevalent during this period and can prove difficult for the filter. We do not consider this to be a
480 significant limitation as this is expected from this data and impacts a relatively insignificant
481 proportion of the overall data.

482 The presence of a sporadic-E layer blanketing 1F echoes is a noticeable effect in the summer months,
 483 especially in 2018. Here, the cluster filter essentially removes all echoes as the regular occurrence of
 484 sporadic-E is either the sole source of echoes, or where 1F is not entirely blanketed, it often forms a
 485 cluster that cannot be fully separated from the 1Es-mode and so both are removed. This is a fortunate
 486 effect of the filter, as for periods where a LE cannot be suitably extracted, all data is typically
 487 removed due to the low centroid range and virtual height. This largely prevents comparison of
 488 otherwise uncertain data. A summary plot of a period where Sporadic-E is significant is presented in
 489 Figure 11, showing the capacity of the filter to reliably remove almost all of the unwanted echoes,
 490 whilst keeping what 1F-mode can be reliably identified. It should be noted that there are clear
 491 instances in Figure 11 where the filter does not correctly remove non-1F echoes such as at
 492 approximately 03:00 and 08:00 on the 25th.



493

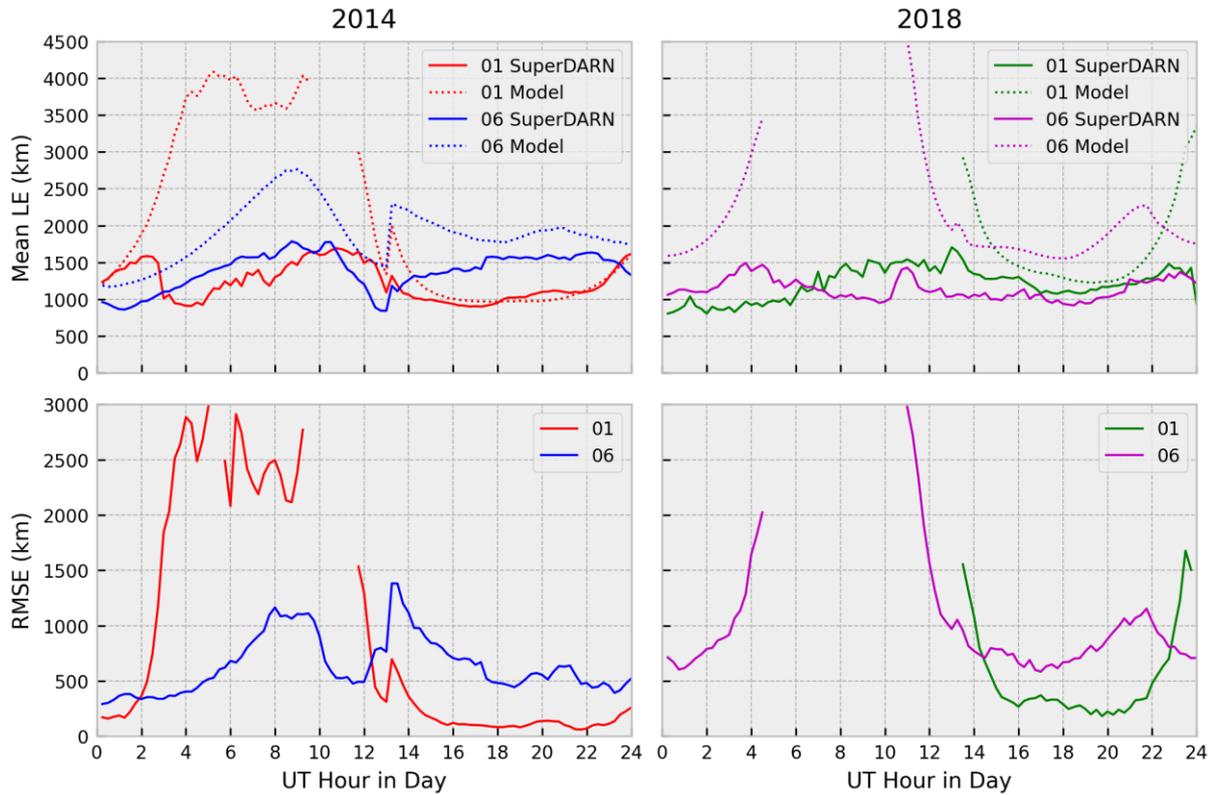
494 *Figure 11. Example time variation of filter flags showing the presence of blanketing sporadic-E for much of June 2018. The*
 495 *filter performs reliably across this period, with minor inconsistencies where sporadic-E is incorrectly. The filtered echoes in*
 496 *the model are from 1E backscatter as sporadic-E is not modelled in the IRI2016 model. These echoes are likely also in the*
 497 *SuperDARN data but are difficult to distinguish from sporadic-E.*

498 A more concise assessment of LE error climatology can be facilitated by averaging across the month
 499 in the form of a 15-minutely RMSE as presented in Figure 12. The monthly averaged performance of

500 the model during the daytime is seen to be reasonable, showing errors as low as 100 km and 250 km
501 for January 2014 and 2018, respectively. For this context, 100 km is considered a low level of error as
502 the group range resolution of the Blackstone radar is 45 km and we often see minute-to-minute
503 variability of the leading edge across 2-3 range bins such as in Figure 9. In contrast, positioning errors
504 for OTHR are typically expected to be less than 30 km in range and measurement resolution is
505 approximately 3-30 km for normal operating modes (Fabrizio, 2013).

506 It is reassuring to observe stable performance across the daytime hours in January of each year, as this
507 suggests we can expect acceptable accuracy when modelling oblique propagation using the IRI-2016
508 model at these times. Despite this, summer performance is seen to be degraded, showing minimum
509 errors of 400 km and significant departures approaching 800 km, albeit this may be partially attributed
510 to nuisance Sporadic-E degrading the data quality. In Figure 12, caution is recommended when
511 inspecting periods of data sparsity, as this will degrade the robustness of our statistical analysis. To
512 this end, nighttime LE assessments in January 2014 and the full month of June 2018 are generally less
513 reliable due to the absence of consistent data. Errors in the nighttime hours exceed 1000 km in all
514 months.

515



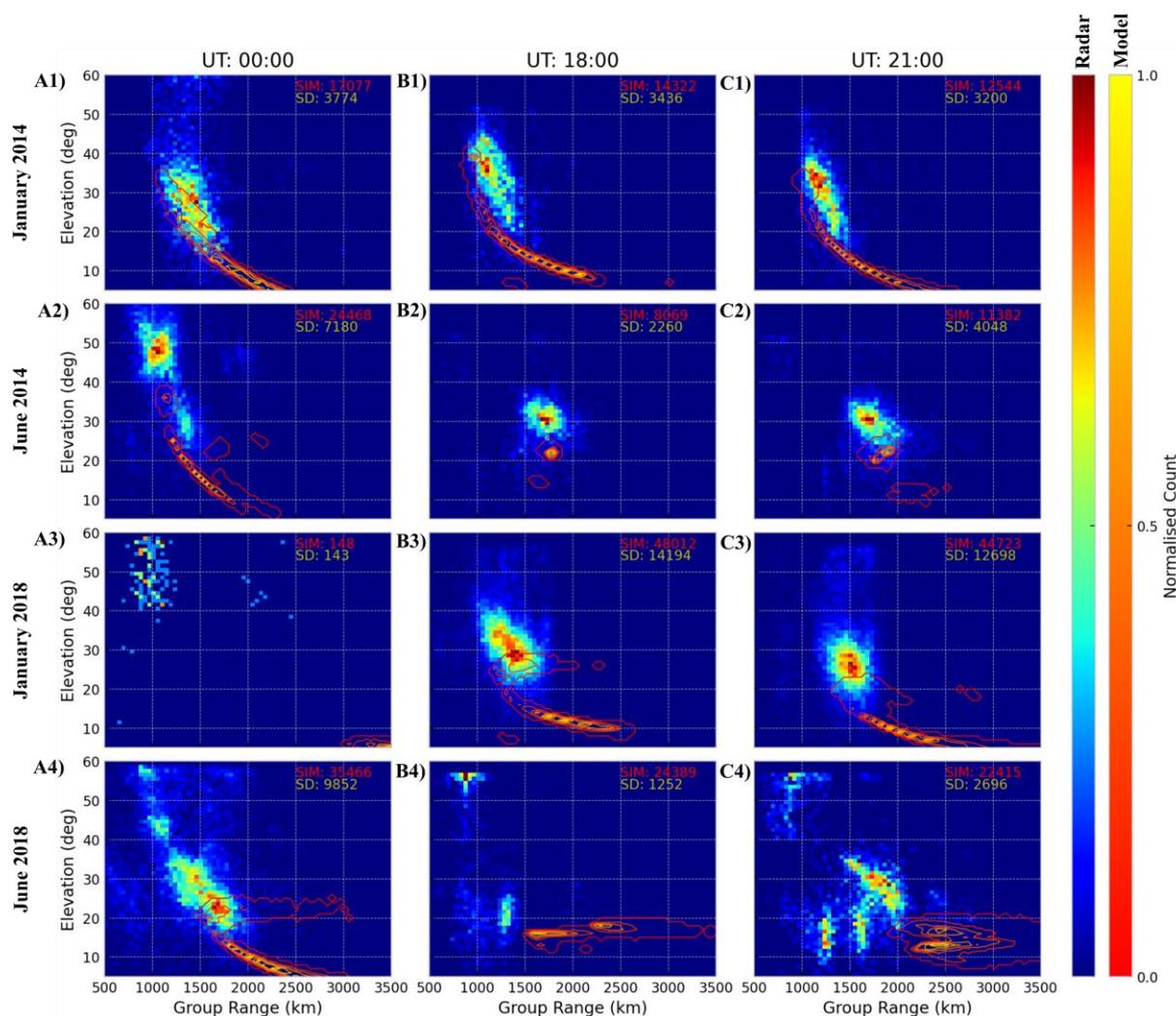
516

517 *Figure 12. Day variations in 15-minute month averaged leading edge slant range (top) and the corresponding RMSE*
 518 *(bottom) in 2014 (left) and 2018 (right). Instances where no data is available restricts full day coverage of this analysis in all*
 519 *cases but June 2014.*

520 3.3 Elevation Angle Distributions with Group Range

521 The provision of elevation data by the SuperDARN interferometers permits further inspection of
 522 model errors beyond the LE analysis, as we can directly compare the slant range- elevation
 523 distributions between the two data sets. This comparison is presented in Figure 13 for three UT times,
 524 where the 2D histograms are created by including all echoes across the month occurring within the
 525 specified hour for 1° elevation bins. As these distributions are averaged across the full month, we see
 526 a much greater broadening of the Blackstone radar echo distributions as compared to the simulation
 527 due to the greater variability of the real ionosphere in comparison to the monthly median IRI-2016.
 528 The merit of elevation angle estimates within SuperDARN data is notable in this context, as the upper
 529 limit to echo elevation values that are physically possible is directly related to NmF2 to the first order
 530 by Equation 2. It is important to note that whilst Equation 2 can provide useful context when
 531 diagnosing errors in NmF2, an equation that incorporates spherical Earth geometry such as in (Gilles
 532 et al., 2009) should be used when calculating absolute NmF2 error values. Figure 14 permits

533 diagnosis of potential NmF2 and hmF2 errors whilst highlighting distinct propagation modes so that
 534 the effectiveness of the E-region filter can be assessed.



535

536 *Figure 13. Slant range - elevation echo distribution histograms for the Blackstone radar shown by the base colormap and*
 537 *for the model by the overlaid contours. All echoes occurring within the specified hour across the full month are included in*
 538 *each panel, with the total count included indicated in the top right corner of each.*

539 Figure 13 shows generally good agreement between the Blackstone radar and model distribution LEs
 540 in January 2014, where the average LE is seen to occur between 1000- and 1300-km with the closest
 541 range occurring near the middle of the day at 18:00 UT as expected. At high elevations, the
 542 distributions occupy the same range-elevation space for this month but begin to depart at lower
 543 elevations as the Blackstone radar trailing edge does not extend in the same manner. As previously
 544 mentioned, this is likely due to low power echoes not being detected; however, it is important to note
 545 that this results in the peak of the model contour shifting towards further ranges and lower elevations.

546 This is also seen to occur at 00:00 in June 2014, 18:00 and 21:00 UT in January 2018 and in all of
547 June 2018, suggesting a systematic overestimate of trailing edge power.

548 At 18:00 and 21:00 UT of June 2014, we see distinct localised peaks in the distributions, with
549 minimal spread in elevation for both Blackstone radar and model data, indicating that the model
550 predicts this behaviour well. Nonetheless, we observe a distinct offset in the elevation peaks of
551 approximately 8° that suggests the model is likely underestimating NmF2 here. A similar difference
552 was observed by Oinats et al. (2016) and was attributed to underestimates in the IRI's representation
553 of the electron density peaks. An interesting number of echo populations are observed at 00:00 UT of
554 June 2014 that suggests distinct propagation modes. Whilst the low-density group centred on 47° at
555 1900 km is a distinct contribution from 2F echoes, the two closer peaks appear to both be 1F echoes.
556 The occurrence of a double peak population can be explained by variability in the ionospheric peak
557 density broadening the distribution, and inspection of the processed data confirms this as no E-region
558 echoes are observed.

559 Insufficient data is available for 00:00 Jan 2018 due to the lack of nighttime echoes. Conversely, the
560 distributions at 18:00 and 21:00 show the greatest number of echoes that permits underestimates in
561 elevation to be identified for these times.

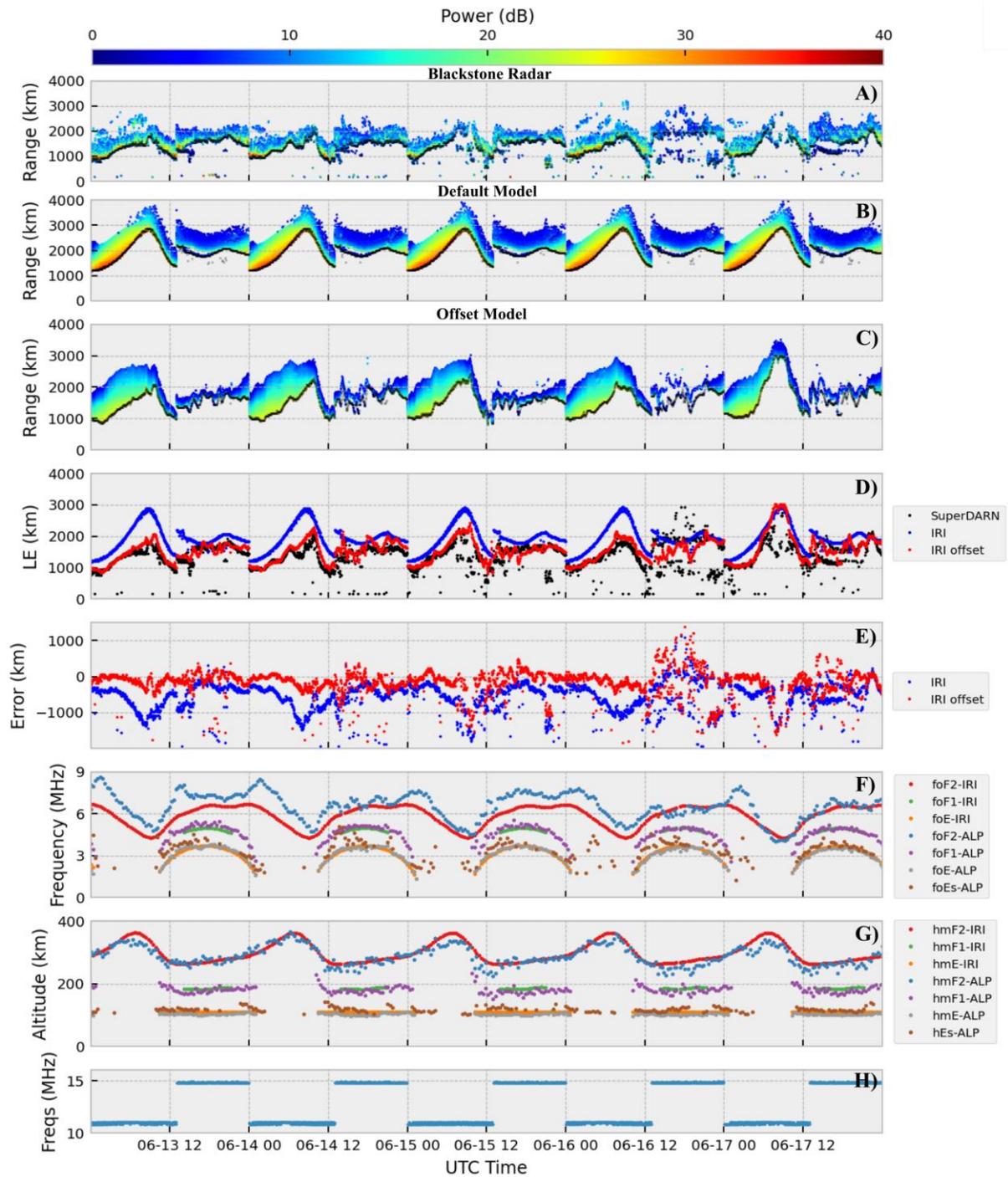
562 The presence of Sporadic-E is clearly identifiable during June 2018 by the characteristically high
563 elevation angles occupied by these distributions at close ranges. We also see a distinct E-mode
564 population at 15° at a range of 1,250 km at 21:00 UT ahead of the expected 1F population. Whilst it is
565 clear the filter has accepted a statistically significant number of E-region echoes, it is worth noting
566 that the relative proportion of E-region echoes compared to that of the F-region is significantly greater
567 for much of the month, and so it is reassuring that the 1F echoes are presented so dominantly at 00:00
568 and 21:00. This implies that the filter is working acceptably well as indicated in Figure 12 but is
569 insufficient to warrant a reliable analysis of the LE due to the statistical significance of E-region
570 echoes in the data.

571 An interesting feature observed in the model for 00:00 of June 2014, 18:00 and 21:00 of January 2014
572 and in June 2014 is that of a broadening of the distribution at higher elevations towards further ranges
573 in the shape of a ‘C’. This is characteristic of high angle rays occurring within the F-region and are
574 typically associated with low powers due to the defocussing effect of rays near the F-layer peak.

575 **3.4 Ionosonde Conjunction**

576 To demonstrate the potential performance of the model when ionospheric peak parameters are known,
577 we simulate the period of 13th-17th of June 2014 with the IRI-2016 model driven by ionosonde
578 measured values. The Alpena ionosonde located down range of the radar at 45.1N, 83.6W is used in
579 this assessment and provides an opportunity to assess the robustness of our validation technique.
580 These results are presented in Figure 14 and are compared to that of the default model for context.
581 Ionograms recorded at 15-minute intervals throughout this period are manually scaled to extract
582 ionospheric parameters and presented in comparison to model values in panels F and G of Figure 14.
583 As the IRI-2016 model permits the manual input of any of the bottomside parameterisation values, we
584 take the relative difference between the ionosonde and IRI-2016 parameters at the nearest point on the
585 radar beams great circle (GC) path and apply constant multipliers to the entire GC slice such that the
586 parameters match exactly at that point. The offset location is 45.24N, 83.51W and corresponds to a
587 ground range of 1,016.7 km from the radar and 16.7 km from the ionosonde. At times when the IRI-
588 2016’s F1 region model is inactive, it is not possible to override the parameter, and so we are forced to
589 leave it off, which is at times in disagreement with the ionosonde. Whilst the ionogram measurements
590 are only representative of the ionosphere for an area related to the typical ionospheric decorrelation
591 distance (Forsythe et al., 2020), they provide a useful means to assess modelled ionospheric dynamics
592 beyond the monthly median. This is clear by the introduction of travelling ionospheric disturbance
593 (TID) features into the modelled backscatter in Figure 14 panel (C), which are not seen in the default
594 IRI-2016 in panel (B).

595



596

597 *Figure 14. Comparison of Blackstone radar (A), model (B), and ionosonde driven model (C) backscatter LE variations (D)*
 598 *and errors (E). Default IRI-2016 and ionosonde peak density and height parameters are compared in panels (F) and (G),*
 599 *respectively, whilst operating frequency is provided in (H).*

600 It is immediately clear upon inspection of Figure 14 that the ionosonde input provides a dramatic
 601 improvement in both the modelled backscatter echo distribution and LE variation, with the latter
 602 showing errors centred near zero for much of the period and at times providing improvements in
 603 excess of ~800 km. The greatest improvements are regularly seen during the nighttime periods. Panel

604 (F) shows that almost all of this improvement can be attributed to the mitigation of errors in NmF2, as
605 the IRI-2016 is otherwise able to represent all other parameters with reasonable accuracy, except for
606 the occurrence of the F1 region and of course the presence of sporadic-E.

607 A clear limitation in our approach here is that minor TID features measured by the ionosonde and seen
608 in the Blackstone radar data are massively overestimated. This is likely because such features are
609 often localised over a relatively small distance and are inherently directional; this presents problems
610 in our model as the ionosonde is not directly under the reflection point and our offsets are applied
611 equally along the GC.

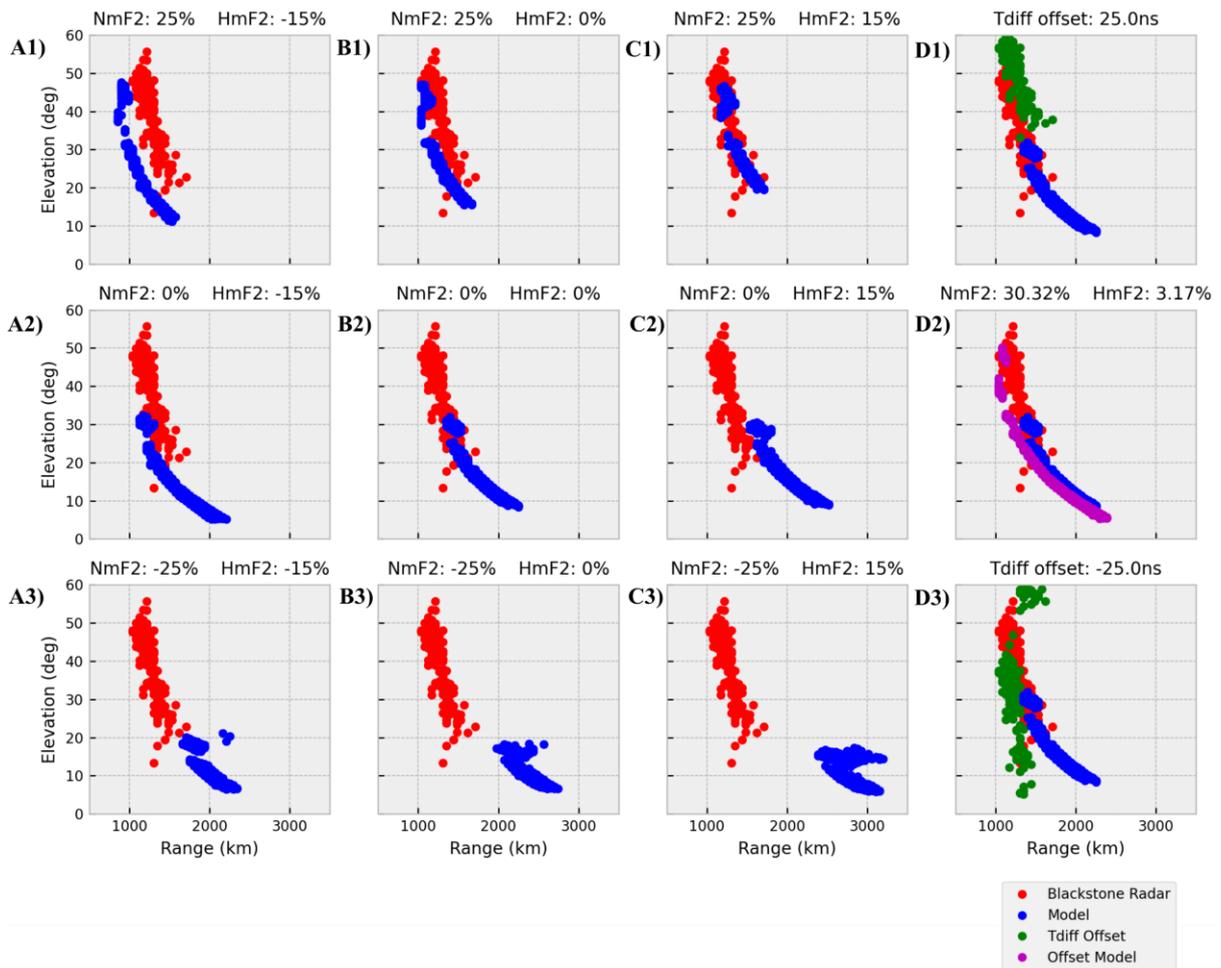
612 A small number of echoes are present at 9:00 UT on the 15th and 17th and cause a significant increase
613 in errors for both modelled LEs, with these appearing to be either auroral E-mode or ½-hop echoes
614 that are not properly removed by the filtering or ground flag, respectively. It is unexpected to see
615 echoes at such close ranges during the night time as 1F echoes are typically seen to retreat to further
616 ranges as the ionospheric density drops and only low elevation angles are available. Furthermore, E-
617 mode echoes remain in the Blackstone radar data at 21:00 UT on the 15th and at 22:00 on the 16th,
618 with this corresponding to an unreasonable increase in both modelled LE's. It is interesting to note
619 however, that a small population of echoes is often seen in all three data sets ahead of the main 1F
620 backscatter during several of the days that arises from the F1-region. The occurrence of this feature
621 coincides with increased errors and error spread in the modelled LE's as the small population appears
622 inconsistent in both the Blackstone radar and driven model data, potentially being due to such low
623 echo powers as suggested by Figure 14. Nonetheless, Figure 14 demonstrates that improvements in
624 model NmF2 values can dramatically improve model performance such that the much of the real
625 propagation environment can be reliably modelled using numerical raytracing.

626

627 **3.5 Error Diagnostics**

628 Significant insights can be gained on the origin of model errors by exploring the effect of offsets to
629 model NmF2 and hmF2, specifically how these parameters impact the range elevation distribution of

630 echoes. To examine the impact of specific errors in the ionospheric model on the range-elevation
 631 space, we simulate the hour of 3:00 on the 14th of June 2014 with combinations of $\pm 25\%$ and $\pm 15\%$
 632 offsets to NmF2 and hmF2, respectively. Furthermore, we recalculate elevation angles for the
 633 Blackstone radar data in panel D1 and D3 with ± 25.0 ns offsets from the calibrated values of T_{diff} .
 634 This seeks to demonstrate the relative impact of the ionosphere and interferometry on the distributions
 635 and to present the effect of uncalibrated T_{diff} values on the error analysis.



636

637 *Figure 15. Diagnostics of model errors by applying NmF2 and hmF2 offsets (blue) compared to calibrated Blackstone radar*
 638 *backscatter (red). T_{diff} perturbations are demonstrated in panels (D1) and (D3) in (green), with ionosonde driven model*
 639 *backscatter also shown in (D2) in (magenta).*

640 From Figure 15 it is clear that an increase in NmF2 shifts the distribution forward and up to higher
 641 elevations, with the opposite being true for a negative offset. Conversely, modifying hmF2 does not
 642 impact the elevations occupied by the distribution and instead a forward and backwards translation in
 643 slant range is seen for negative and positive offsets, respectively. We see that the applied offsets

644 account for deviations in elevation and range of approximately 15° and 300 km in each direction,
645 respectively. Besides hmF2 modifications resulting in range translations, we also see a minor shift in
646 elevation angles. This is an expected result and is due to changes in NmF2 that arise as the location of
647 the reflection point is shifted in range to a different region of the downrange ionosphere.

648 By the apparent difference between the original model (B2) and that of the model offset by +25%
649 NmF2 (B1) demonstrating a much better agreement with the Blackstone radar distribution, we can
650 infer that there is an error in NmF2 on the order of 30%. This is in direct agreement with the
651 ionosonde driven distribution (D2) that confirms that the difference in the modelled and measured
652 NmF2 values differ by 30.32% and show better agreement with the Blackstone radar distribution with
653 this offset applied.

654 As noted by Ponomarenko et al. (2018), the relation between measured phase and elevation angle is
655 highly nonlinear, and this is demonstrated by the distribution occupying a significantly greater range
656 of elevations in panel D3 as opposed to that in D1. The range of elevations occupied by the echoes is
657 dramatically changed by the T_{diff} offset, with a +25 ns offset having elevations covering 30° to 60°
658 and the -25 ns offset having a much broader range of 5° to 60° . The deviation in elevation near the top
659 of the distributions for the T_{diff} offsets is approximately 5° from the calibrated value, and this remains
660 relevant when compared to the impact of NmF2 offsets. Thus, when diagnosing NmF2 information
661 from SuperDARN elevation data, it is paramount that the data is properly calibrated.

662

663 **4. Discussion**

664 The marked increase in errors at times near the local terminator seen in our analysis for Figures 9, 10,
665 12 and 13 is expected. These periods present a marked challenge that some ionospheric models may
666 perform poorly during due to the rapidly changing NmF2 and hmF2, meaning incorrect timings of
667 sunrise or sunset by the model can result in large errors in these values. A further expected
668 shortcoming for the IRI at these periods is its inclusion of an occurrence based F1-layer that toggles
669 on and off abruptly as this can introduce non-physical density gradients along the generated great

670 circle grid. Despite this, our method identifies that the model performs poorly during these periods as
671 we would expect, indicating that caution is warranted when performing HF modelling with the IRI
672 near the terminator.

673 Whilst our technique may be applied to any radar in the network, further caution is required when
674 using radars with the LPDA array due to the requirement to use the FOV detection algorithm. Despite
675 the algorithm providing reliable classification of most echoes, the impact of unassigned echoes
676 thinning the data can hinder a robust analysis. In the case that LE echoes are unassigned, the LE will
677 appear further in range and may suggest either errors in the model or an improved agreement; both of
678 which may not be true. This is a notable limitation of our method, and it is hoped that improvements
679 can be achieved through optimisation of the FOV algorithm parameters.

680 In all backscatter simulated by the model, a considerable overestimate of the trailing edge extent has
681 been noted and attributed to the power normalisation technique included herein. Beyond limitations in
682 the approach, the problem is likely related to the quality of the default D-region model in the IRI-2016
683 resulting in incorrect absorption estimates. Future comparison of the IRI-2016 model with a different
684 D-region model, such as that from the Faraday International Reference Ionosphere (FIRI) (Friedrich
685 et al., 2018), will provide evidence on the origin of the trailing edge overestimate. Better agreement
686 with SuperDARN backscatter in this case will support the normalisation technique and demonstrate
687 that the inconsistency is representative of the model description. However, further investigation in this
688 area is required. We therefore restrict our current analysis of the trailing edge as it is not necessarily
689 indicative of the model.

690 The formation of Sporadic-E layers at midlatitudes is a significant issue for HF radars operating in
691 these regions during the summertime when Sporadic-E, caused by convergence by diurnal and semi-
692 diurnal tides (Haldoupis, 2011; Hodos et al., 2022; Kunduri et al., 2023), is quite common as these
693 formations can significantly degrade the performance of such radars by limiting the maximum ranges
694 that can be reached. Plasma comprising Sporadic-E layers is often of sufficiently high density that it is
695 capable of blanketing propagation to higher regions of the ionosphere by reflecting HF radio waves at
696 a wide range of elevation angles in this lower region. As our current focus is on assessments of the 1F

697 echo variations, we see this as a significant limitation for the SuperDARN data, which limits our
698 current analysis to periods where Sporadic-E is not present. The blanketing effect of Sporadic-E is a
699 phenomenon that limits validation using any ground-based HF instruments. Besides not entirely
700 blocking the F-region, auroral-E echoes are also observed in some of the data and indicate a further
701 source of ionisation that can present significant departures between the modelled propagation with
702 that of the real ionosphere. We have previously demonstrated the sensitivity of OTHR coverage and
703 propagation with aurora, including the occurrence of ducted modes (Ruck & Themens, 2021).

704 This raises the important question of whether errors calculated for models where E-region echoes
705 such as Sporadic-E, auroral-E, and meteor scatter are not removed is a more thorough validation; we
706 follow the opinion that whilst this would result in the truest validation, it serves little purpose beyond
707 degrading the usefulness of such comparisons for ionospheric models that do not contain deliberate
708 considerations to these features. The problem of Sporadic-E we experience in the Blackstone radar
709 data, and our removal efforts highlights the significant impact of not including these ionisation
710 features in models. It is also important to note that whilst we remove E-region echoes in our
711 comparisons, it is obvious that the actual ionisation in the real ionosphere remains and will have an
712 impact on the cumulative path of propagating radio waves reflected by the F-region.

713 Although E-region echoes present a challenge for our current analysis, we see notable success with
714 our cluster-based filtering approach in this task, which may be applicable to studies focussed on the
715 automatic detection of Sporadic-E and auroral-E in the context of climatological assessments. We
716 observed Sporadic-E to occur for a considerable proportion of the summer months we investigate here
717 with substantial modifications to the propagation environment seen. To this end, the performance of
718 operational systems without inclusion of Sporadic-E models is expected to be catastrophic for
719 midlatitude OTHR, particularly for the FMS where the notable modifications to available ranges
720 manifest as incorrect coverage predictions with errors in excess of 1,000 km. Furthermore, the same
721 problem applies to Arctic OTHR operating within the vicinity of the aurora (Ruck & Themens, 2021).

722 It is these considerations that motivate the development of regional ionospheric models such as that of
723 the Empirical Canadian High Arctic Ionospheric Model (E-CHAIM) (Themens et al., 2018; Themens

724 et al., 2017; Themens et al., 2019; Watson et al., 2021) or GPS Ionospheric Inversion (GPSII)
725 (Fridman et al., 2006; Fridman et al., 2009) that can represent a greater proportion of the features
726 observed in the regional ionosphere.

727 Due to the significant information that can be gained from assessment of the SuperDARN range-
728 elevation distributions on NmF2 and hmF2, we envision this data set as being highly suitable for
729 validation or assimilation into RTIMs. Such use demands that a reliable means of interferometer
730 calibration monitoring can be performed in real time using an automated technique such as that by
731 Ponomarenko et al. (2018). This is required to ensure significant non-physical changes in elevation
732 angle are detected and not included into the assimilation. In this work we have not considered the
733 impact of thickness parameters on the range-elevation distributions and the information that may be
734 ascertained. It is expected that the use of ionospheric models utilizing data assimilation schemes will
735 show much reduced errors in LE due to their better representation of the immediate ionosphere.

736

737 **5. Conclusions**

738 We have demonstrated a new technique for performing validation of ionospheric models using the
739 SuperDARN ground backscatter data set. Our method has shown utility in assessing model errors at a
740 range of timescales for propagation contextually relevant for OTHR operation. The LE based
741 assessment provides a contextualisation of what positional accuracy we may expect in OTHR
742 coordinate registration and how this may vary through time for a given model. We show that analysis
743 of range-elevation distributions permits significant information to be gleaned on the origin of model
744 errors with good agreement with ionosonde values. Beyond this, we provide context to the extent of
745 elevation calibration errors on the echo distributions and show they can be significant in the context of
746 NmF2 errors. The demonstration of ionosonde driven model backscatter conclusively shows that
747 model performance can be dramatically improved by better representations of NmF2, with
748 improvements of ~800 km observed during the nighttime. For the IRI-2016 model, we observed
749 monthly averaged RMS leading edge errors consistently below 400 km during the daytime hours of

750 January 2014 and 2018, with significant increases during the nighttime and as the terminator
751 approaches. Overall model performance was seen to be considerably worse during summer, with this
752 attributed to the addition of more propagation modes and blanketing Sporadic-E degrading our data.
753 We note the critical importance of including Sporadic-E in operational models for midlatitude systems
754 as it is expected to be catastrophic for HF radar operation if not appropriately considered. Based on
755 our current analysis of IRI-2016 performance at Blackstone, we believe this method provides a
756 distinct opportunity to perform quantitative validation campaigns of models over a wide range of
757 geographical areas and time periods by expanding analysis to other radars in the network.

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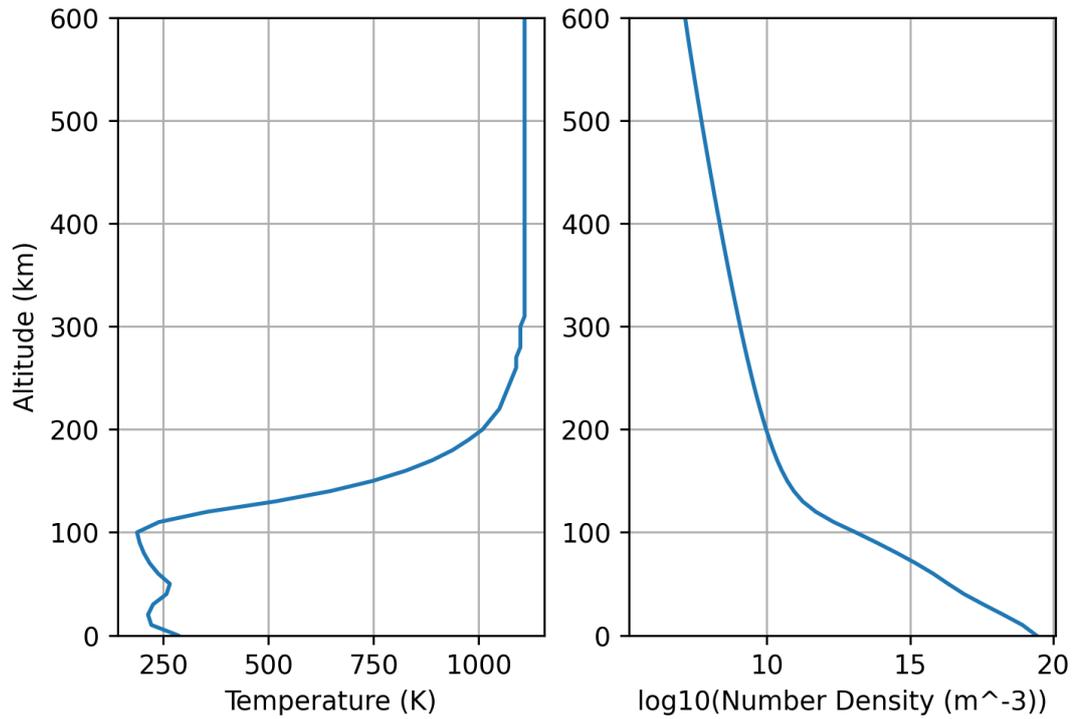
769 **Open Research**

770 Antenna radiation patterns modelled and used in this validation study are available for access and
771 download from Zenodo via <https://doi.org/10.5281/zenodo.10797004>. All validation data produced in
772 this study for figures and analysis is available for access and download from Zenodo via
773 <https://doi.org/10.5281/zenodo.10797245>. The International Reference Ionosphere (IRI) model is
774 available from the following website <https://irimodel.org/>. The High Frequency Radar Model (HFRM)

775 used to model propagation is the proprietary property of the Space Environment and Radio
 776 Engineering (SERENE) group at the University of Birmingham and is not available for distribution.

777 **Appendix**

778 **1. Neutral temperature and density profiles**



779

780 *Neutral atmosphere temperature and number density profiles used to calculate ionospheric absorption.*

781 **2. T_{diff} values**

T _{diff} (ms)	2014	2018
January	-0.322	-0.330
June	-0.332	-0.327

782 *Interferometer calibration values for each month of the validation period. During periods of high noise during January*
 783 *2014, an alternate value of -0.320 ms is used. This data is also available in the data availability section.*

784

785

786 **References**

787 Bland, E. C., McDonald, A. J., de Larquier, S., & Devlin, J. C. (2014). Determination of ionospheric
788 parameters in real time using SuperDARN HF Radars [<https://doi.org/10.1002/2014JA020076>].
789 Journal of Geophysical Research: Space Physics, 119(7), 5830-5846.
790 <https://doi.org/https://doi.org/10.1002/2014JA020076>

791 Burke, G. J., & Poggio, A. J. (1981). Numerical Electromagnetics Code (NEC) - Method of Moments.
792 Part 1: Program Description - Theory. <http://www.nec2.org/other/nec2prt1.pdf>

793 Chakraborty, S., Ruohoniemi, J. M., Baker, J. B. H., & Nishitani, N. (2018). Characterization of short-
794 wave fadeout seen in daytime SuperDARN ground scatter observations. Radio Science, 53, 472–484.
795 <https://doi.org/10.1002/2017RS006488>

796 Chen, J., Ren, X., Zhang, X., Zhang, J., & Huang, L. (2020). Assessment and Validation of Three
797 Ionospheric Models (IRI-2016, NeQuick2, and IGS-GIM) From 2002 to 2018. Space Weather, 18(6),
798 e2019SW002422. <https://doi.org/https://doi.org/10.1029/2019SW002422>

799 Chisham, G., Burrell, A. G., Marchaudon, A., Shepherd, S. G., Thomas, E. G., & Ponomarenko, P.
800 (2021). Comparison of interferometer calibration techniques for improved SuperDARN elevation
801 angles. Polar Science, 28, 100638. <https://doi.org/https://doi.org/10.1016/j.polar.2021.100638>

802 Chisham, G., Yeoman, T. K., & Sofko, G. J. (2008). Mapping ionospheric backscatter measured by
803 the SuperDARN HF radars – Part 1: A new empirical virtual height model. Ann. Geophys.,
804 26(4), 823-841. <https://doi.org/10.5194/angeo-26-823-2008>

805 Chisham, G., Lester, M., Milan, S. E., Freeman, M. P., Bristow, W. A., Grocott, A., McWilliams, K.
806 A., Ruohoniemi, J. M., Yeoman, T. K., Dyson, P. L., Greenwald, R. A., Kikuchi, T., Pinnock, M.,
807 Rash, J. P. S., Sato, N., Sofko, G. J., Villain, J. P., & Walker, A. D. M. (2007). A decade of the Super
808 Dual Auroral Radar Network (SuperDARN): scientific achievements, new techniques and future
809 directions. Surveys in Geophysics, 28(1), 33-109. <https://doi.org/10.1007/s10712-007-9017-8>

810 Chou, M.-Y., Yue, J., Wang, J., Huba, J. D., El Alaoui, M., Kuznetsova, M. M., Rastätter, L., Shim, J.
811 S., Fang, T.-W., Meng, X., Fuller-Rowell, D., & Retterer, J. M. (2023). Validation of Ionospheric

812 Modeled TEC in the Equatorial Ionosphere During the 2013 March and 2021 November Geomagnetic
813 Storms. *Space Weather*, 21(6), e2023SW003480.
814 <https://doi.org/https://doi.org/10.1029/2023SW003480>

815 Coleman, C. J. (1997). On the simulation of backscatter ionograms. *Journal of Atmospheric and*
816 *Solar-Terrestrial Physics*, 59(16), 2089-2099. <https://doi.org/https://doi.org/10.1016/S1364->
817 [6826\(97\)00038-2](https://doi.org/https://doi.org/10.1016/S1364-6826(97)00038-2)

818 Coleman, C. J. (1998). A ray tracing formulation and its application to some problems in over-the-
819 horizon radar [<https://doi.org/10.1029/98RS01523>]. *Radio Science*, 33(4), 1187-1197.
820 <https://doi.org/https://doi.org/10.1029/98RS01523>

821 Custovic, E., Nguyen, H. Q., Devlin, J. C., Whittington, J., Elton, D., Console, A., Ye, H., Greenwald,
822 R. A., Andre, D. A., & Parsons, M. J. (2011, 21-24 Nov. 2011). Evolution of the SuperDARN antenna:
823 twin terminated folded dipole antenna for HF systems. 7th International Conference on Broadband
824 Communications and Biomedical Applications,

825 Davies, K. (1965). *Ionospheric Radio Propagation*. United States Department of Commerce, National
826 Bureau of Standards.

827 Edwards, D., & Cervera, M. (2022). Seasonal Variation in Land and Sea Surface Backscatter
828 Coefficients at High Frequencies. *Remote Sensing*, 14(21), 5514. <https://www.mdpi.com/2072->
829 [4292/14/21/5514](https://www.mdpi.com/2072-4292/14/21/5514)

830 Edwards, D., Cervera, M., & MacKinnon, A. (2022). A Comparison of the Barrick and Backscatter
831 Ionogram Methods of Calculating Sea Surface Backscatter Coefficients. *Remote Sensing*, 14(9).

832 Ester, M., Kriegel, H.-P., Sander, J., & Xu, X. (1996). A density-based algorithm for discovering
833 clusters in large spatial databases with noise *Proceedings of the Second International Conference on*
834 *Knowledge Discovery and Data Mining*, Portland, Oregon.

835 Fabrizio, G. A. (2013). *High Frequency Over-the-Horizon Radar: Fundamental Principles, Signal*
836 *Processing, and Practical Applications*. MCGRAW-HILL Professional.

837 Forsythe, V. V., Azeem, I., & Crowley, G. (2020). Ionospheric Horizontal Correlation Distances:
838 Estimation, Analysis, and Implications for Ionospheric Data Assimilation. *Radio Science*, 55(12),
839 e2020RS007159. <https://doi.org/https://doi.org/10.1029/2020RS007159>

840 Fridman, S. V., Nickisch, L. J., Aiello, M., & Hausman, M. (2006). Real-time reconstruction of the
841 three-dimensional ionosphere using data from a network of GPS receivers
842 [<https://doi.org/10.1029/2005RS003341>]. *Radio Science*, 41(5).
843 <https://doi.org/https://doi.org/10.1029/2005RS003341>

844 Fridman, S. V., Nickisch, L. J., & Hausman, M. (2009). Personal-computer-based system for real-time
845 reconstruction of the three-dimensional ionosphere using data from diverse sources
846 [<https://doi.org/10.1029/2008RS004040>]. *Radio Science*, 44(3).
847 <https://doi.org/https://doi.org/10.1029/2008RS004040>

848 Fridman, S. V., Nickisch, L. J., & Hausman, M. (2012). Inversion of backscatter ionograms and TEC
849 data for over-the-horizon radar [<https://doi.org/10.1029/2011RS004932>]. *Radio Science*, 47(4).
850 <https://doi.org/https://doi.org/10.1029/2011RS004932>

851 Friedrich, M., Pock, C., & Torkar, K. (2018). FIRI-2018, an Updated Empirical Model of the Lower
852 Ionosphere. *Journal of Geophysical Research: Space Physics*, 123(8), 6737-6751.
853 <https://doi.org/https://doi.org/10.1029/2018JA025437>

854 Gillies, R. G., Hussey, G. C., Sofko, G. J., McWilliams, K. A., Fiori, R. A. D., Ponomarenko, P., &
855 St.-Maurice, J. P. (2009). Improvement of SuperDARN velocity measurements by estimating the
856 index of refraction in the scattering region using interferometry. *Journal of Geophysical Research:*
857 *Space Physics*, 114(A7). <https://doi.org/https://doi.org/10.1029/2008JA013967>

858 Greenwald, R. A., Baker, K. B., Hutchins, R. A., & Hanuise, C. (1985). An HF phased-array radar for
859 studying small-scale structure in the high-latitude ionosphere
860 [<https://doi.org/10.1029/RS020i001p00063>]. *Radio Science*, 20(1), 63-79.
861 <https://doi.org/https://doi.org/10.1029/RS020i001p00063>

862 Greenwald, R. A., Baker, K. B., Dudeney, J. R., Pinnock, M., Jones, T. B., Thomas, E. C., et al.
863 (1995). DARN/SUPERDARN. *Space Science Reviews*, 71(1–4), 761–796.
864 <https://doi.org/10.1007/BF00751350>

865 Haselgrove, J. (1955). Ray Theory and a New Method for Ray Tracing.

866 Hodos, T. J., Nava, O. A., Dao, E. V., & Emmons, D. J. (2022). Global Sporadic-E Occurrence Rate
867 Climatology Using GPS Radio Occultation and Ionosonde Data. *Journal of Geophysical Research:*
868 *Space Physics*, 127(12), e2022JA030795. <https://doi.org/https://doi.org/10.1029/2022JA030795>

869 Hughes, J. M., Bristow, W. A., Greenwald, R. A., & Barnes, R. J. (2002). Determining characteristics
870 of HF communications links using SuperDARN. *Ann. Geophys.*, 20(7), 1023-1030.
871 <https://doi.org/10.5194/angeo-20-1023-2002>

872 Jiang, W., Liu, E., Kong, X., Shi, S., & Liu, J. (2022). Zhongshan HF Radar Elevation Calibration
873 Based on Ground Backscatter Echoes. *Electronics*, 11(24).

874 Koustov, A. V., Ullrich, S., Ponomarenko, P. V., Ghalamkarian Nejad, M., Themens, D. R., & Gillies,
875 R. G. (2022). Occurrence Rates of SuperDARN Ground Scatter Echoes and Electron Density in the
876 Ionosphere. *Radio Science*, 57(11), e2022RS007520.
877 <https://doi.org/https://doi.org/10.1029/2022RS007520>

878 Kunduri, B. S. R., Erickson, P. J., Baker, J. B. H., Ruohoniemi, J. M., Galkin, I. A., & Sterne, K. T.
879 (2023). Dynamics of Mid-Latitude Sporadic-E and Its Impact on HF Propagation in the North
880 American Sector. *Journal of Geophysical Research: Space Physics*, 128(9), e2023JA031455.
881 <https://doi.org/https://doi.org/10.1029/2023JA031455>

882 Kunduri, B. S. R., Baker, J. B. H., Ruohoniemi, J. M., Thomas, E. G., & Shepherd, S. G. (2022). An
883 Examination of SuperDARN Backscatter Modes Using Machine Learning Guided by Ray-Tracing.
884 *Space Weather*, 20(9), e2022SW003130. <https://doi.org/https://doi.org/10.1029/2022SW003130>

885 Martyn, D. F. (1935). The propagation of medium radio waves in the ionosphere. *Proceedings of the*
886 *Physical Society*, 47(2), 323. <https://doi.org/10.1088/0959-5309/47/2/311>

887 Munk, W. H., & Nierenberg, W. A. (1969). High Frequency Radar Sea Return and the Phillips
888 Saturation Constant. *Nature*, 224(5226), 1285-1285. <https://doi.org/10.1038/2241285a0>

889 Nishitani, N., Ruohoniemi, J. M., Lester, M., Baker, J. B. H., Koustov, A. V., Shepherd, S. G.,
890 Chisham, G., Hori, T., Thomas, E. G., Makarevich, R. A., Marchaudon, A., Ponomarenko, P., Wild, J.
891 A., Milan, S. E., Bristow, W. A., Devlin, J., Miller, E., Greenwald, R. A., Ogawa, T., & Kikuchi, T.
892 (2019). Review of the accomplishments of mid-latitude Super Dual Auroral Radar Network
893 (SuperDARN) HF radars. *Progress in Earth and Planetary Science*, 6(1), 27.
894 <https://doi.org/10.1186/s40645-019-0270-5>

895 Oinats, A. V., Nishitani, N., Ponomarenko, P., & Ratovsky, K. G. (2016). Diurnal and seasonal
896 behavior of the Hokkaido East SuperDARN ground backscatter: simulation and observation. *Earth,*
897 *Planets and Space*, 68(1), 18. <https://doi.org/10.1186/s40623-015-0378-9>

898 Perry, G. W., Ruzic, K. D., Sterne, K., Howarth, A. D., & Yau, A. W. (2022). Modeling and Validating
899 a SuperDARN Radar's Poynting Flux Profile [<https://doi.org/10.1029/2021RS007323>]. *Radio*
900 *Science*, 57(3), e2021RS007323. <https://doi.org/https://doi.org/10.1029/2021RS007323>

901 Ponomarenko, P., & McWilliams, K. A. (2023). Climatology of HF Propagation Characteristics at
902 Very High Latitudes From SuperDARN Observations. *Radio Science*, 58(5), e2023RS007657.
903 <https://doi.org/https://doi.org/10.1029/2023RS007657>

904 Ponomarenko, P., Nishitani, N., Oinats, A. V., Tsuya, T., & St.-Maurice, J.-P. (2015). Application of
905 ground scatter returns for calibration of HF interferometry data. *Earth, Planets and Space*, 67(1), 138.
906 <https://doi.org/10.1186/s40623-015-0310-3>

907 Ponomarenko, P., St.-Maurice, J.-P., & McWilliams, K. A. (2018). Calibrating HF Radar Elevation
908 Angle Measurements Using E Layer Backscatter Echoes. *Radio Science*, 53(11), 1438-1449.
909 <https://doi.org/https://doi.org/10.1029/2018RS006638>

910 Ponomarenko, P. V., St. Maurice, J. P., Hussey, G. C., & Koustov, A. V. (2010). HF ground scatter
911 from the polar cap: Ionospheric propagation and ground surface effects

912 [<https://doi.org/10.1029/2010JA015828>]. *Journal of Geophysical Research: Space Physics*, 115(A10).
913 <https://doi.org/https://doi.org/10.1029/2010JA015828>

914 AJ Ribeiro, Kevin Sterne, Sebastien de Larquier, Ashton Reimer, Matt Wessel, Muhammad Rafiq
915 (Maimaitirebike Maimaiti), Jef Spaleta, Angeline Burrell, Bharat Kunduri, Xueling Shi, Christer van
916 der Meeren, Pål Ellingsen, Ray Greenwald, Nathaniel Frissell, Anurag Sharma, & Phil Erickson.
917 (2020). vtsuperdarn/davitpy: Final release of davitpy (v0.9). Zenodo.
918 <https://doi.org/10.5281/zenodo.3824466>

919 Ruck, J. J., & Themens, D. R. (2021). Impacts of Auroral Precipitation on HF Propagation: A
920 Hypothetical Over-the-Horizon Radar Case Study. *Space Weather*, 19(12), e2021SW002901.
921 <https://doi.org/https://doi.org/10.1029/2021SW002901>

922 Shepherd, S. G. (2017). Elevation angle determination for SuperDARN HF radar layouts. *Radio*
923 *Science*, 52(8), 938-950. <https://doi.org/https://doi.org/10.1002/2017RS006348>

924 Samson, J. C., R. A. Greenwald, J. M. Ruohoniemi, A. Frey, and K. B. Baker (1990), Goose Bay radar
925 observations of Earth-reflected, atmospheric gravity waves in the high-latitude ionosphere, *J.*
926 *Geophys. Res.*, 95(A6), 7693–7709, doi:10.1029/JA095iA06p07693.

927 Shim, J. S., Kuznetsova, M., Rastätter, L., Bilitza, D., Butala, M., Codrescu, M., Emery, B. A., Foster,
928 B., Fuller-Rowell, T. J., Huba, J., Mannucci, A. J., Pi, X., Ridley, A., Scherliess, L., Schunk, R. W.,
929 Sojka, J. J., Stephens, P., Thompson, D. C., Weimer, D., . . . Sutton, E. (2012). CEDAR
930 Electrodynamics Thermosphere Ionosphere (ETI) Challenge for systematic assessment of
931 ionosphere/thermosphere models: Electron density, neutral density, NmF2, and hmF2 using space
932 based observations [<https://doi.org/10.1029/2012SW000851>]. *Space Weather*, 10(10).
933 <https://doi.org/https://doi.org/10.1029/2012SW000851>

934 Shim, J. S., Kuznetsova, M., Rastätter, L., Hesse, M., Bilitza, D., Butala, M., Codrescu, M., Emery,
935 B., Foster, B., Fuller-Rowell, T., Huba, J., Mannucci, A. J., Pi, X., Ridley, A., Scherliess, L., Schunk,
936 R. W., Stephens, P., Thompson, D. C., Zhu, L., . . . Rideout, B. (2011). CEDAR Electrodynamics
937 Thermosphere Ionosphere (ETI) Challenge for systematic assessment of ionosphere/thermosphere

938 models: NmF2, hmF2, and vertical drift using ground-based observations
939 [<https://doi.org/10.1029/2011SW000727>]. Space Weather, 9(12).
940 <https://doi.org/https://doi.org/10.1029/2011SW000727>

941 Slimming, B., & Cervera, M. A. (2019). Calculation of High Frequency Land Backscatter
942 Coefficients. [https://www.dst.defence.gov.au/publication/calculation-high-frequency-land-backscatter-](https://www.dst.defence.gov.au/publication/calculation-high-frequency-land-backscatter-coefficients)
943 [coefficients](https://www.dst.defence.gov.au/publication/calculation-high-frequency-land-backscatter-coefficients)

944 Thayaparan, T., Marchioni, J., Kelsall, A., & Riddolls, R. (2020). Improved Frequency Monitoring
945 System for Sky-Wave Over-the-Horizon Radar in Canada. *IEEE Geoscience and Remote Sensing*
946 *Letters*, 17(4), 606-610. <https://doi.org/10.1109/LGRS.2019.2928172>

947 Themens, D. R., & Jayachandran, P. T. (2016). Solar activity variability in the IRI at high latitudes:
948 Comparisons with GPS total electron content [<https://doi.org/10.1002/2016JA022664>]. *Journal of*
949 *Geophysical Research: Space Physics*, 121(4), 3793-3807.
950 <https://doi.org/https://doi.org/10.1002/2016JA022664>

951 Themens, D. R., Jayachandran, P. T., Bilitza, D., Erickson, P. J., Häggström, I., Lyashenko, M. V.,
952 Reid, B., Varney, R. H., & Pustovalova, L. (2018). Topside Electron Density Representations for
953 Middle and High Latitudes: A Topside Parameterization for E-CHAIM Based On the NeQuick.
954 *Journal of Geophysical Research: Space Physics*, 123(2), 1603-1617.

955 Themens, D. R., Jayachandran, P. T., Galkin, I., & Hall, C. (2017). The Empirical Canadian High
956 Arctic Ionospheric Model (E-CHAIM): NmF2 and hmF2 [<https://doi.org/10.1002/2017JA024398>].
957 *Journal of Geophysical Research: Space Physics*, 122(8), 9015-9031.
958 <https://doi.org/https://doi.org/10.1002/2017JA024398>

959 Themens, D. R., Jayachandran, P. T., McCaffrey, A. M., Reid, B., & Varney, R. H. (2019). A
960 Bottomside Parameterization for the Empirical Canadian High Arctic Ionospheric Model. *Radio*
961 *Science*, 54(5), 397-414. <https://doi.org/https://doi.org/10.1029/2018RS006748>

962 Themens, D. R., Jayachandran, P. T., & McCaffrey, A. M. (2019). Validating the performance of the
 963 Empirical Canadian High Arctic Ionospheric Model (E-CHAIM) with in situ observations from
 964 DMSP and CHAMP. *J. Space Weather Space Clim.*, 9, A21. <https://doi.org/10.1051/swsc/2019021>

965 Theurer, T. E. and W. A. Bristow (2017), High-frequency radar ground clutter spatial correlation
 966 analysis: Transverse ionospheric drift velocity, *Radio Sci.*, 52, 461–478, doi:10.1002/2016RS006162.

967 Thomas, E. G., & Shepherd, S. G. (2022). Virtual Height Characteristics of Ionospheric and Ground
 968 Scatter Observed by Mid-Latitude SuperDARN HF Radars. *Radio Science*, 57(6), e2022RS007429.
 969 <https://doi.org/https://doi.org/10.1029/2022RS007429>

970 Watson, C., Themens, D. R., & Jayachandran, P. T. (2021). Development and Validation of
 971 Precipitation Enhanced Densities for the Empirical Canadian High Arctic Ionospheric Model
 972 [<https://doi.org/10.1029/2021SW002779>]. *Space Weather*, 19(10), e2021SW002779.
 973 <https://doi.org/https://doi.org/10.1029/2021SW002779>

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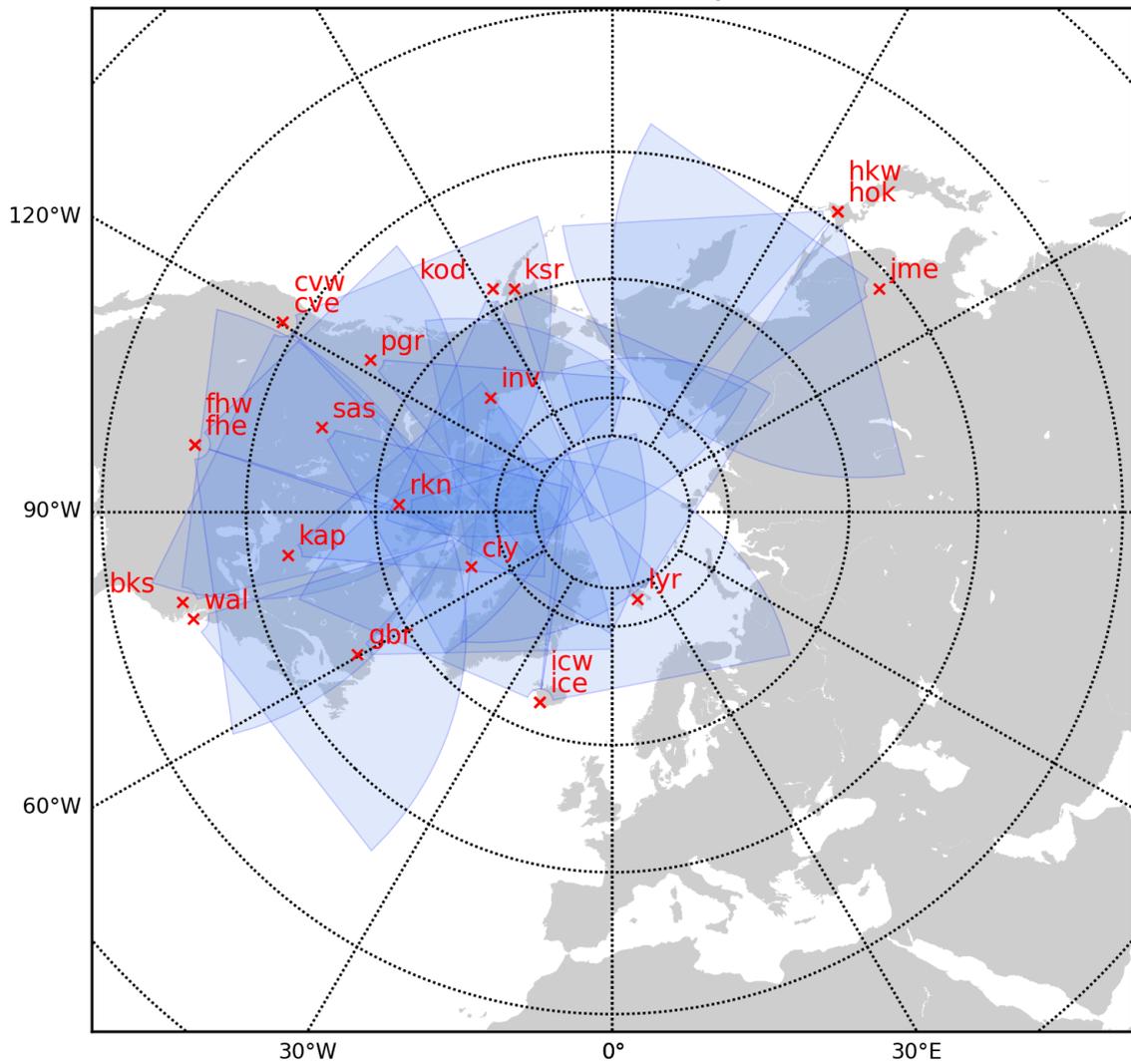
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Figure 1.

Northern Hemisphere



Southern Hemisphere

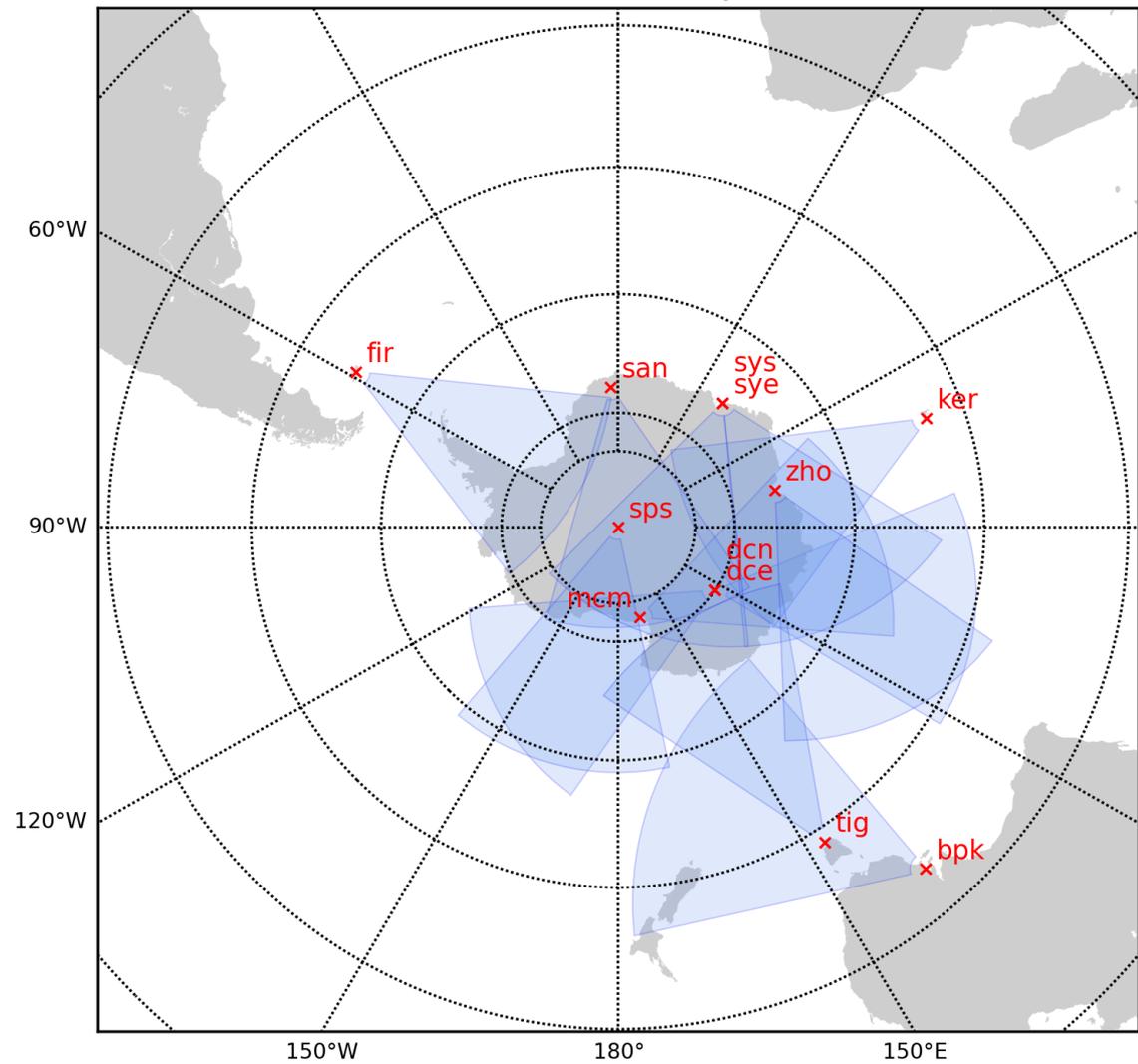


Figure 2.

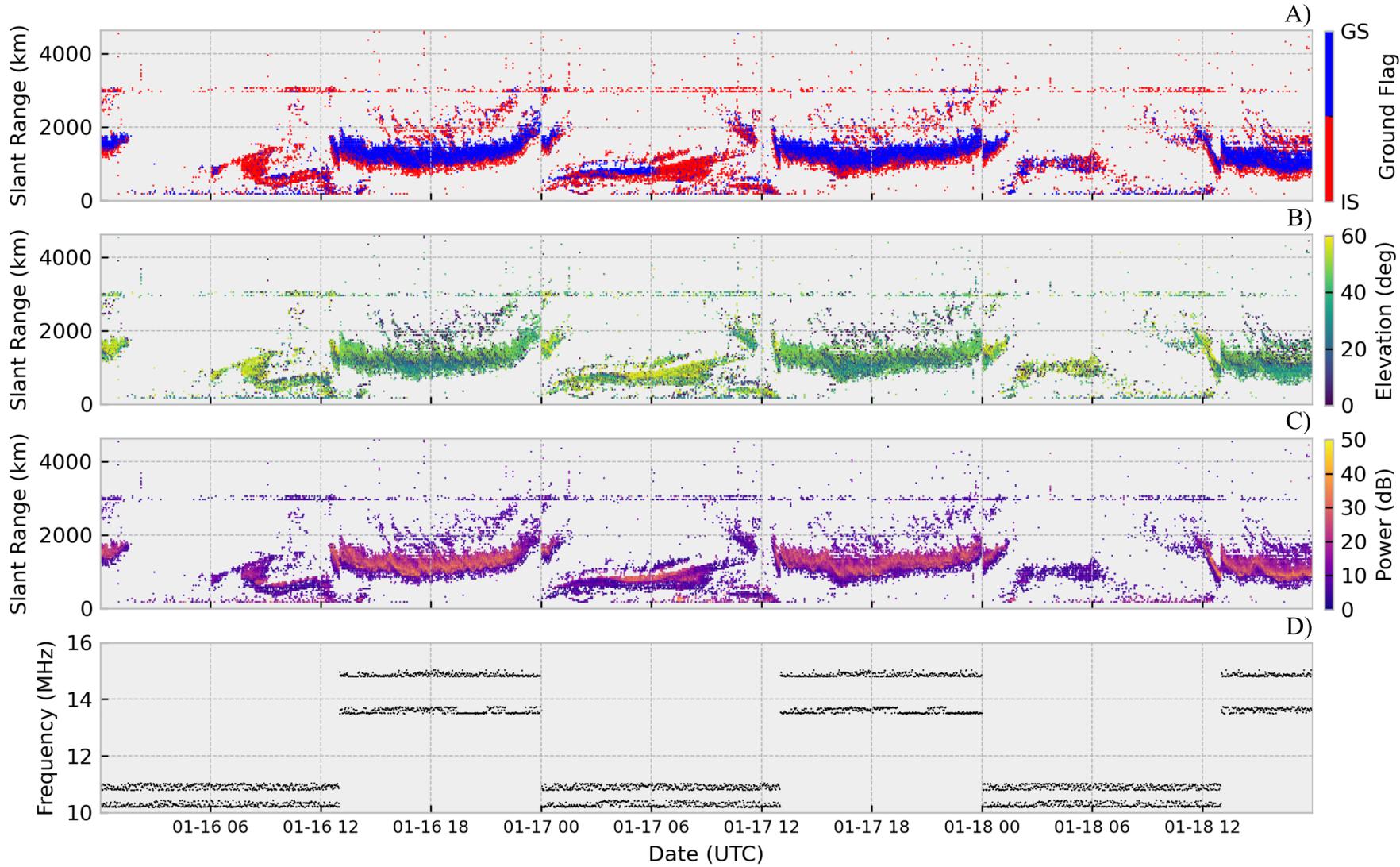


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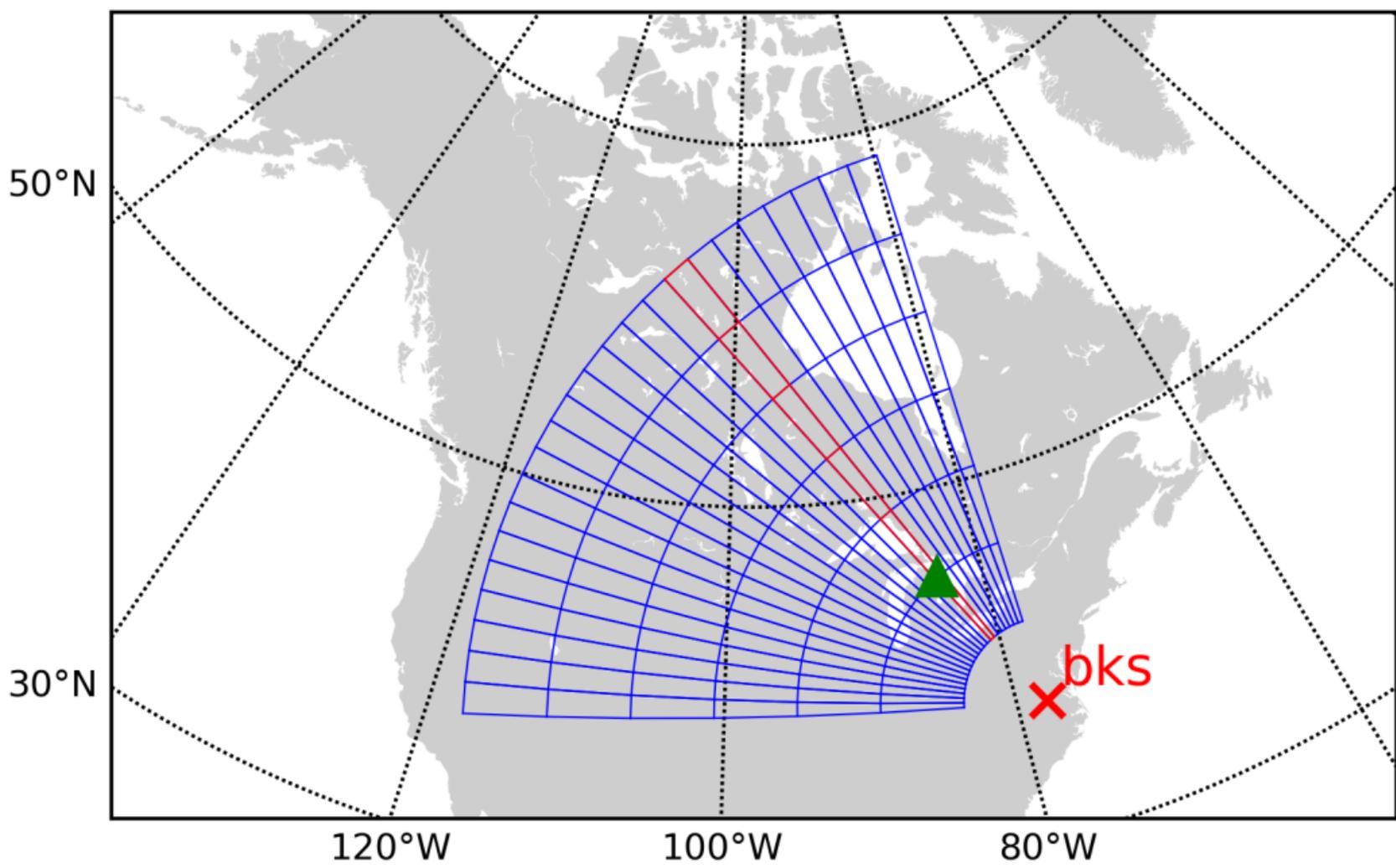


Figure 4.

Lat=[37.1], Lon=[-77.95], Ht=[0.] 25/01/2018, 18:00

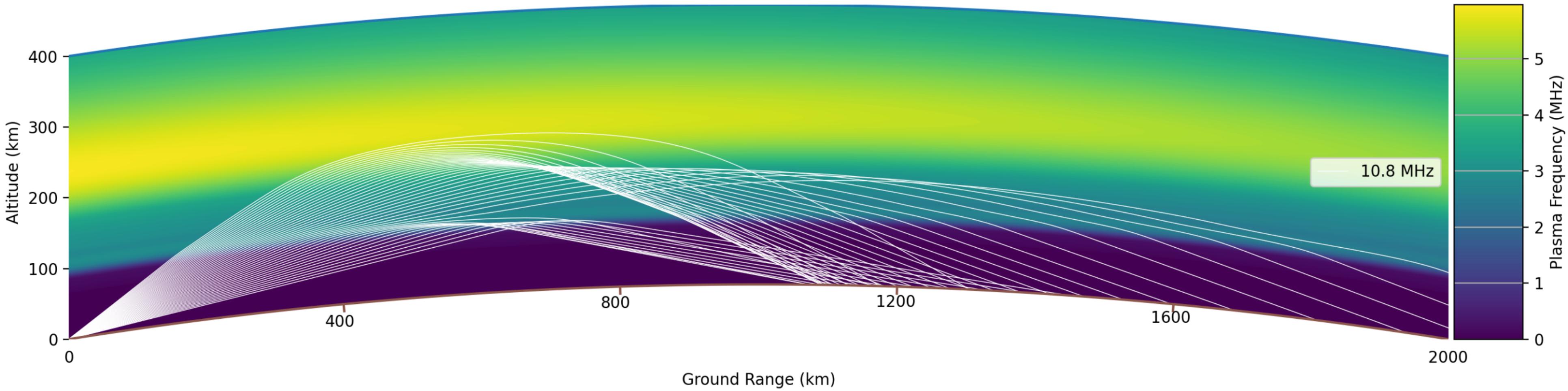


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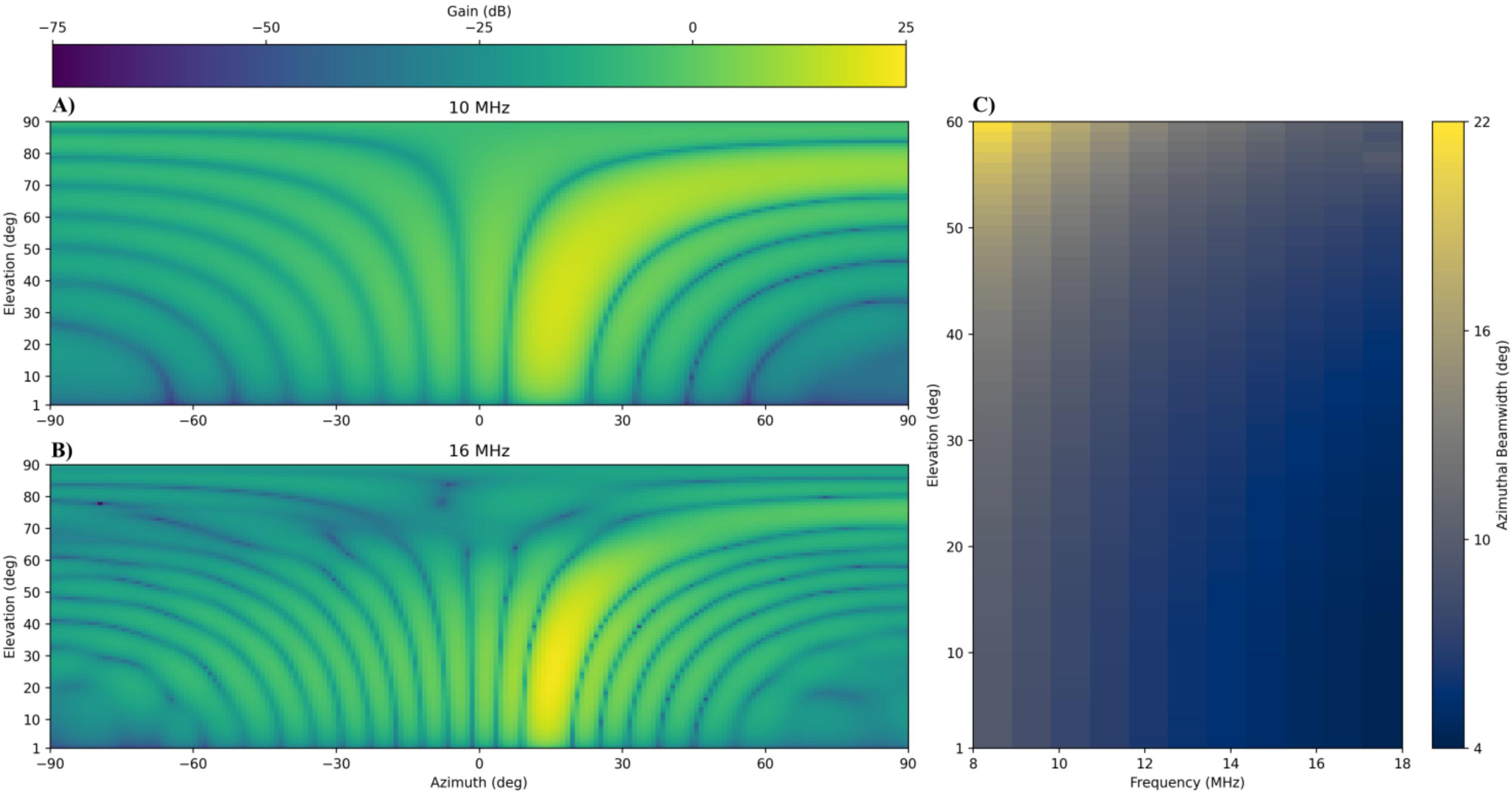


Figure 6.

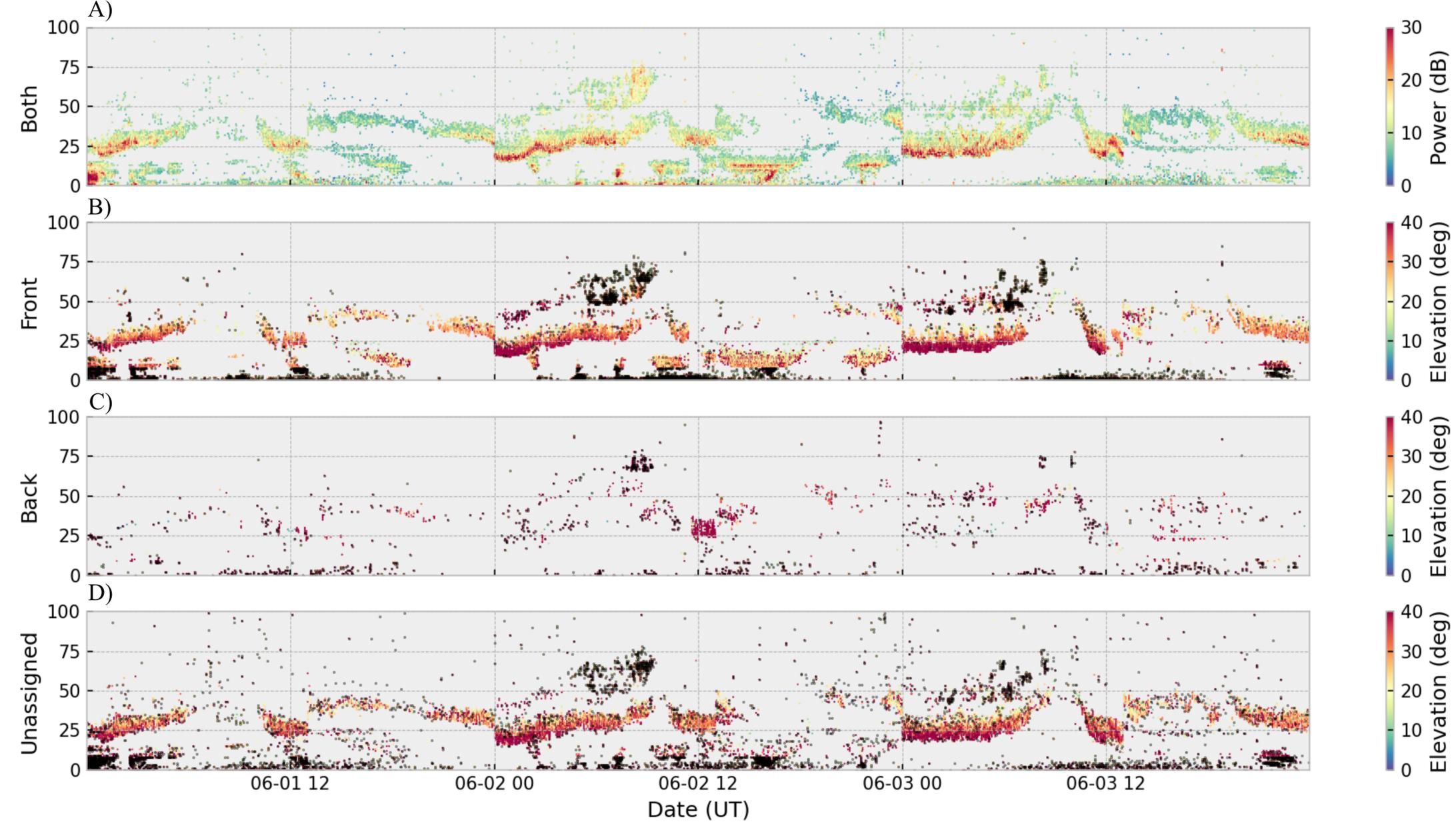


Figure 7.

Blackstone Radar

Model

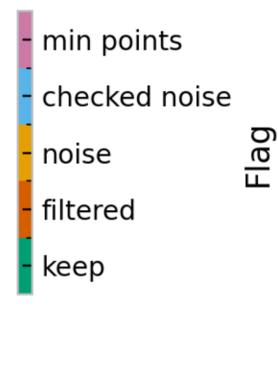
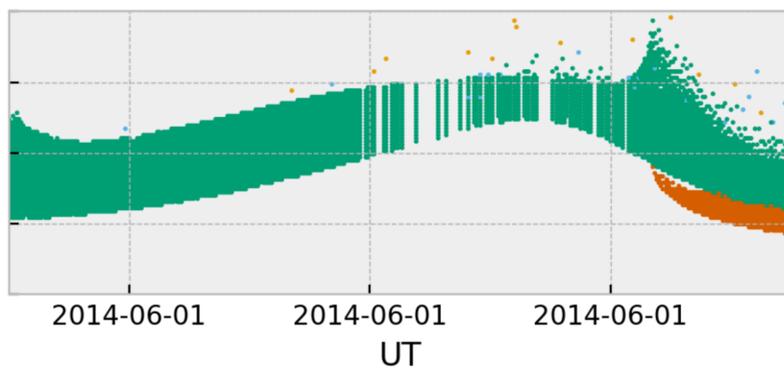
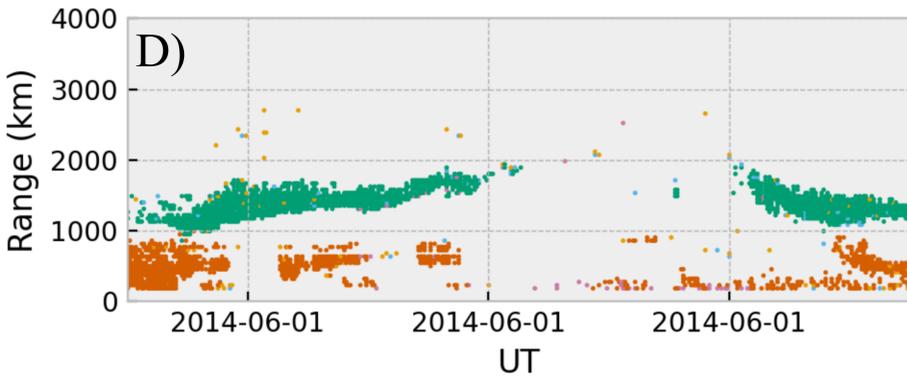
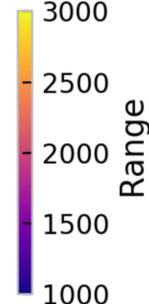
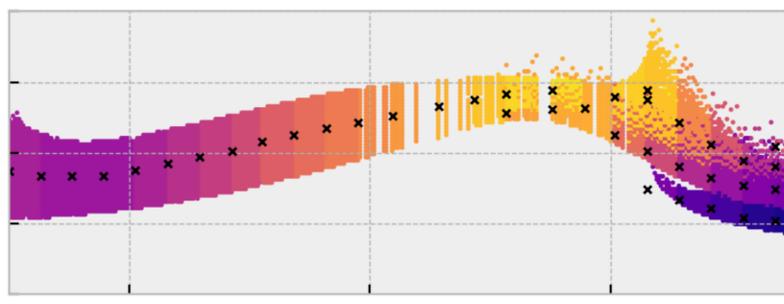
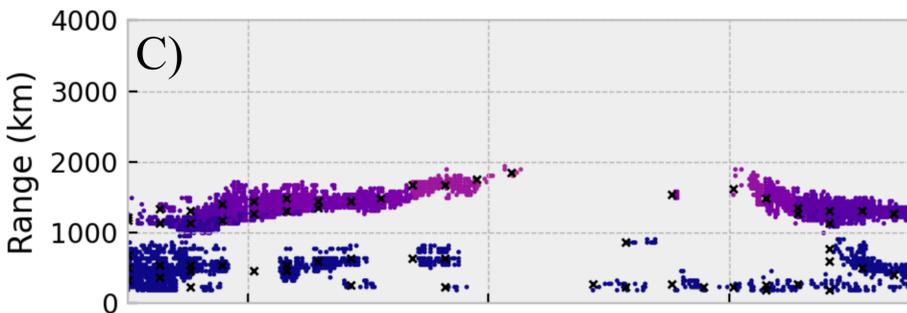
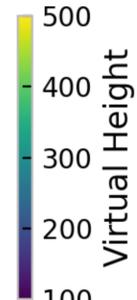
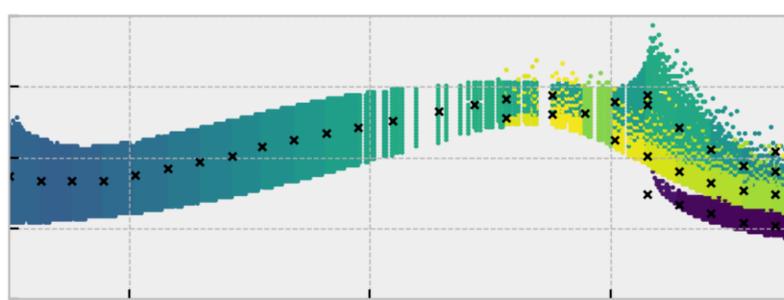
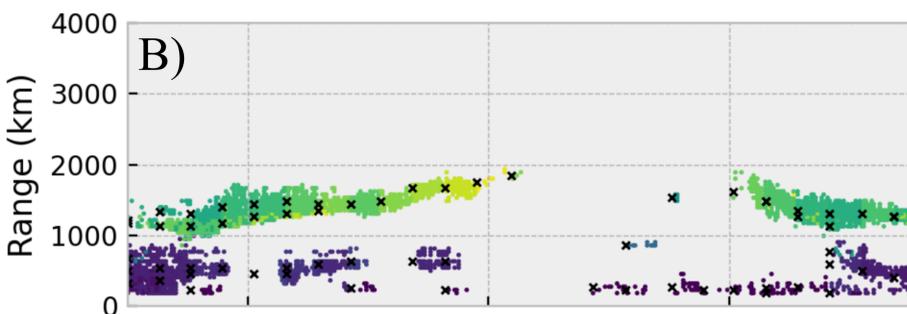
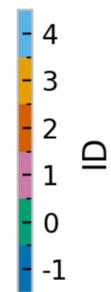
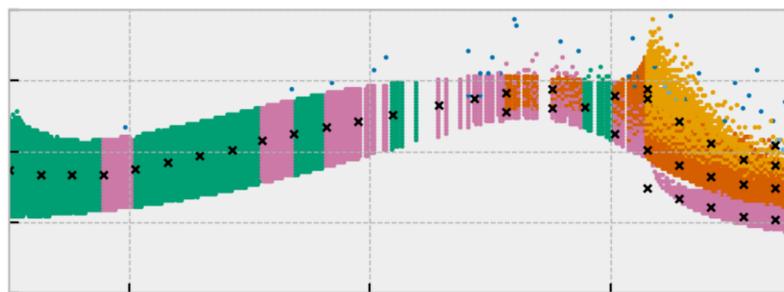
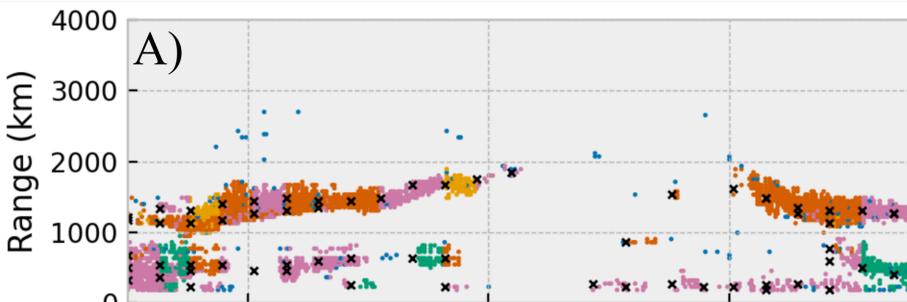


Figure 8.

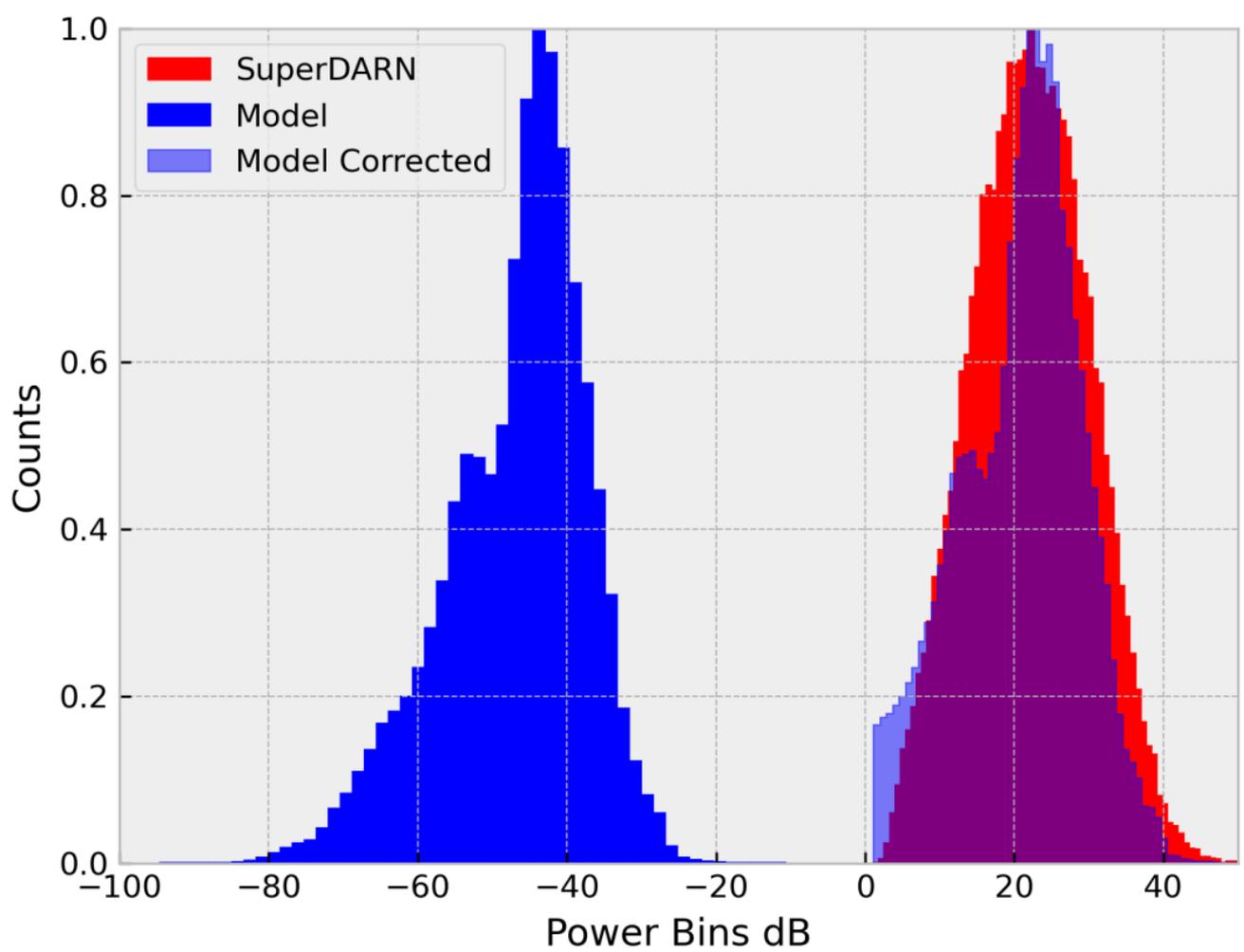


Figure 9.

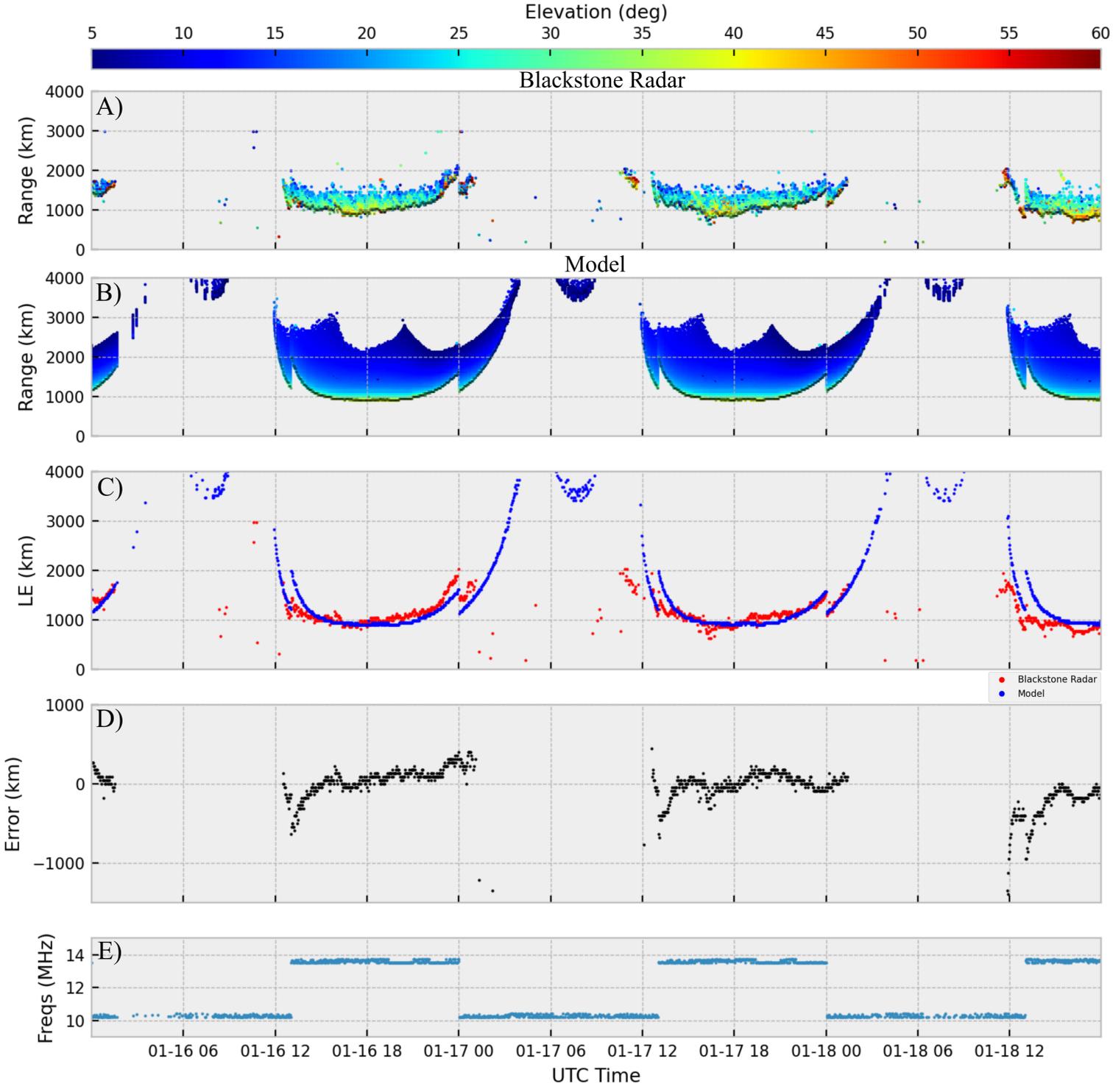


Figure 10.

Blackstone Radar

Model

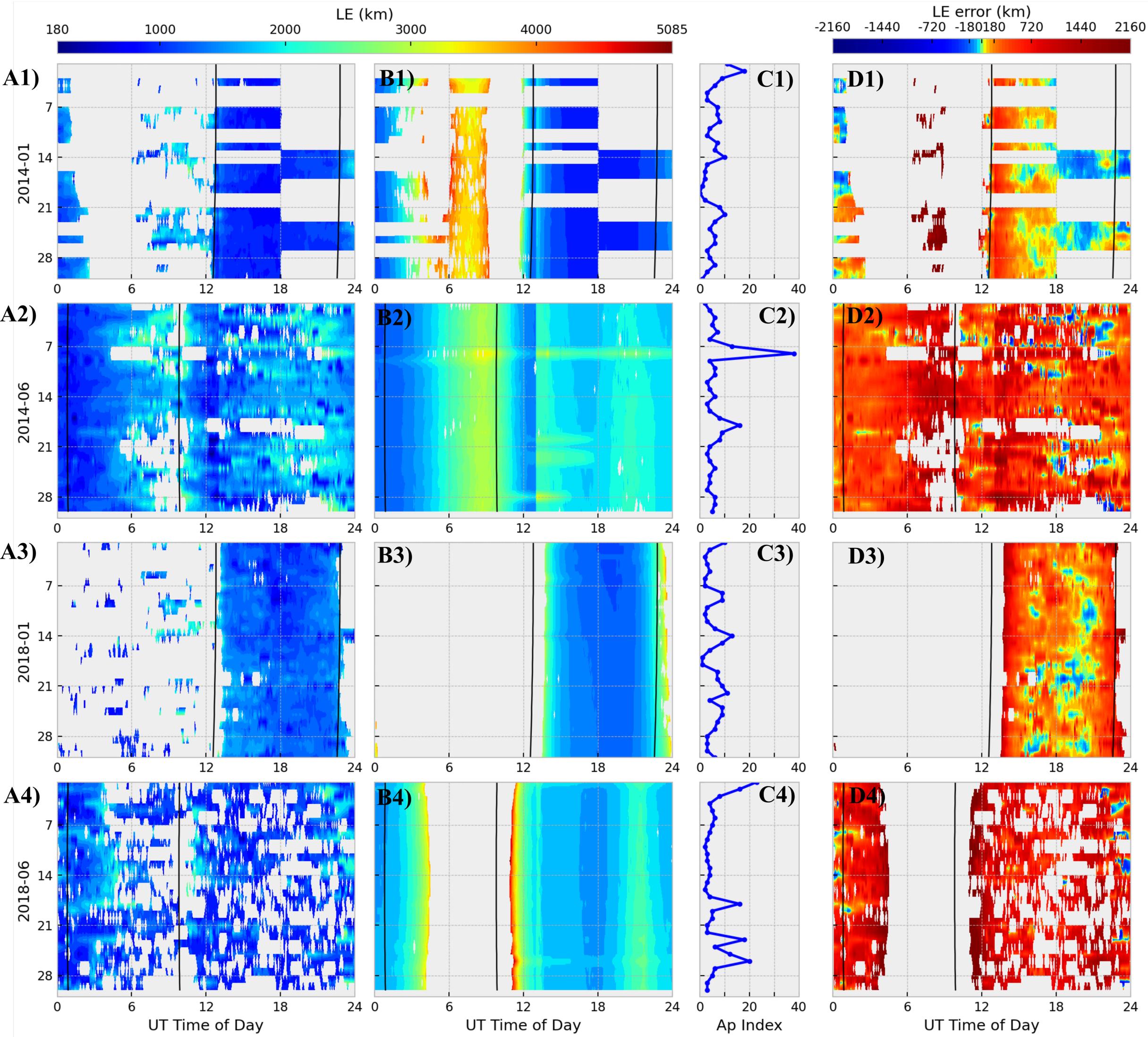


Figure 11.

Blackstone Radar

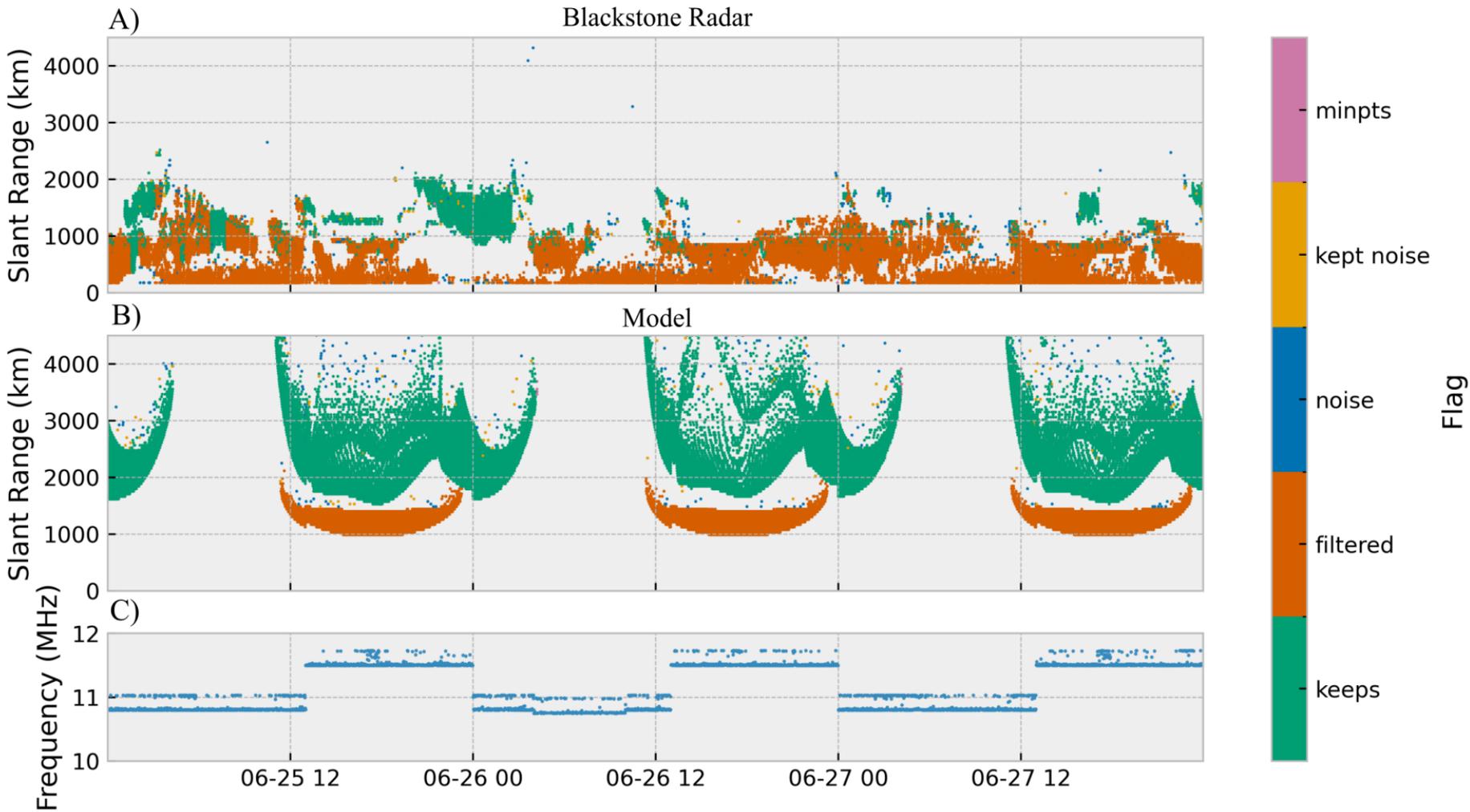
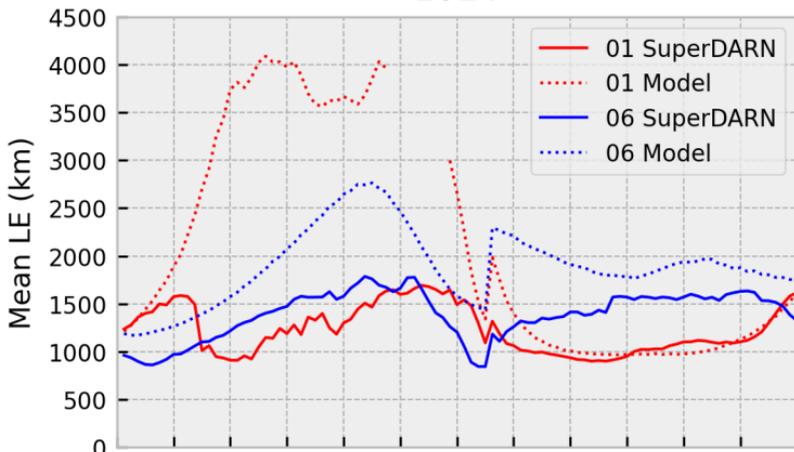


Figure 12.

2014



2018

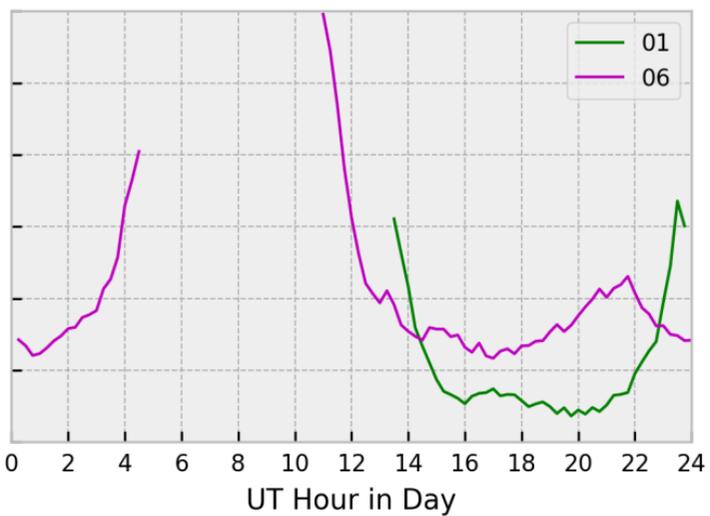
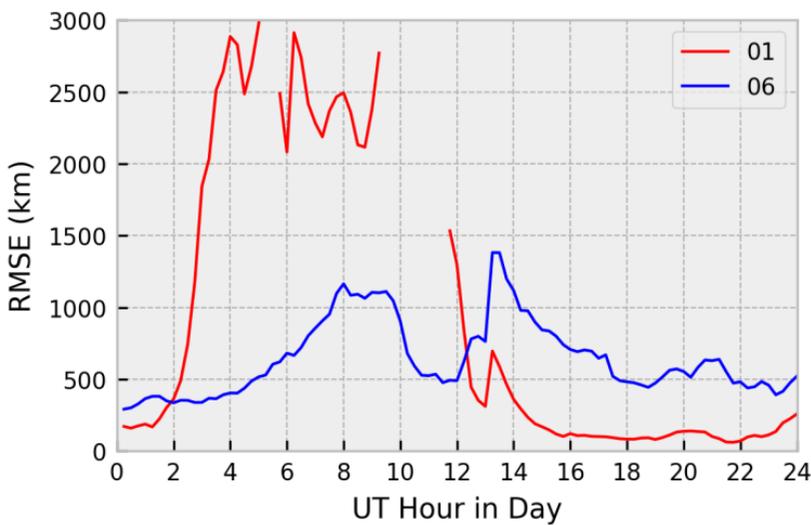
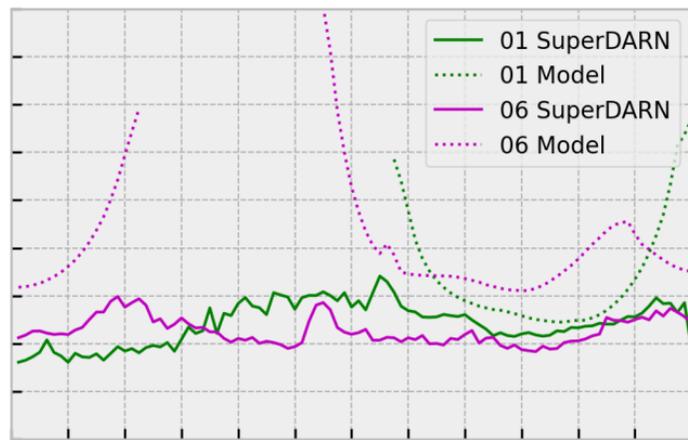


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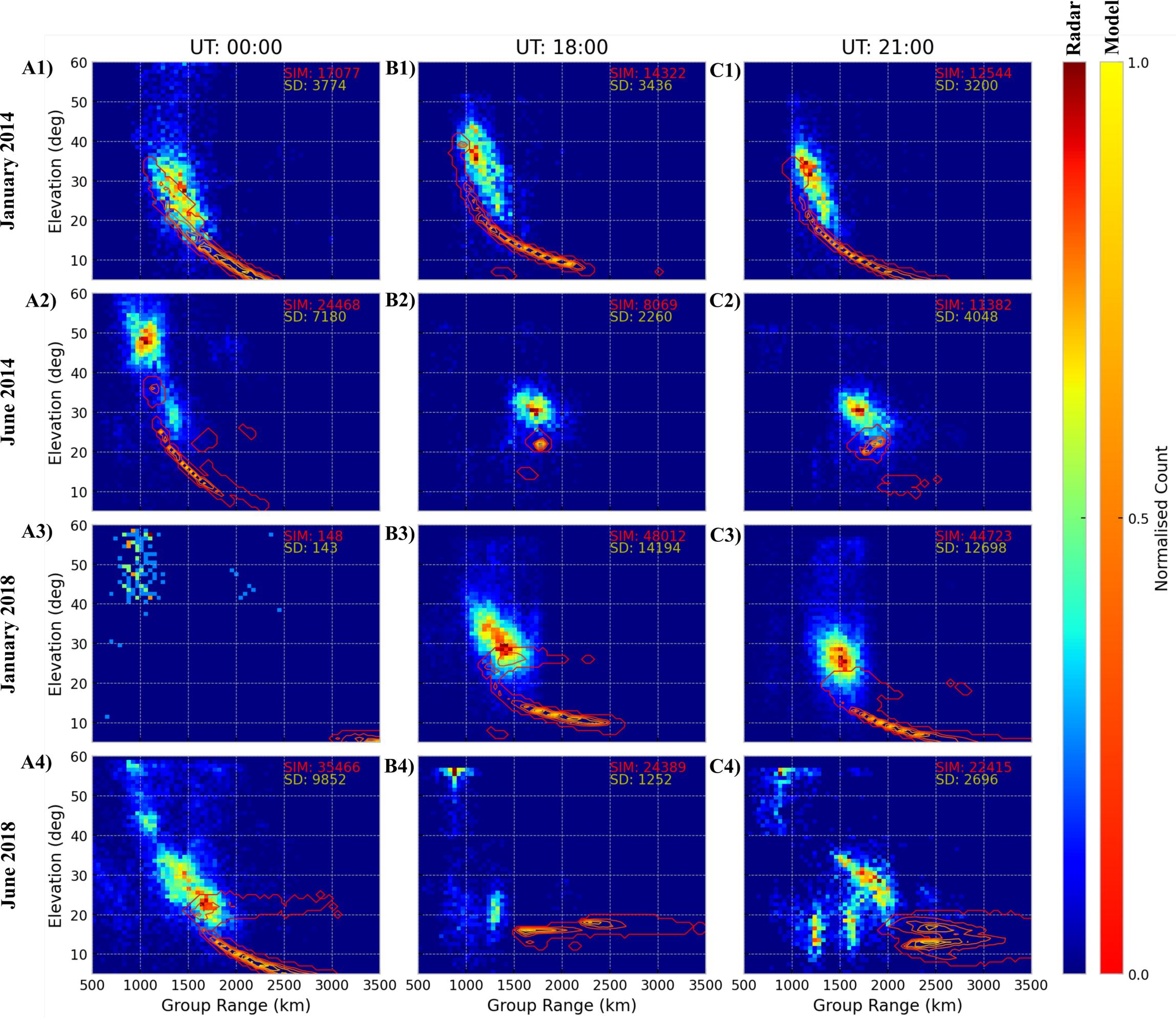


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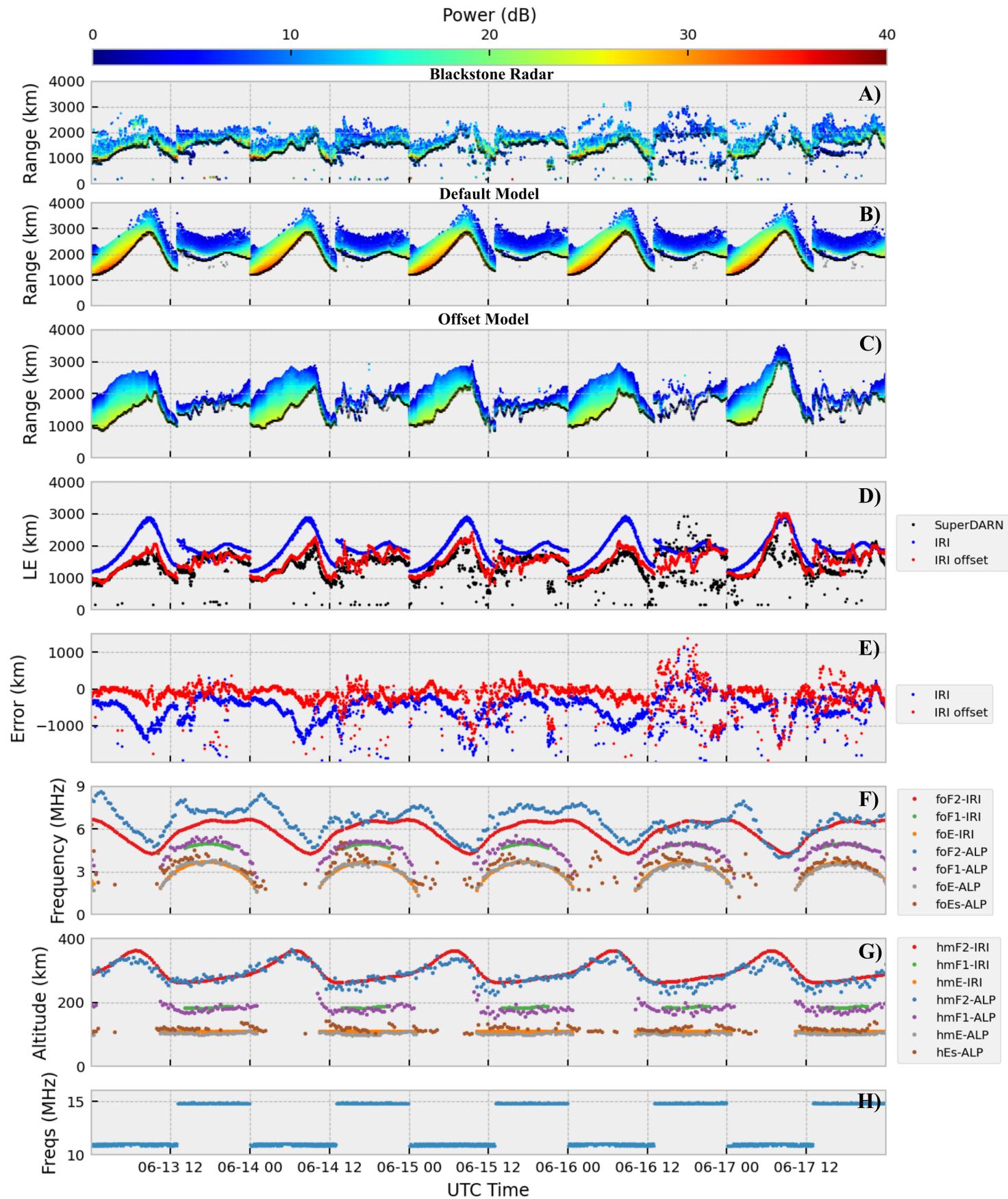


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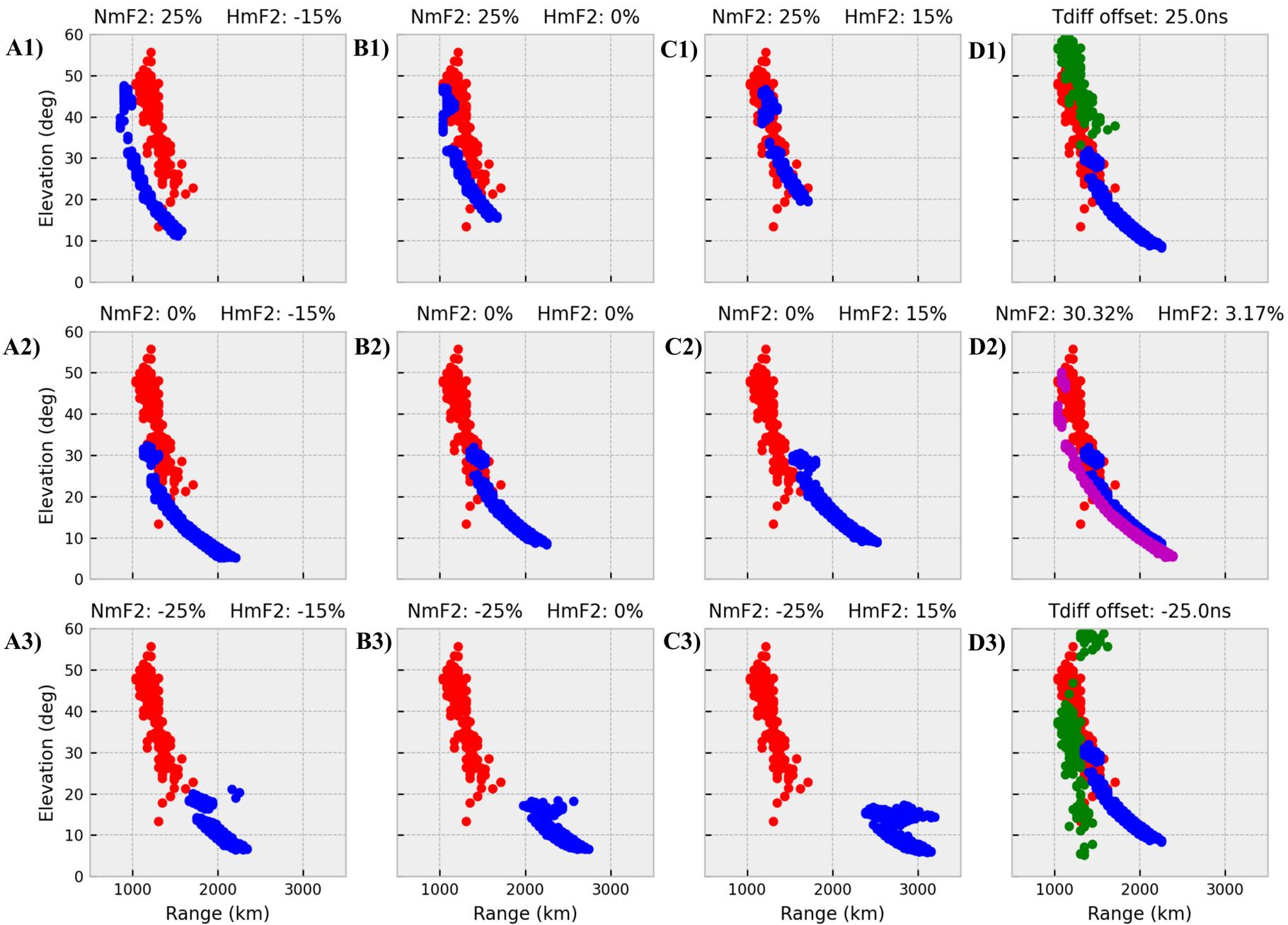


Figure A1.

